

# Determination of volumetric machine tool errors by using a hole-bar material standard (Multi-Feature Bar – MFB)

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le cnam



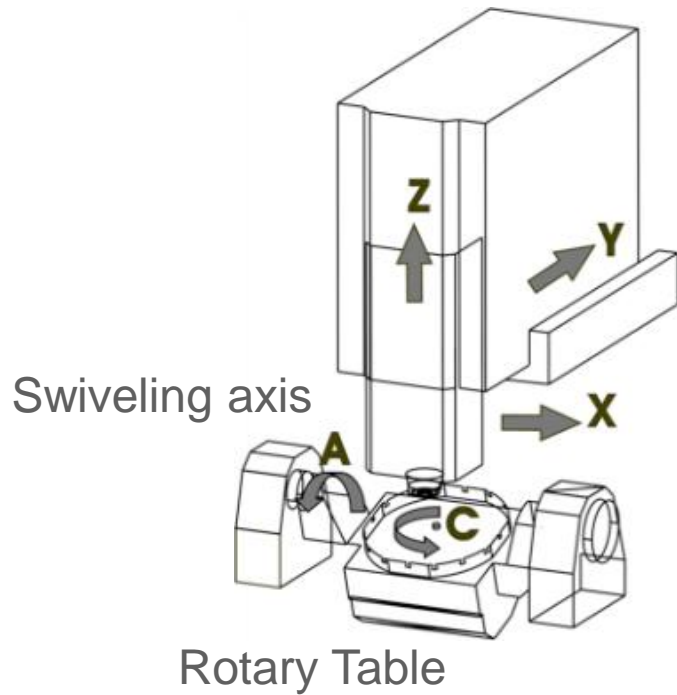
université  
PARIS-SACLAY

French National Metrology Institute LNE-Cnam  
Automated Production Research Laboratory of ENS Cachan – Univ Paris Saclay

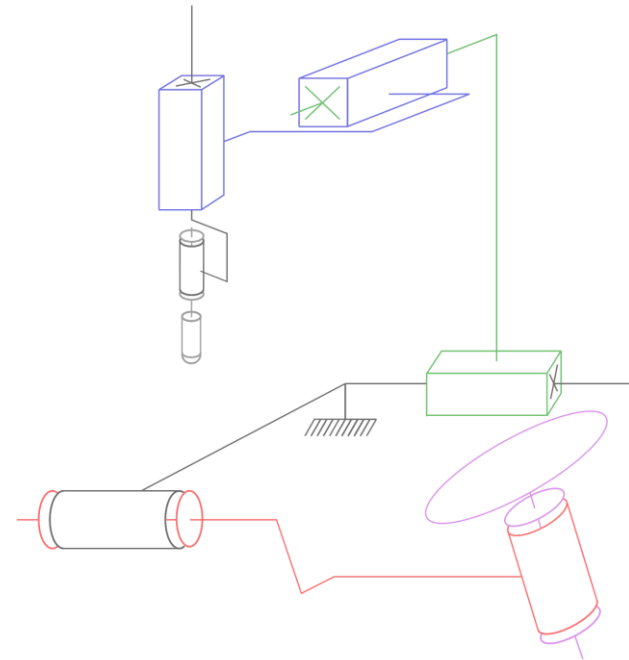
# Introduction : Volumetric accuracy



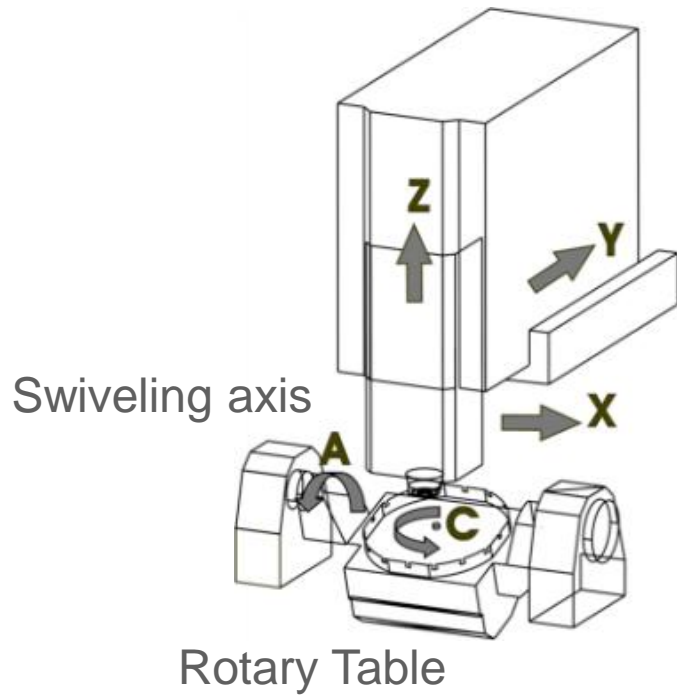
## 5-axis machine tool (Mikron UCP710 at LURPA)



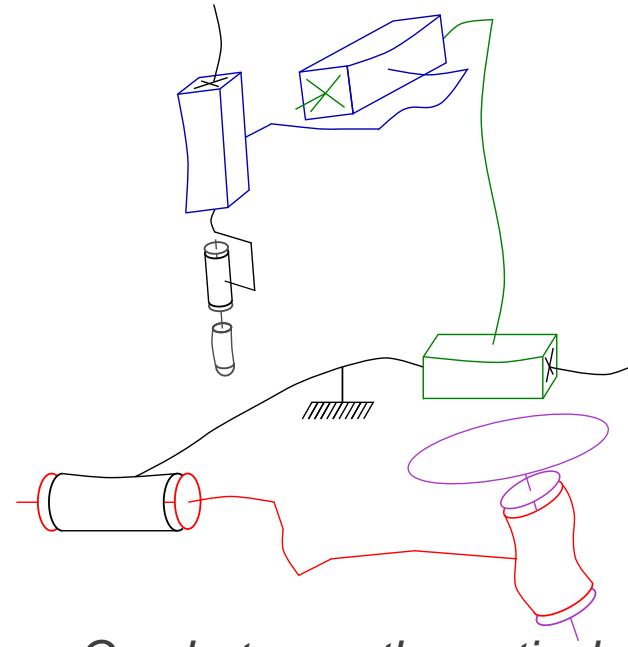
## Kinematic Architecture



## 5-axis machine tool (Mikron UCP710 at LURPA)



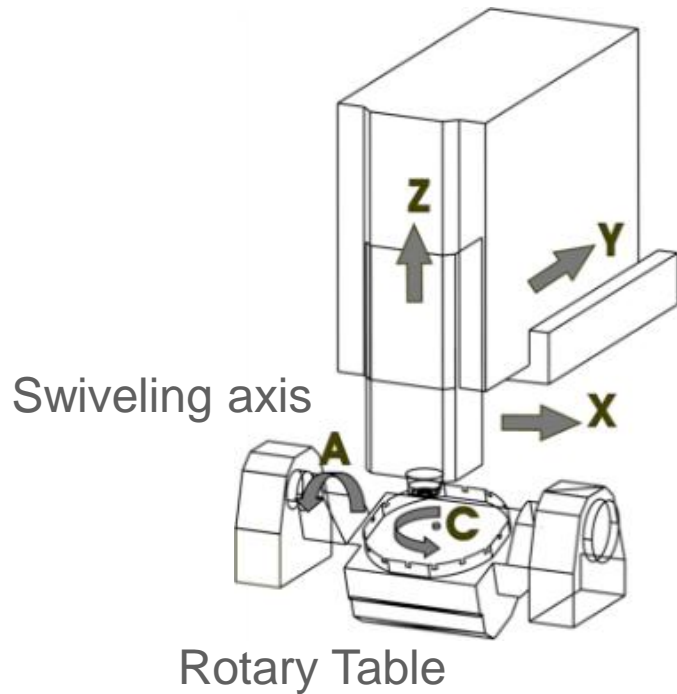
## Kinematic Architecture



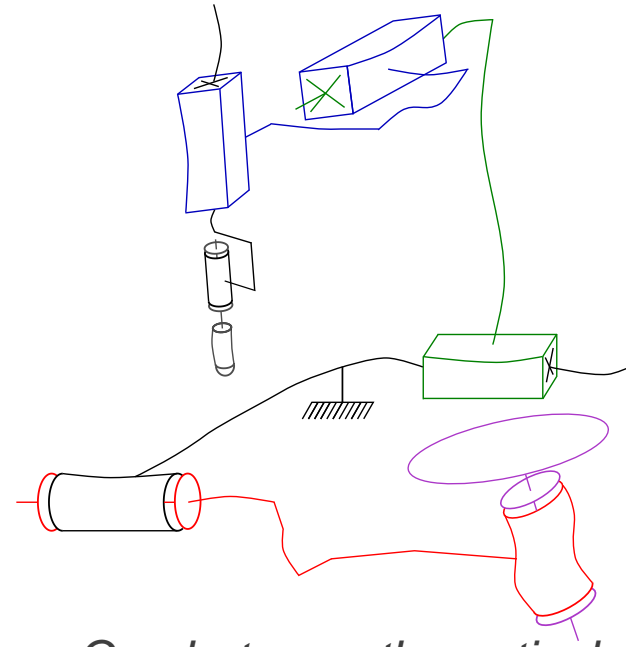
Gap between theoretical  
kinematic and real kinematic



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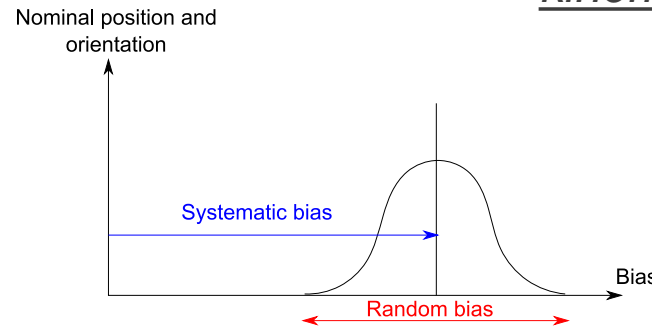


## Kinematic Architecture



### Gap between theoretical kinematic and real kinematic

### Causes of this effect:



- Geometric errors** → ~ 70% - 90%
- Thermo-mechanical phenomena
- Environmental hazards
- Dynamic forces
- Heats
- CNC
- Vibrations
- ...

[Mekid2012]  
[Schwenke2008]



# Introduction : Volumetric accuracy





Maximum range of relative deviations between actual and ideal position and maximum range of orientation deviations in the volume concerned, where the deviations are relative deviations between the tool side and the workpiece side of the machine tool [ISO230-1,2012]:

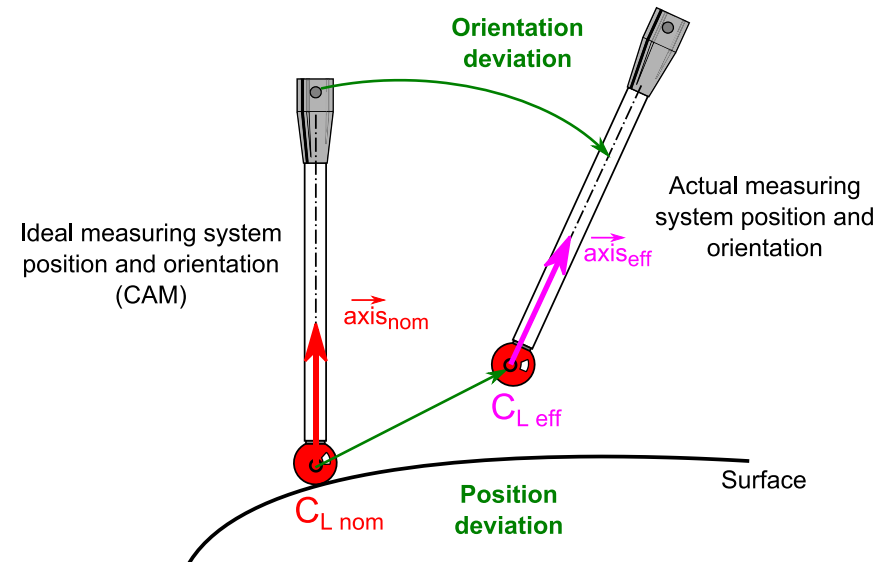
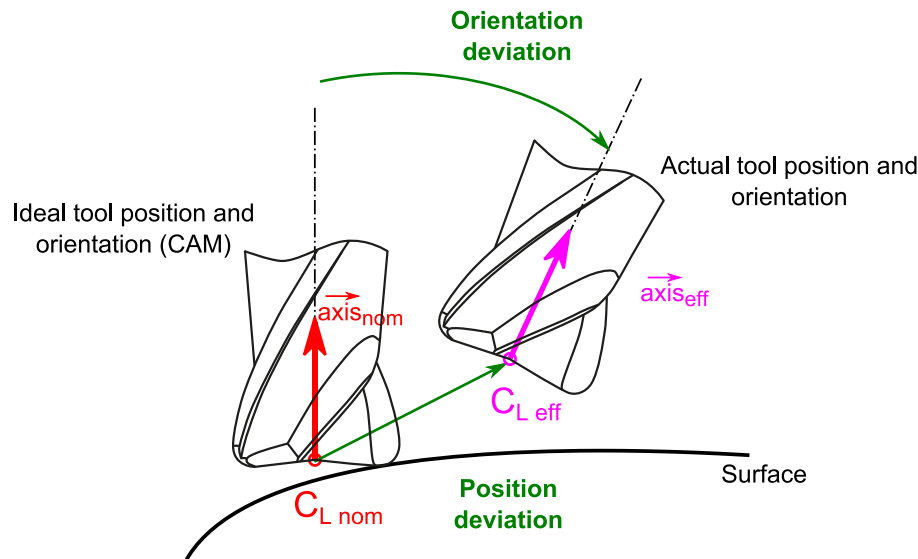
$$\begin{pmatrix} axes_{eff} - axes_{nom} \\ C_{Leff} - C_{Lnom} \end{pmatrix}_{6 \times 1} = \begin{pmatrix} \delta r \\ \delta u \end{pmatrix}_{6 \times 1} = V_{xyz}$$



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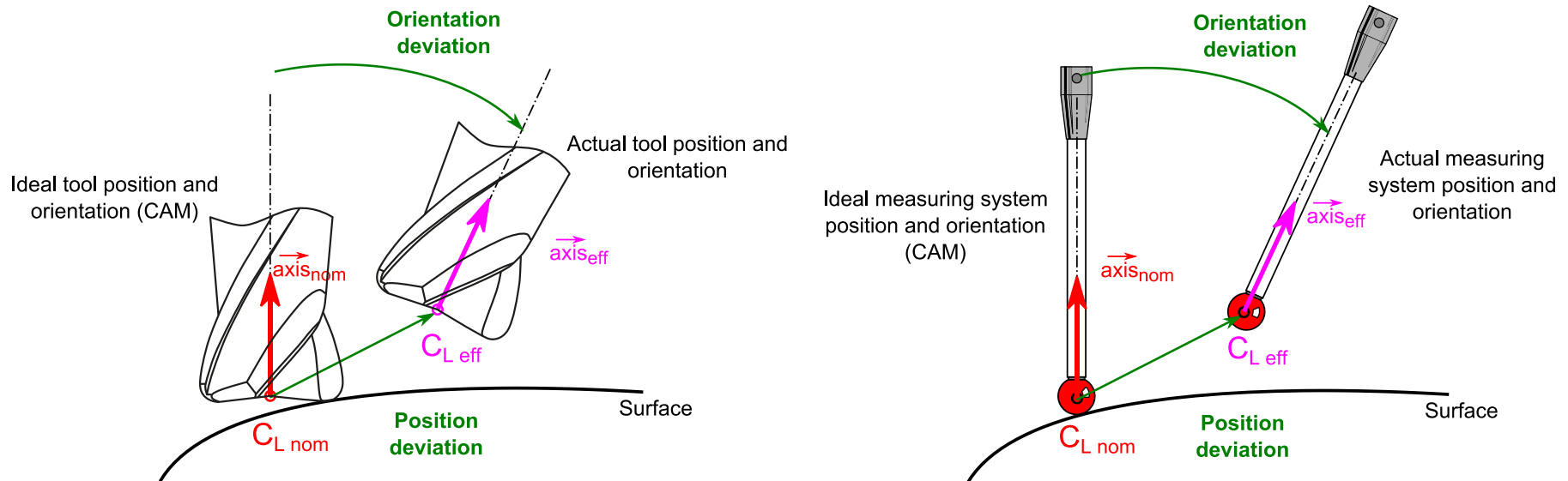
$$\begin{pmatrix} \vec{axis}_{eff} - \vec{axis}_{nom} \\ \vec{C}_{L_{eff}} - \vec{C}_{L_{nom}} \end{pmatrix}_{6 \times 1} = \begin{pmatrix} \delta r \\ \delta u \end{pmatrix}_{6 \times 1} = V_{xyz}$$





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The aim of this study is to develop a novel material standard to identify motion errors:

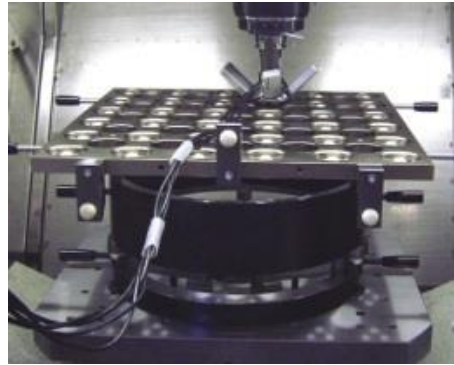
- Usable on CMM, **3 or 5 machine tool**, by **on-line measurement**, to insure **traceable and accurate results**
- With large field of its application: **Metrology room or Manufacturing shop**



# Introduction : Literature review



Hole plate  
[Trapet1991]



Ball plate  
[Bringmann2009]

1



Hole Bar  
[Lim2005]

3



Ball Bar  
[Zhang1991]



2

Conventional method [ISO 230], [ISO 10360], [ISO 10791], [ISO 13041], [ISO 3070]

4



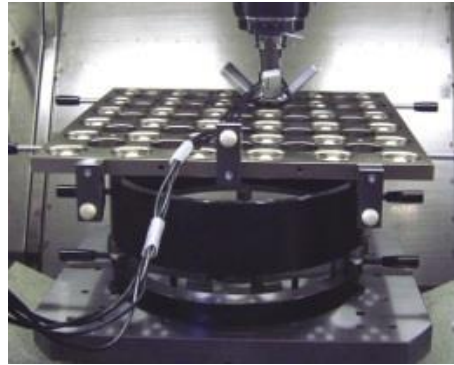
Laser Interferometry (On-line measurement)  
[Schwenke2005], [Chen1999]



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Hole plate  
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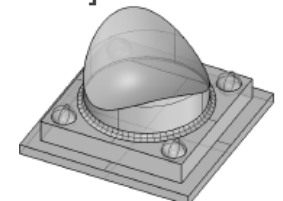
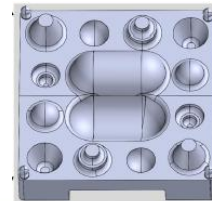
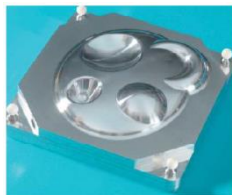
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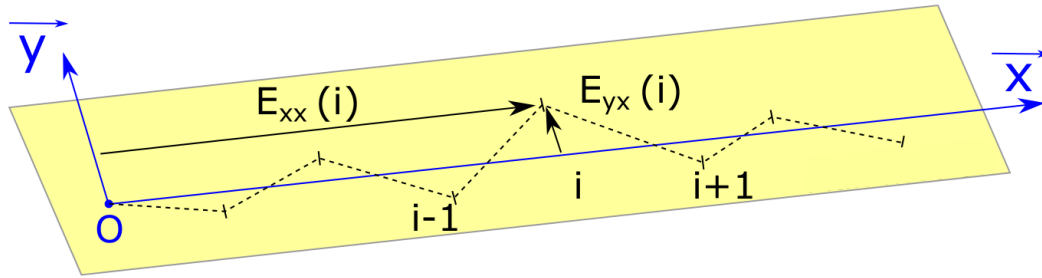


Laser Interferometry (On-line measurement)  
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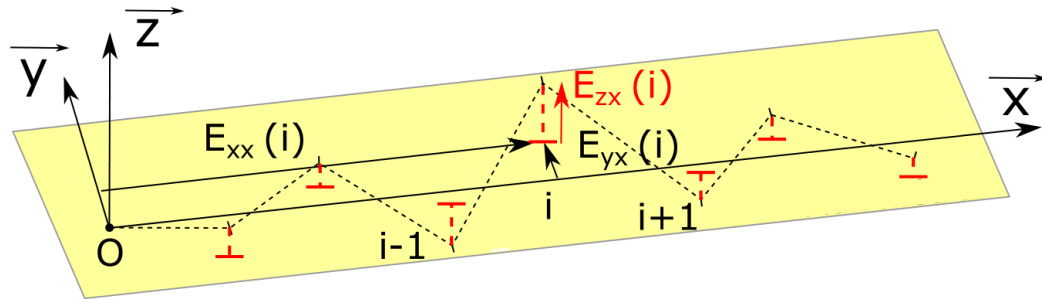


Actual Hole-Bar in litterature:

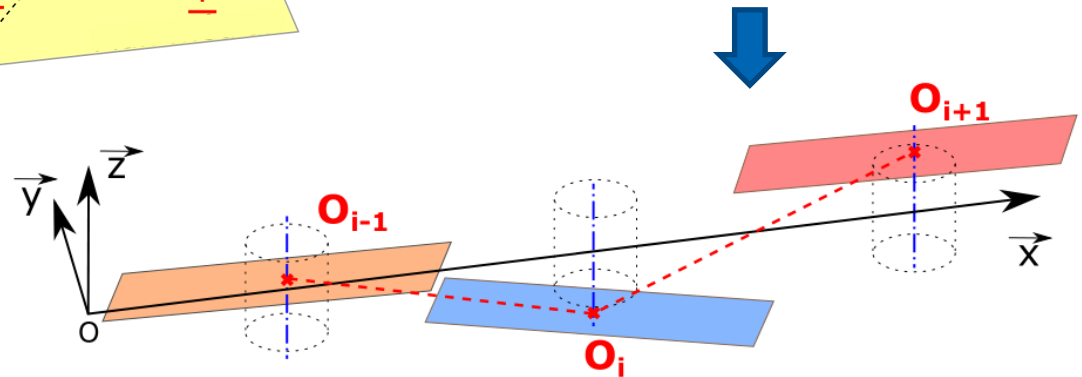


- ➔ One linear positioning error  $E_{xx}$
- ➔ One linear positioning error  $E_{xx}$  and one horizontal straightness  $E_{yx}$

Identification of an additional parameter:



- ➔ One linear positioning error  $E_{xx}$  and two straightnesses  $E_{yx}$  and  $E_{zx}$



Development of a novel Hole-Bar with patterns  
 ➔ maximization of the number of geometric errors to identify for each position of the Hole-Bar



- **Development of the Novel Hole-Bar**
  - Principle
  - Technical attributes
- **Calibration**
  - Reversal technique
  - Intercomparison
- **Application on Machine tool**
  - Measurement process
  - Geometric model
  - Results
- **Conclusion**

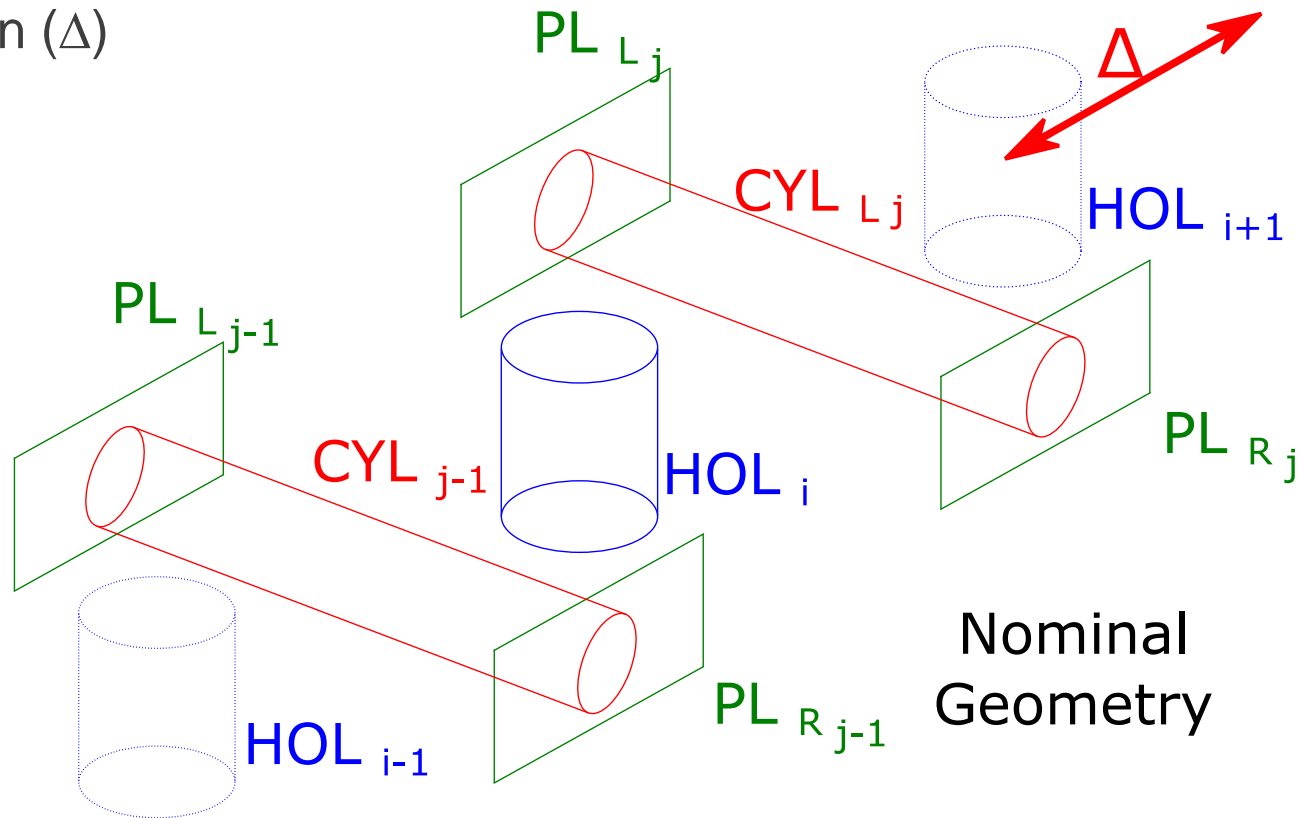


The design of the Hole-Bar consists in a repetition of a 3D pattern in one direction ( $\Delta$ )

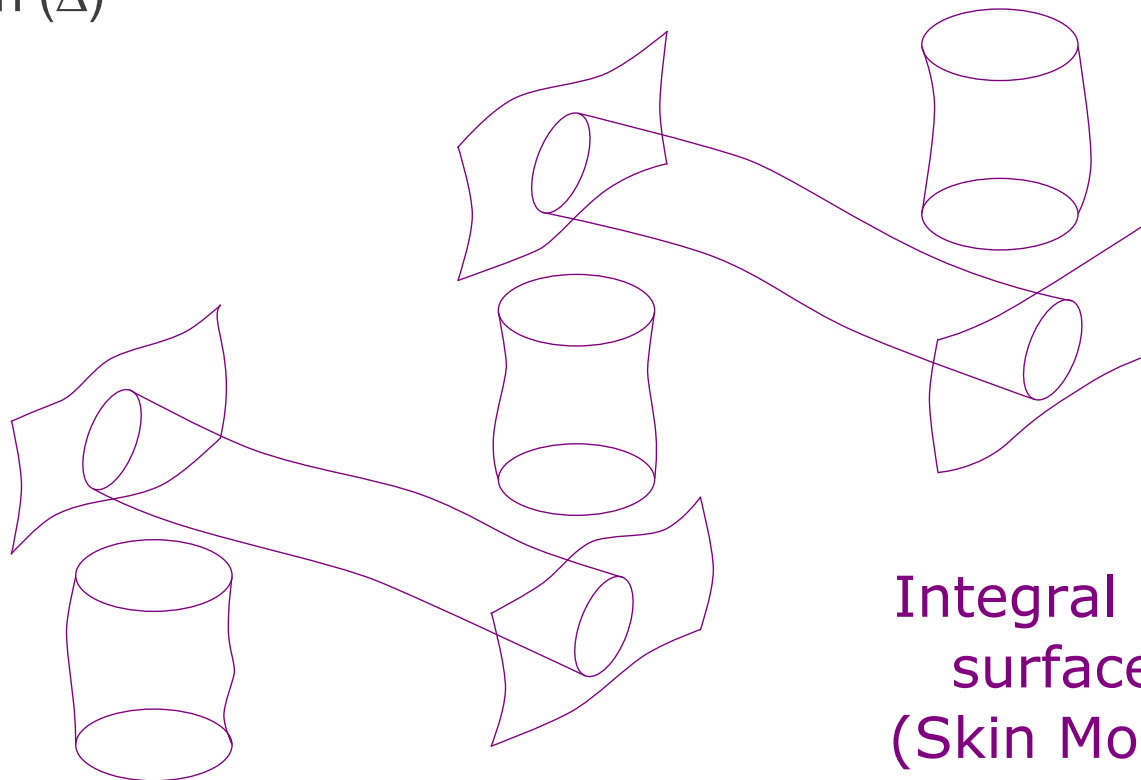




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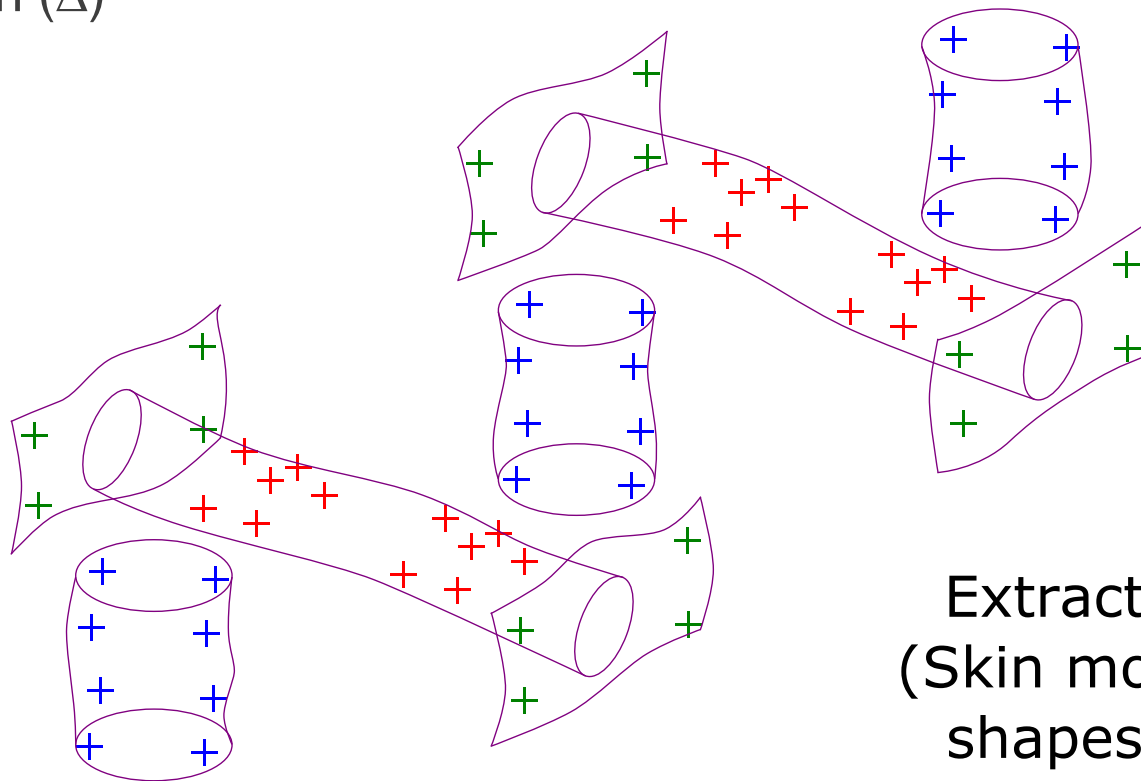


Integral real  
surfaces  
(Skin Model)

[ISO 5459:2011]



The design of the Hole-Bar consists in a repetition of a 3D pattern in one direction ( $\Delta$ )

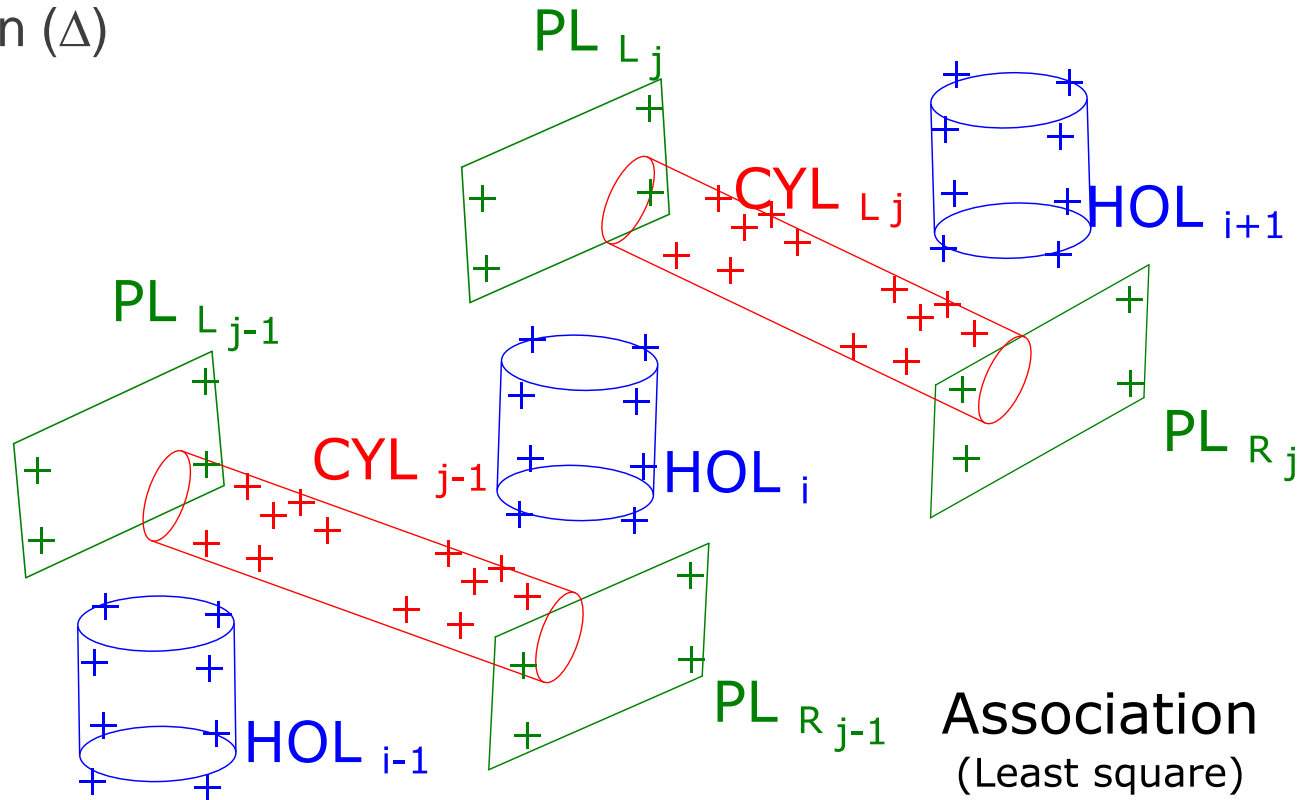


Extraction  
(Skin model  
shapes)

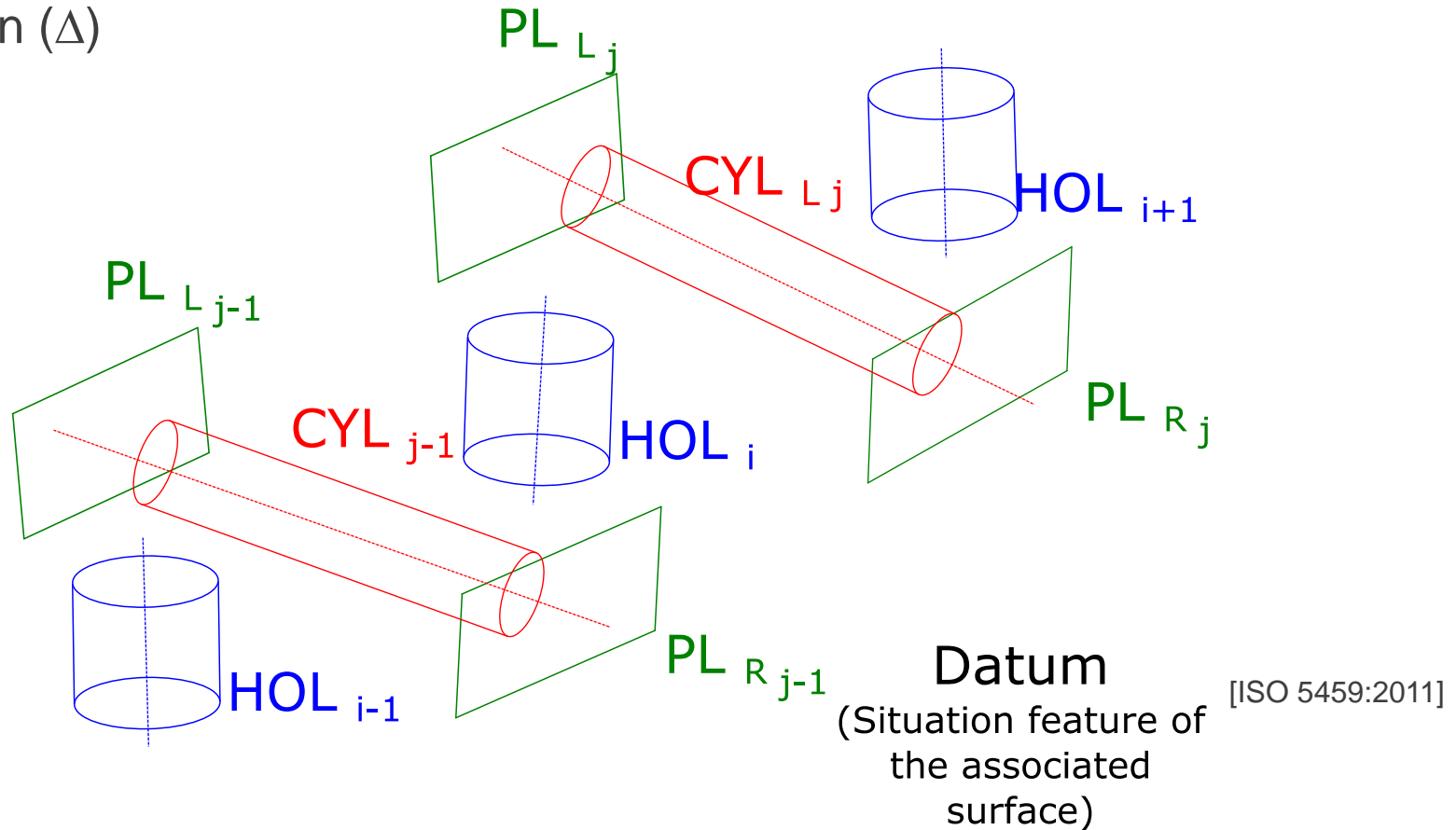
[ISO 5459:2011]



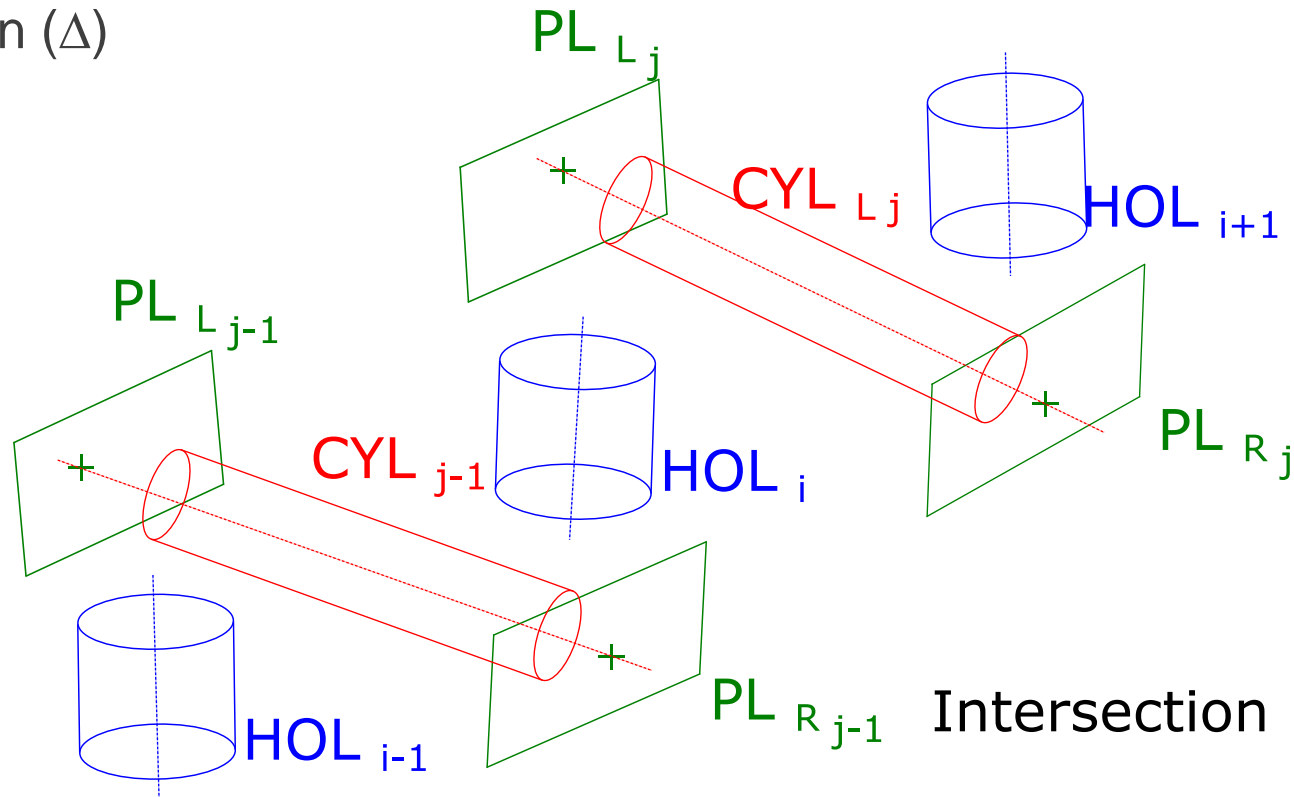
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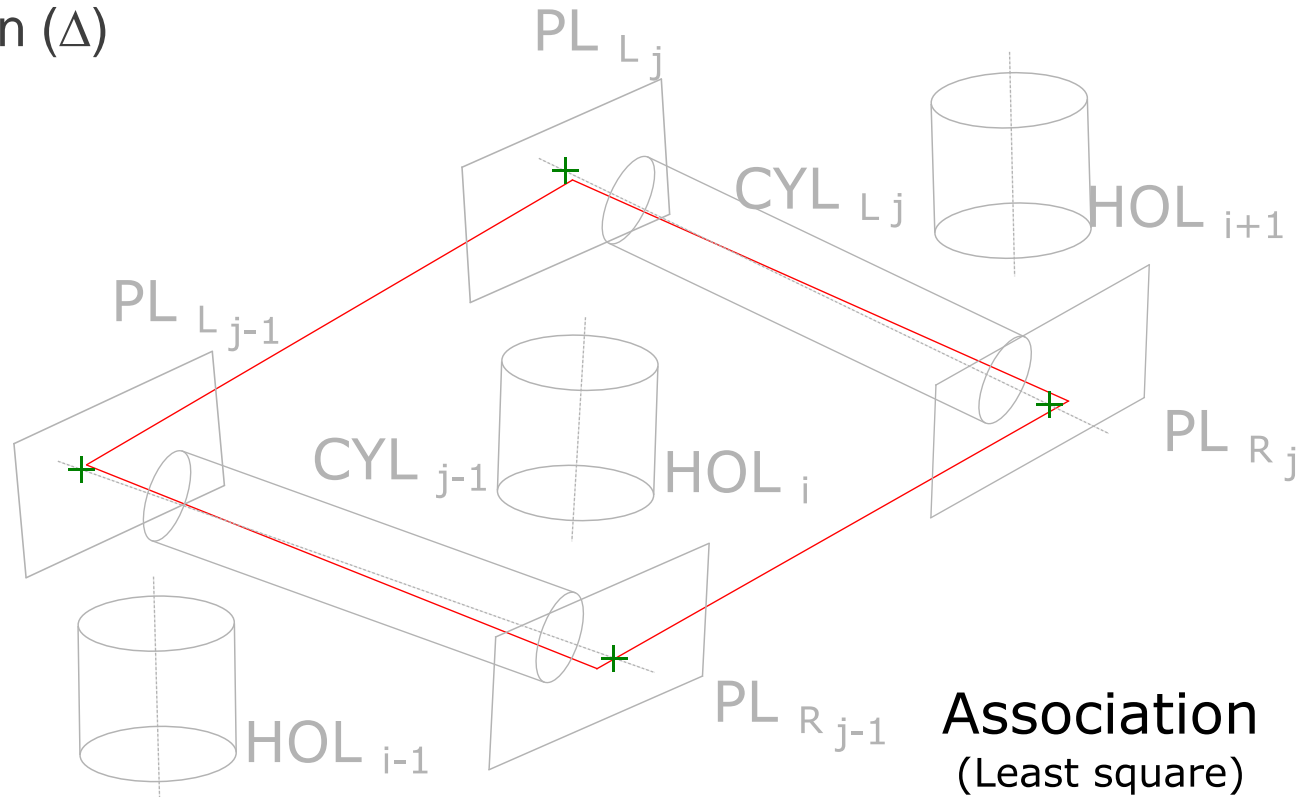


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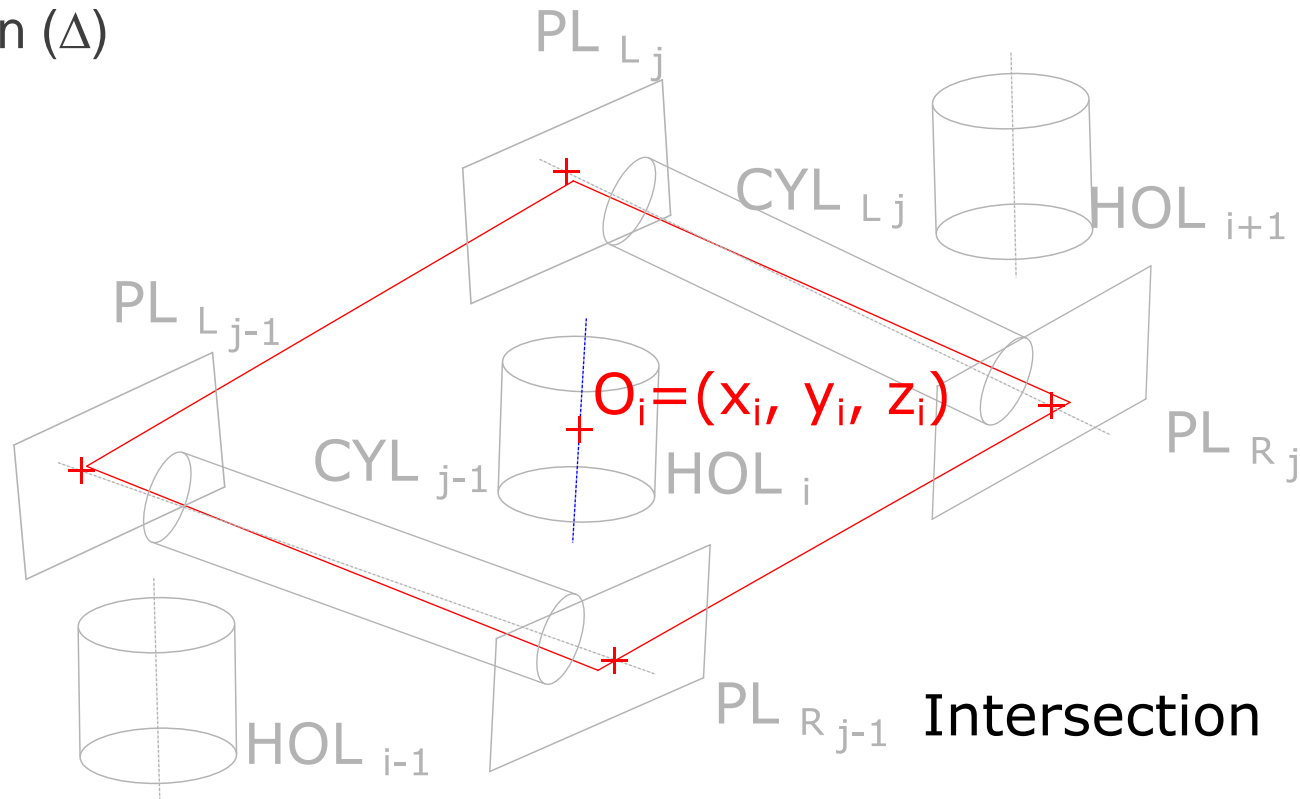




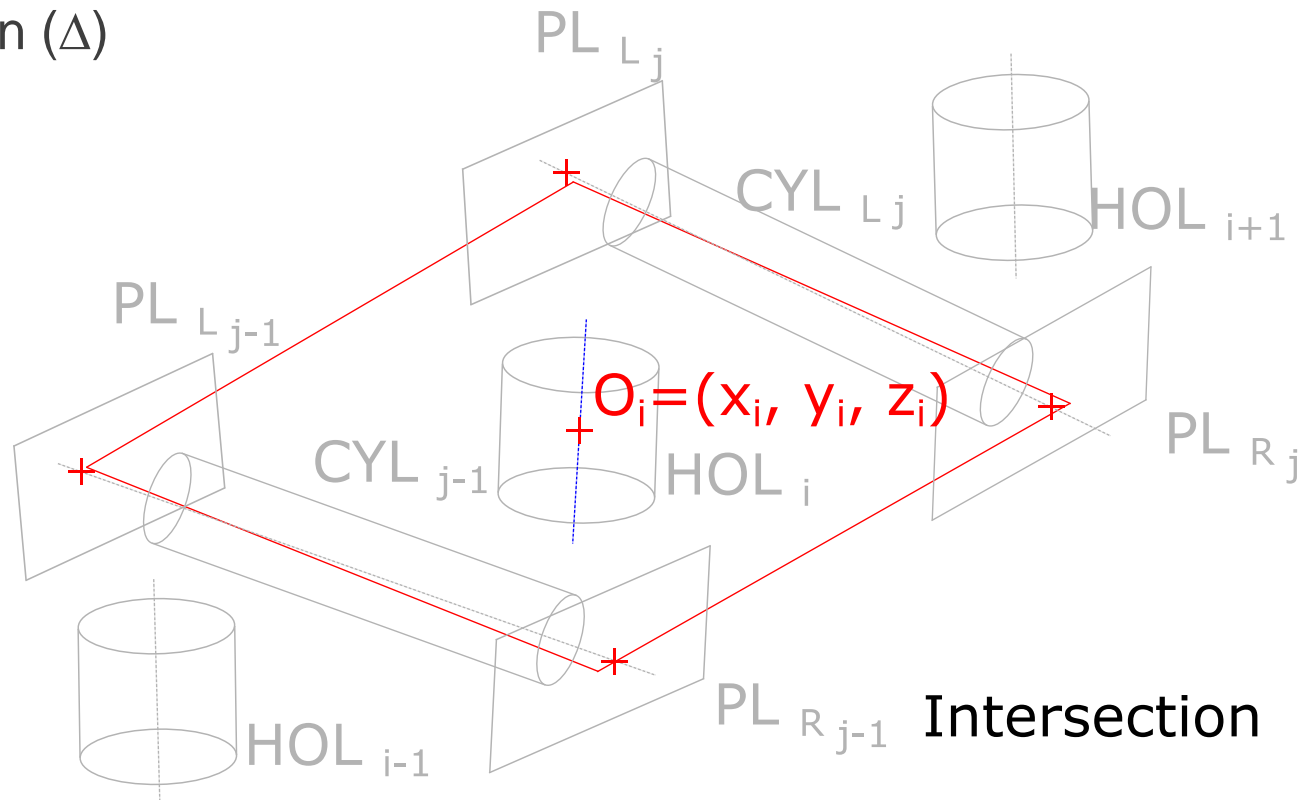
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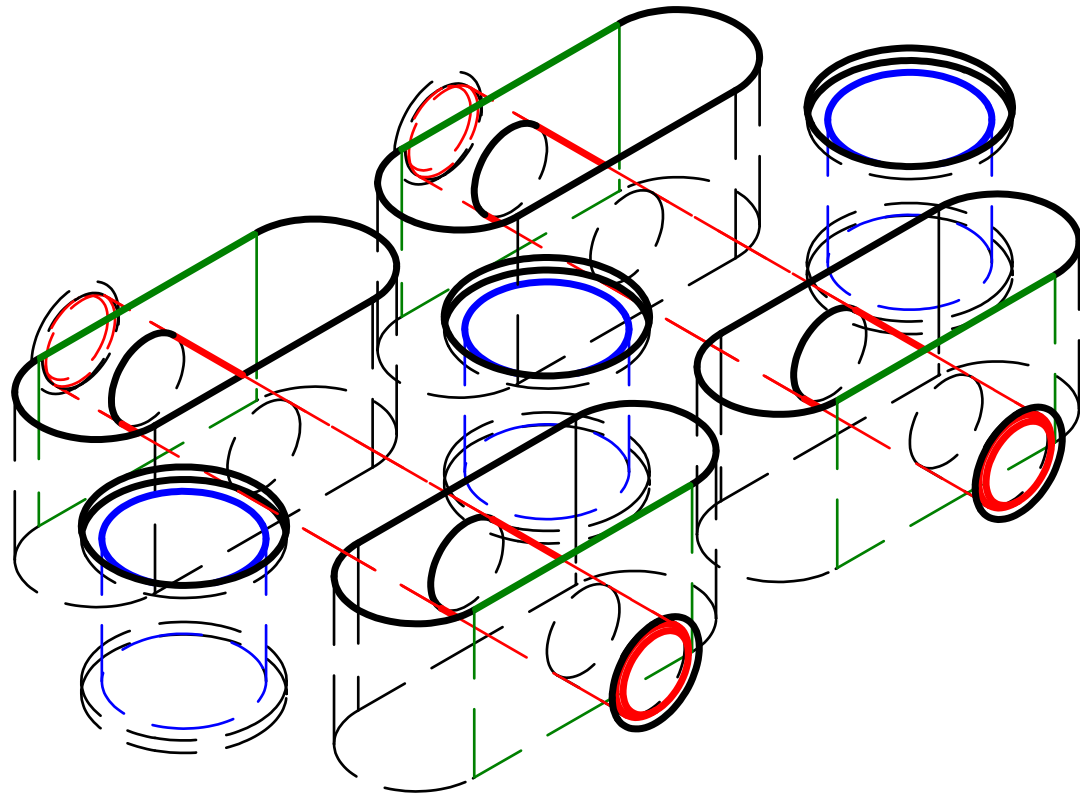


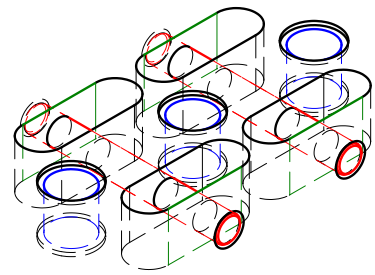
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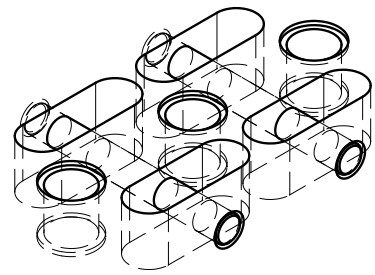


The identified points  $O_i = (x_i, y_i, z_i)$  offers 3 intrinsic geometric parameters: 1 linear positioning and 2 straightnesses

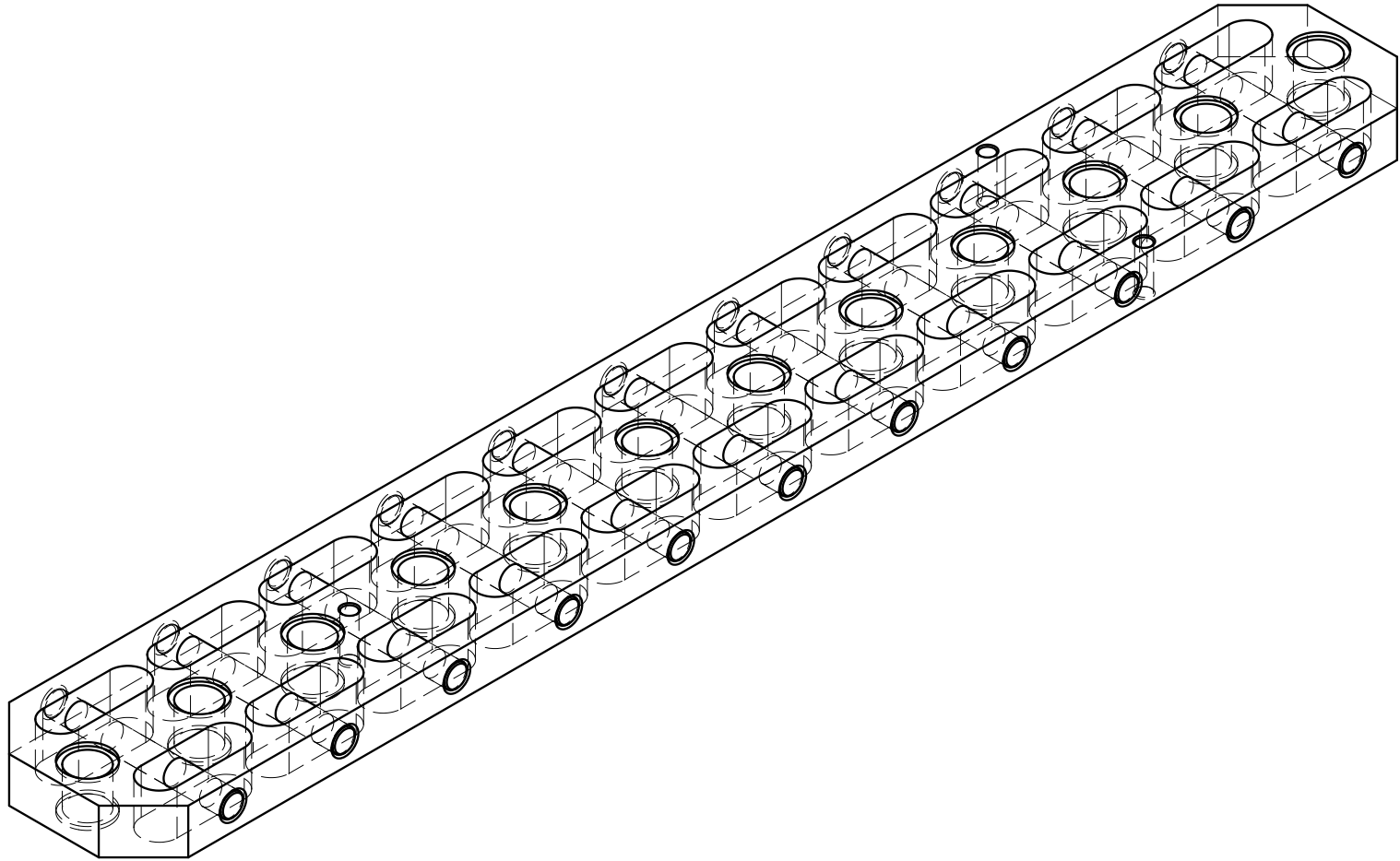


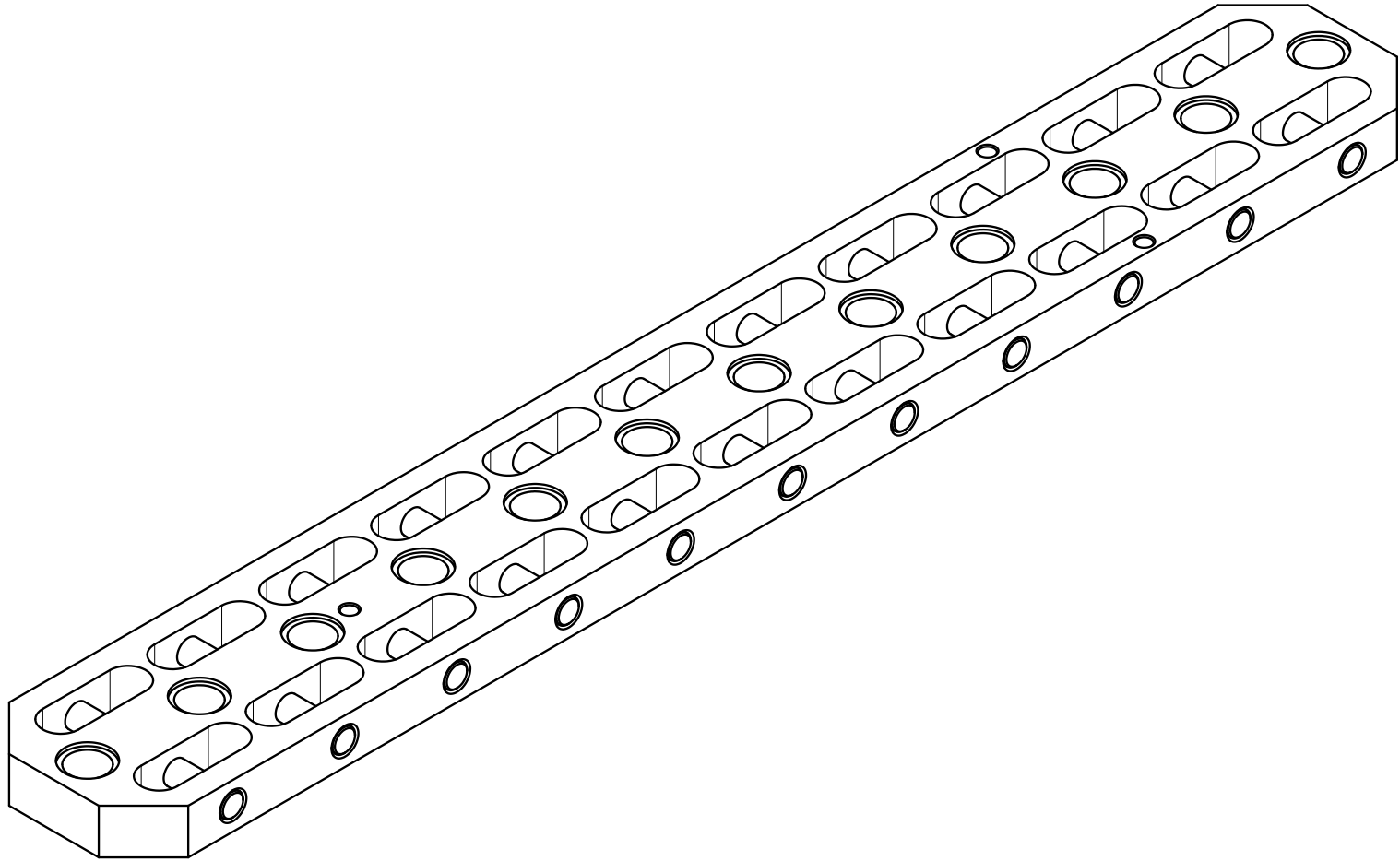


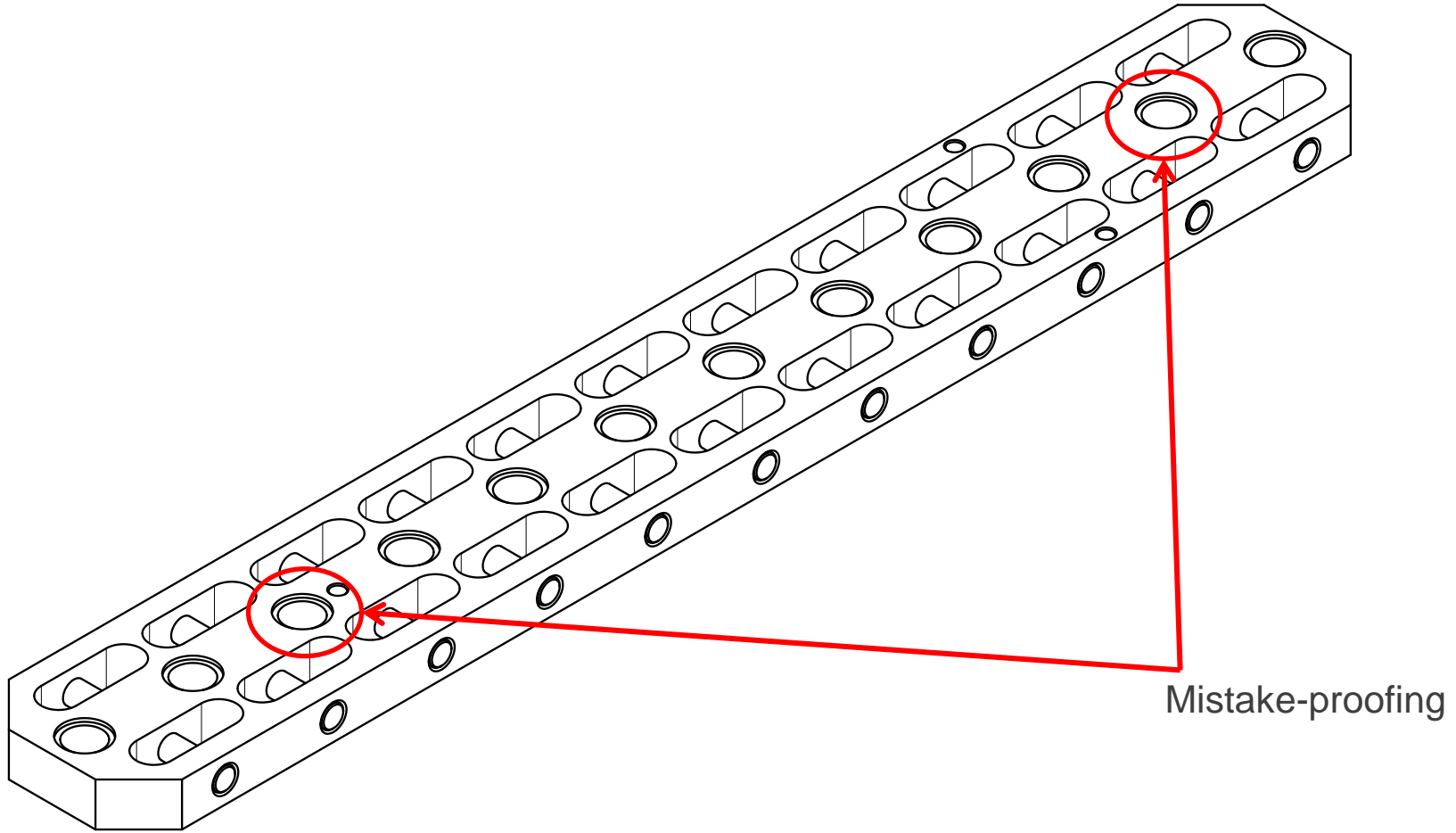


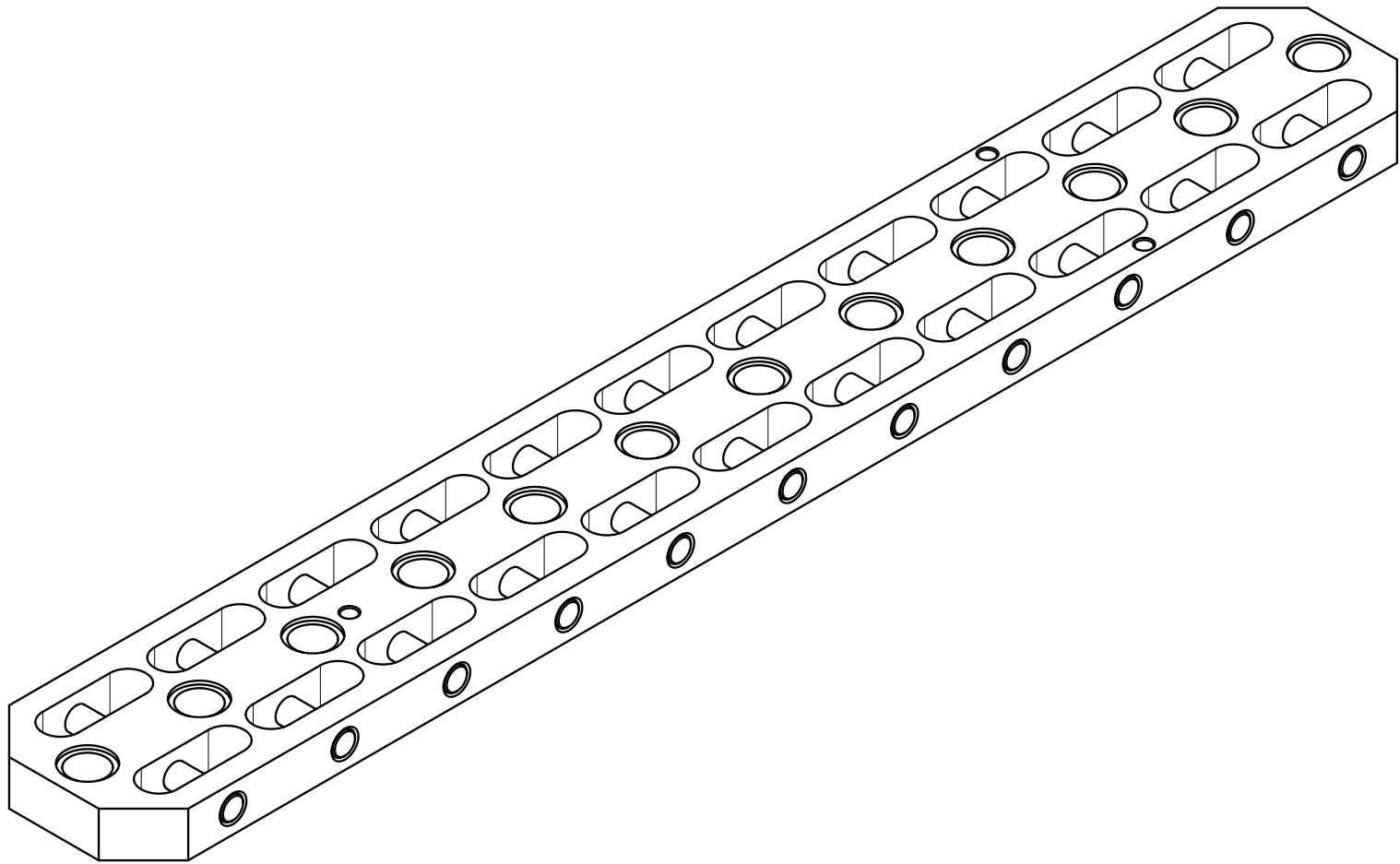


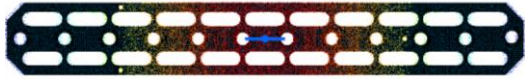




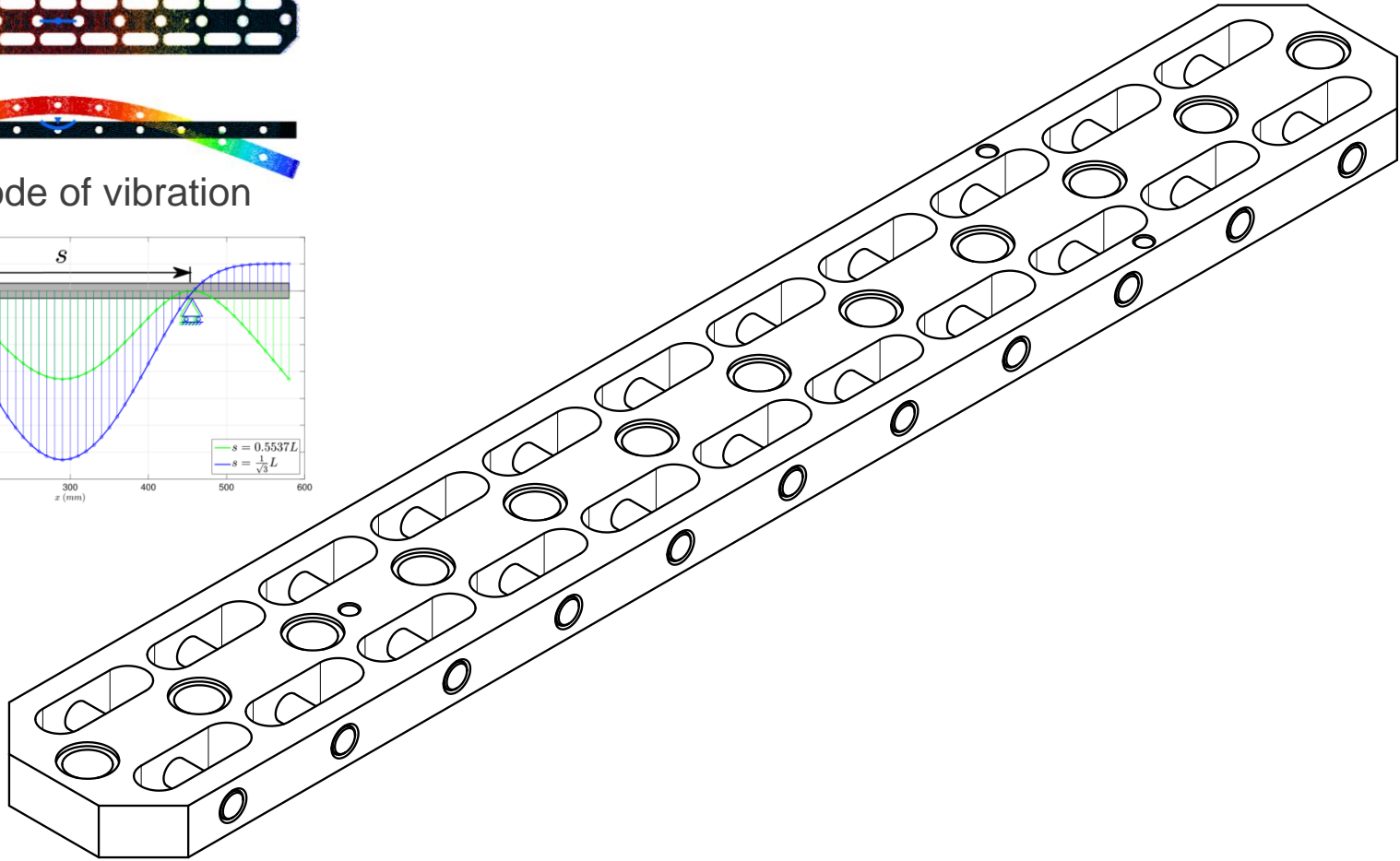
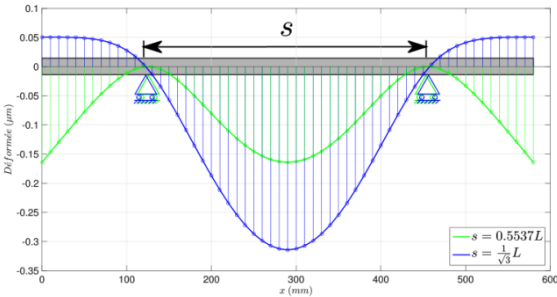




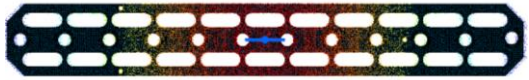




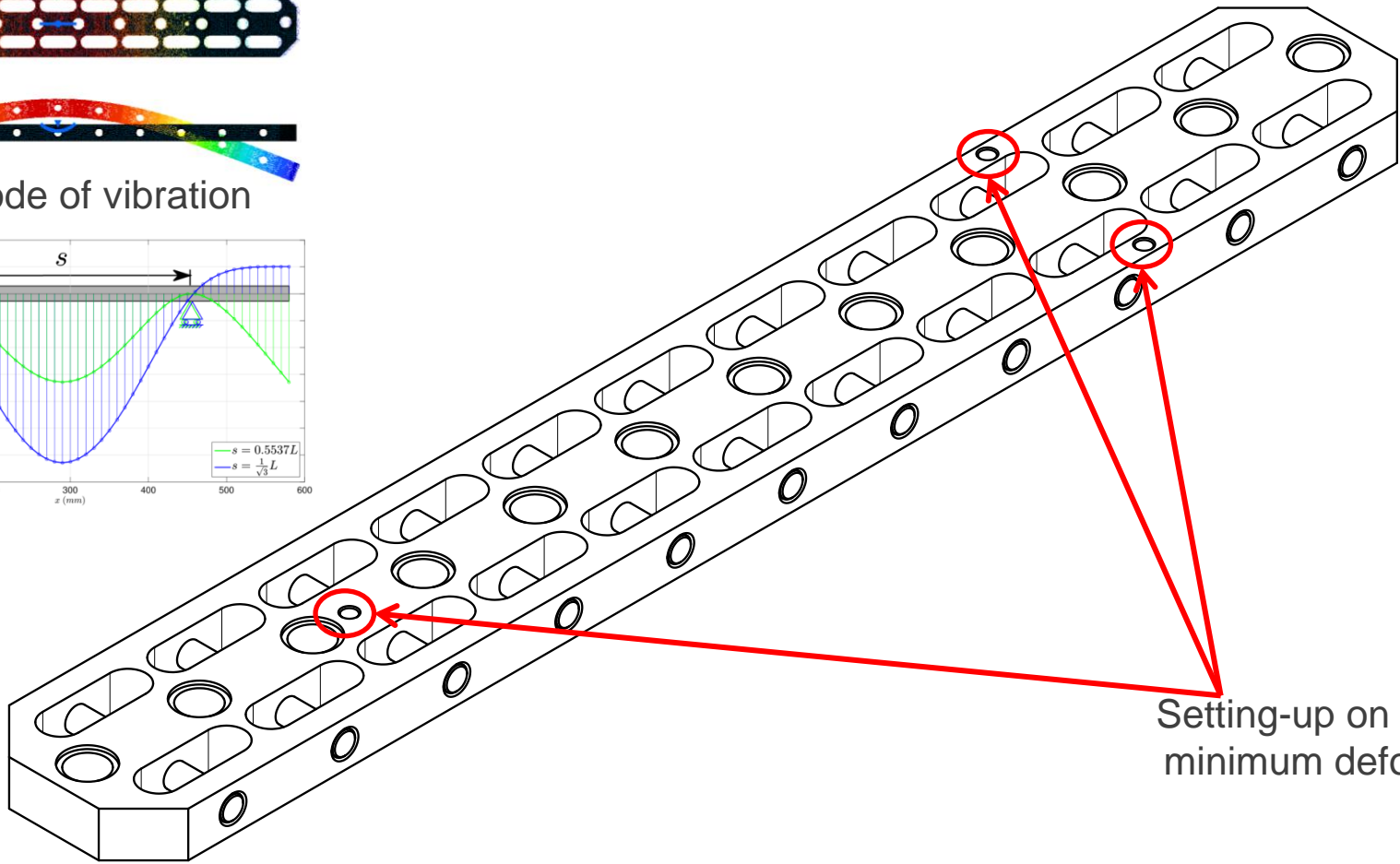
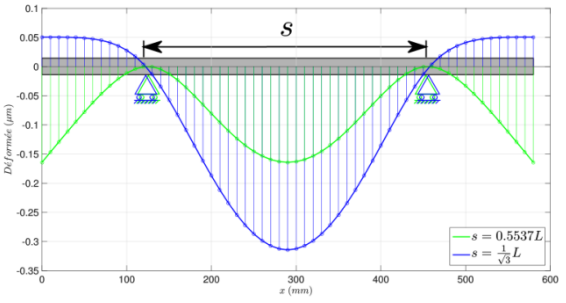
First mode of vibration







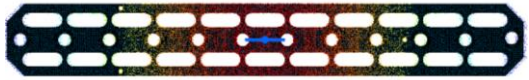
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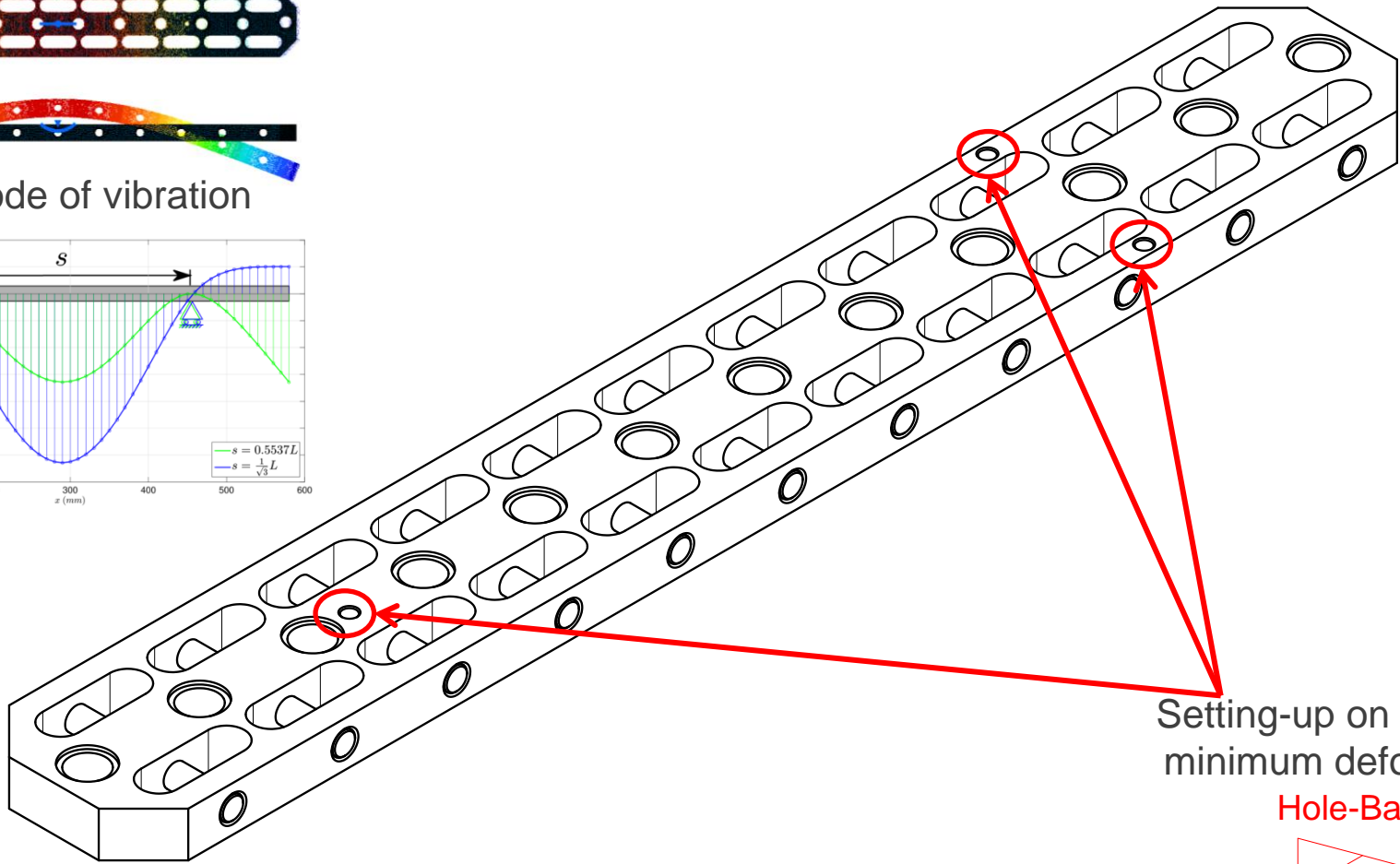
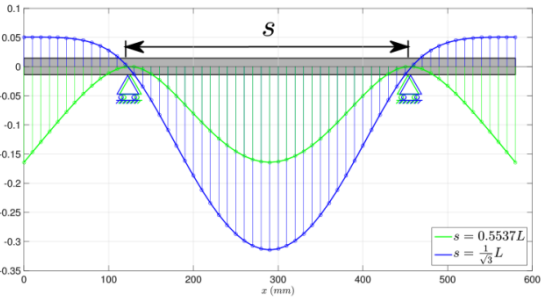
Setting-up on points of minimum deformation



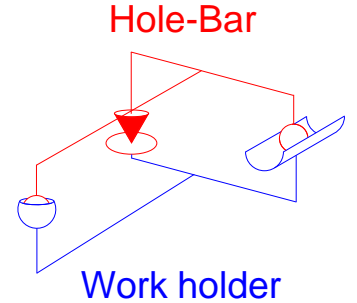




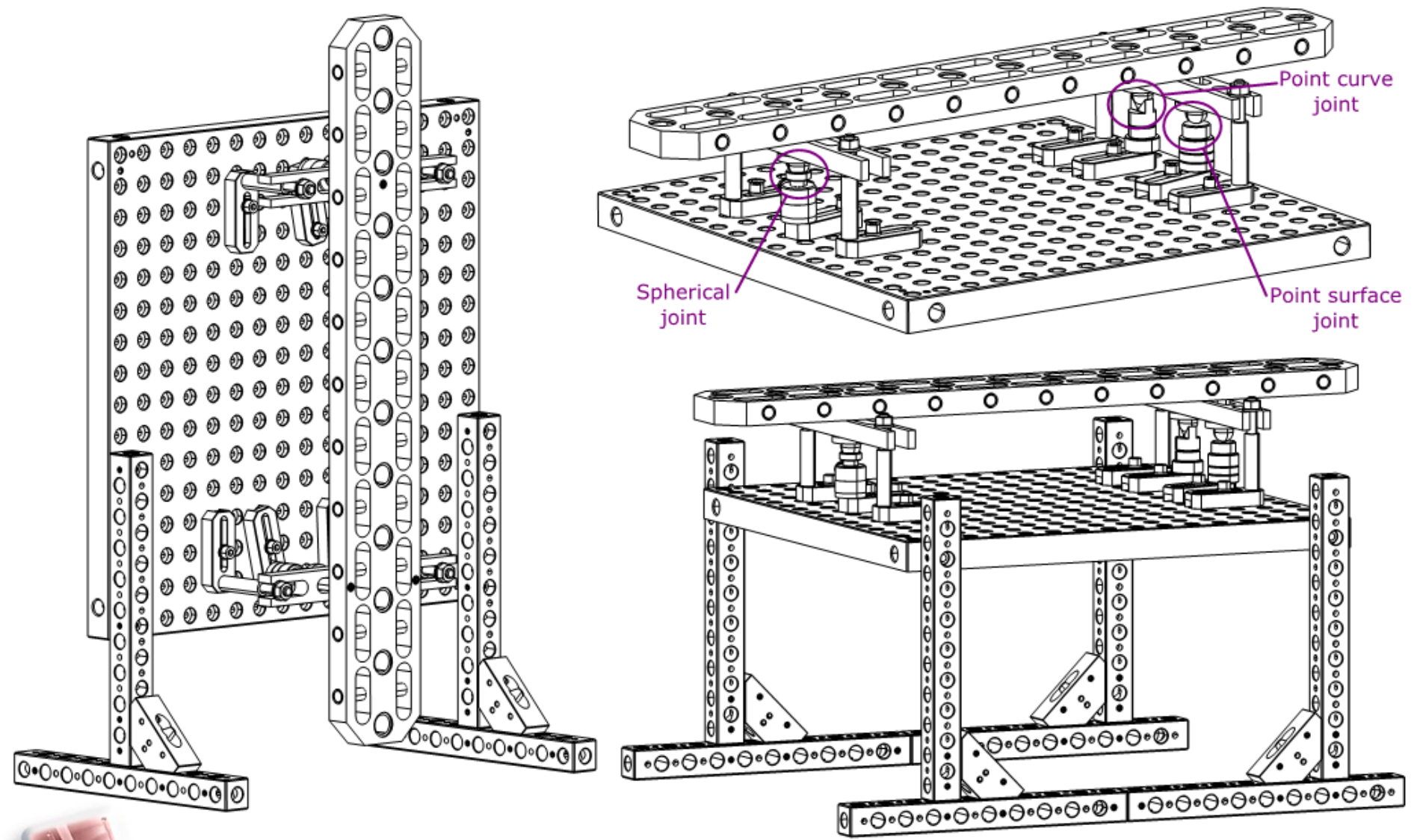
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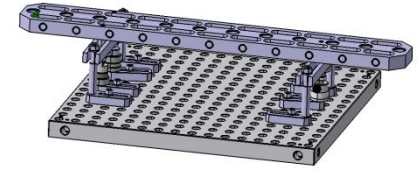






Nominal coordinates (3D-CAD model)

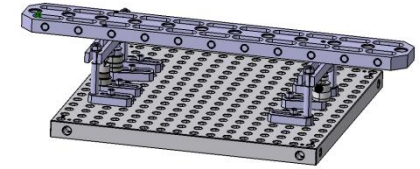
$$\forall i \in \llbracket 1 ; N \rrbracket, \begin{pmatrix} x_i \\ y_i \\ z_i \end{pmatrix}_{R_{HB}} = \begin{pmatrix} (i-1) \times L \\ 0 \\ 0 \end{pmatrix}_{R_{HB}}$$





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Real coordinates (real geometry)

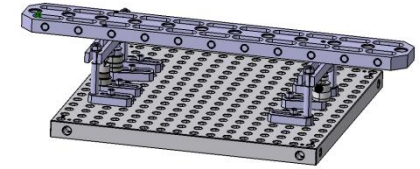
$$\forall i \in \llbracket 1 ; N \rrbracket, \begin{pmatrix} x_i \\ y_i \\ z_i \end{pmatrix}_{R_{HB}} = \begin{pmatrix} (i-1) \times L & + & E_{xx_{HB}}(i) \\ 0 & + & E_{yx_{HB}}(i) \\ 0 & + & E_{zx_{HB}}(i) \end{pmatrix}_{R_{HB}}$$





Nominal coordinates (3D-CAD model)

$$\forall i \in \llbracket 1 ; N \rrbracket, \begin{pmatrix} x_i \\ y_i \\ z_i \end{pmatrix}_{R_{HB}} = \begin{pmatrix} (i-1) \times L \\ 0 \\ 0 \end{pmatrix}_{R_{HB}}$$



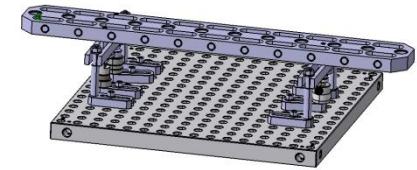
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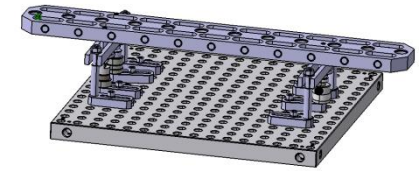
Calibration of the Hole-Bar on accurate  
CMM → insures traceable  
measurements on machine tool

The reversal technique and  
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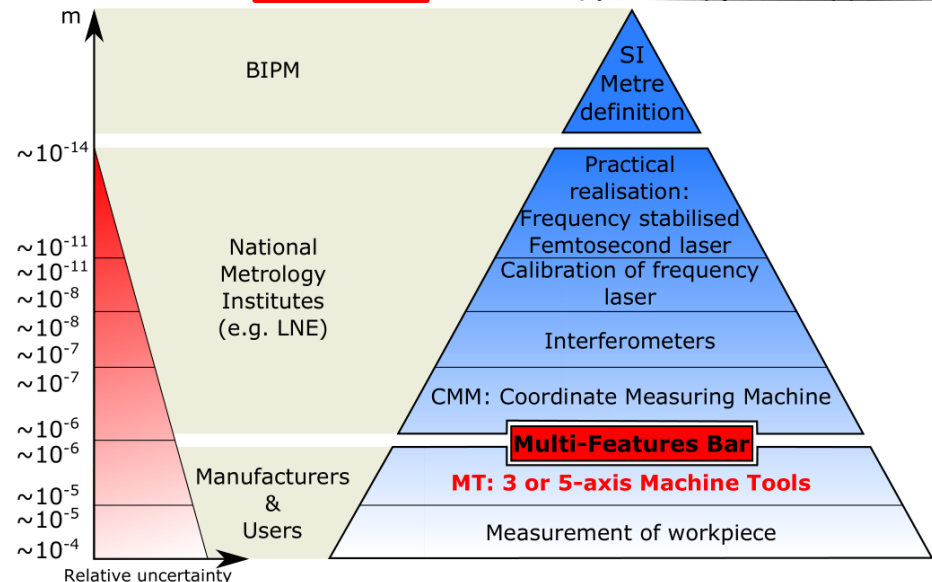
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$$\forall i \in \llbracket 1 ; N \rrbracket, \begin{pmatrix} x_i \\ y_i \\ z_i \end{pmatrix}_{R_{HB}} = \begin{pmatrix} (i-1) \times L + E_{xx_{HB}}(i) \\ 0 + E_{yx_{HB}}(i) \\ 0 + E_{zx_{HB}}(i) \end{pmatrix}_{R_{HB}}$$



Calibration of the Hole-Bar on accurate CMM → insures traceable measurements on machine tool

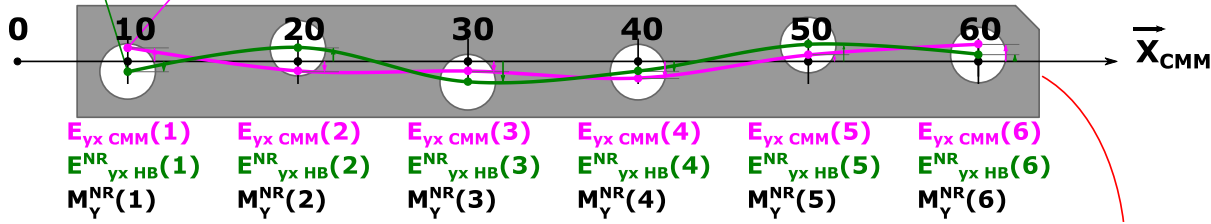
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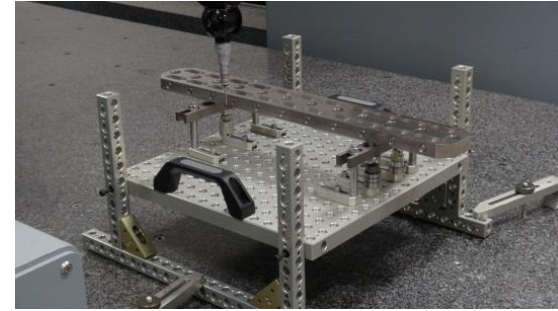
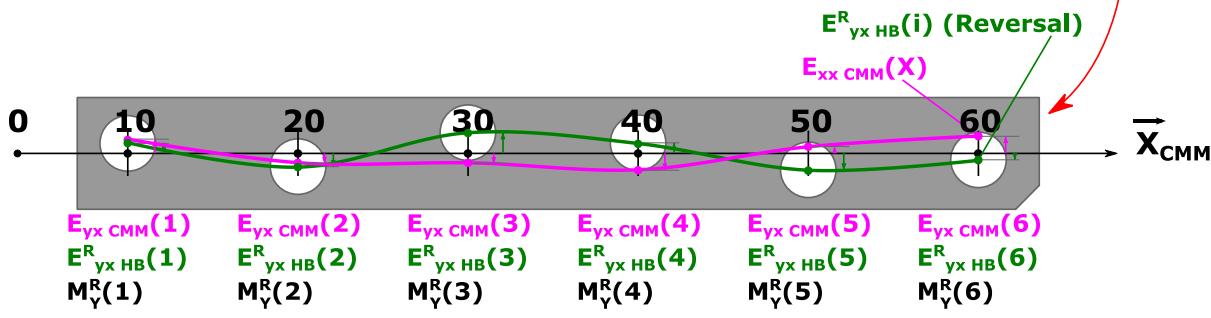
# Calibration: Reversal technique

$E_{yx HB}^{NR}(i)$  (No Reversal)  
*i* = Number of point of interest on Multi-Features Bar (HB)

$E_{xx CMM}(X)$   
*X* : Joint parameter of X-axis



Reversal way



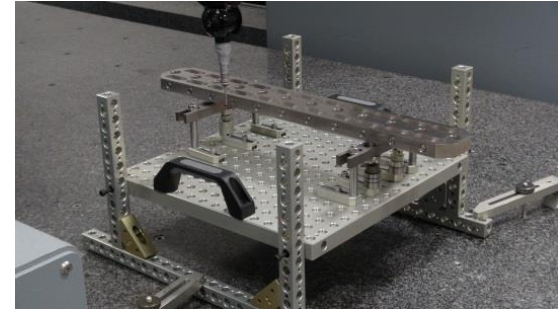
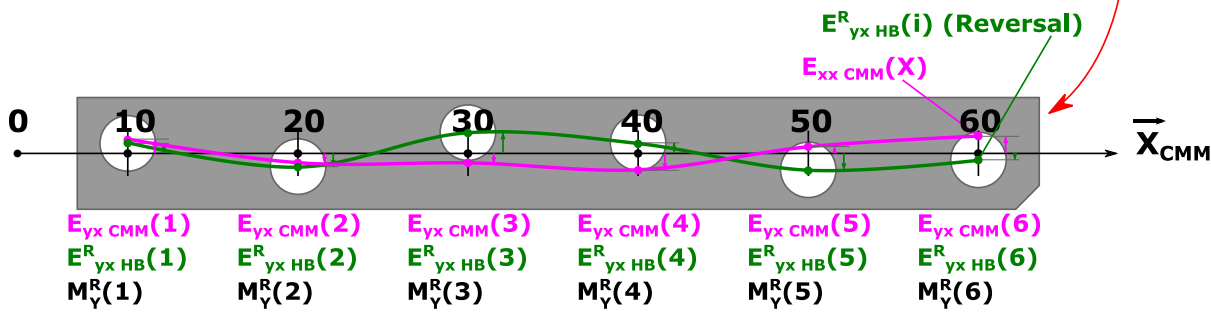
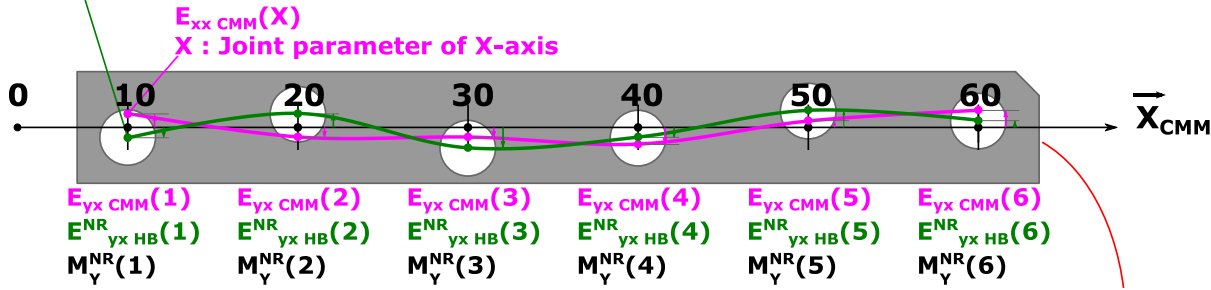
*MFB calibration set-up on CMM at LNE*





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*MFB calibration set-up on CMM at LNE*

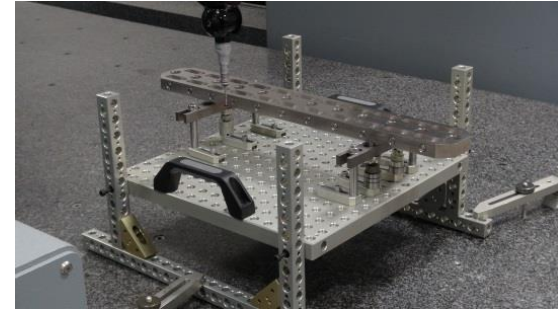
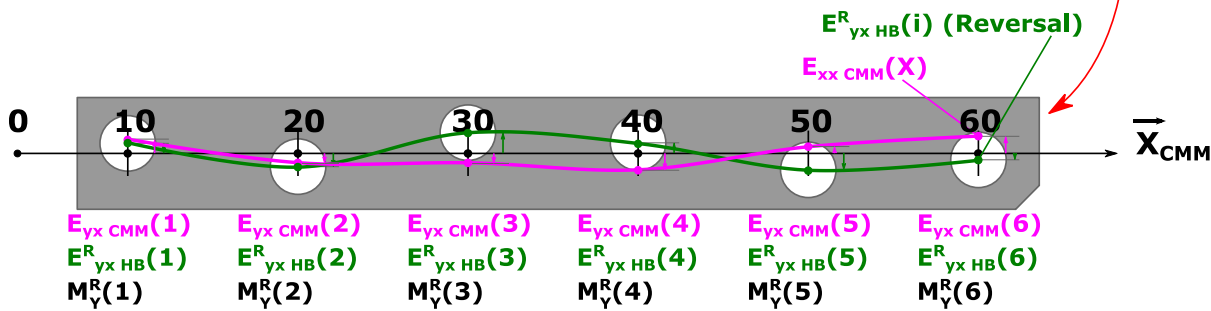
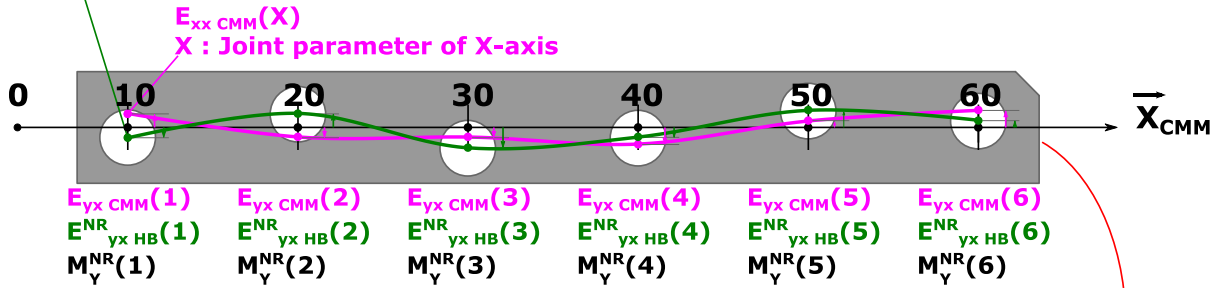
Linear positioning error along  $X_{HB}$

$$E_{xx HB}(i) = \frac{1}{2} \left[ M_x^{NR}(i) + M_x^R(i) \right] - (i-1) \times L - E_{XX CMM} - \epsilon_{ZZ CMM}$$



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$E_{yx HB}^{NR}(i)$  (No Reversal)  
*i* = Number of point of interest on Multi-Features Bar (HB)



*MFB calibration set-up on CMM at LNE*

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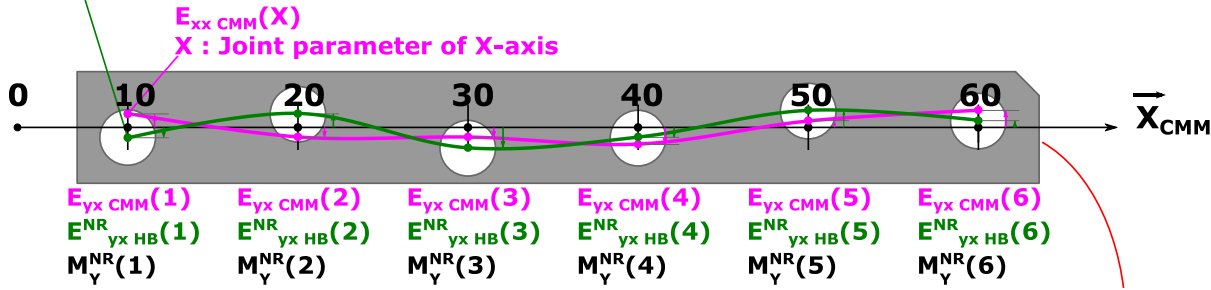
Measurement  
 Nominal geometry  
 Linear positioning error along  $Z_{CMM}$   
 Random error



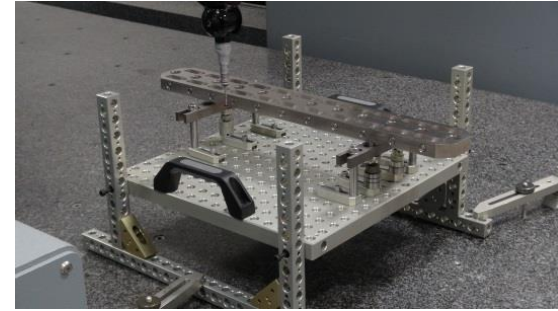
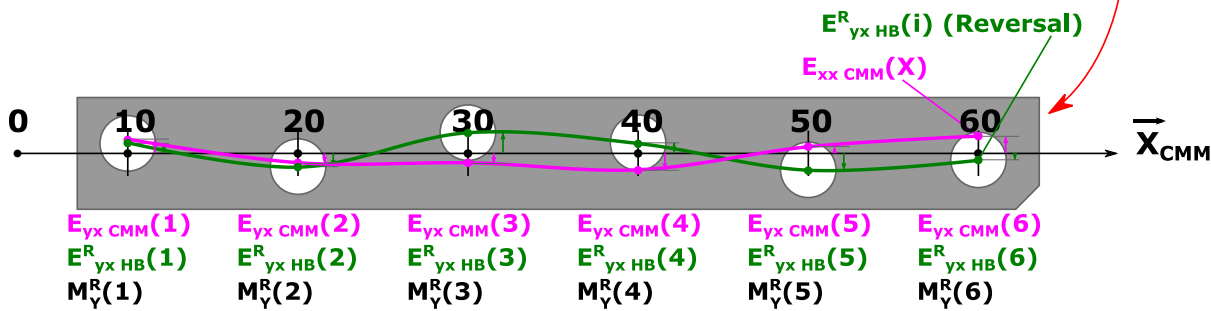


# Calibration: Reversal technique

$E_{yx HB}^{NR}(i)$  (No Reversal)  
*i* = Number of point of interest on Multi-Features Bar (HB)



Reversal way



MFB calibration set-up on CMM at LNE

Linear positioning error along  $X_{HB}$

$$E_{xxHB}(i) = \frac{1}{2} \left[ M_x^{NR}(i) + M_x^R(i) \right] - (i-1) \times L - E_{XXCMM} - \epsilon_{ZZCMM}$$

Straightness error along  $Y_{HB}$  and  $Z_{HB}$

$$\begin{cases} E_{yxHB}(i) = \frac{1}{2} \left[ M_y^{NR}(i) - M_y^R(i) \right] - \epsilon_{YXCMM} \\ E_{zxHB}(i) = \frac{1}{2} \left[ M_z^{NR}(i) - M_z^R(i) \right] - \epsilon_{ZXCMM} \end{cases}$$

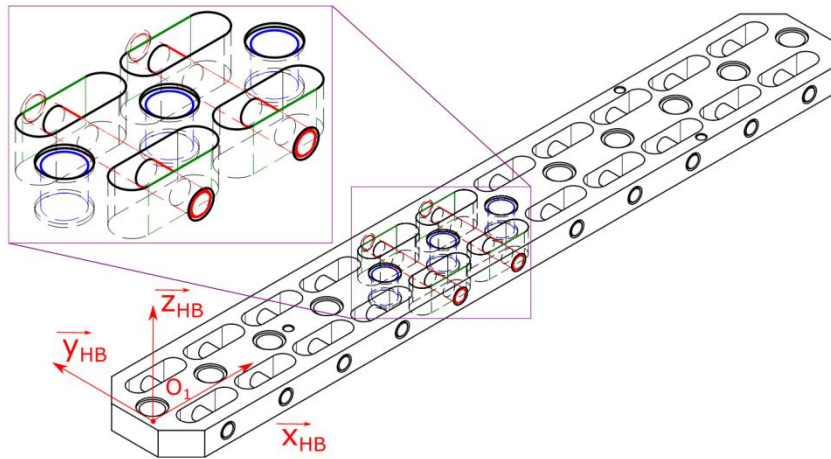
Measurement

Nominal geometry

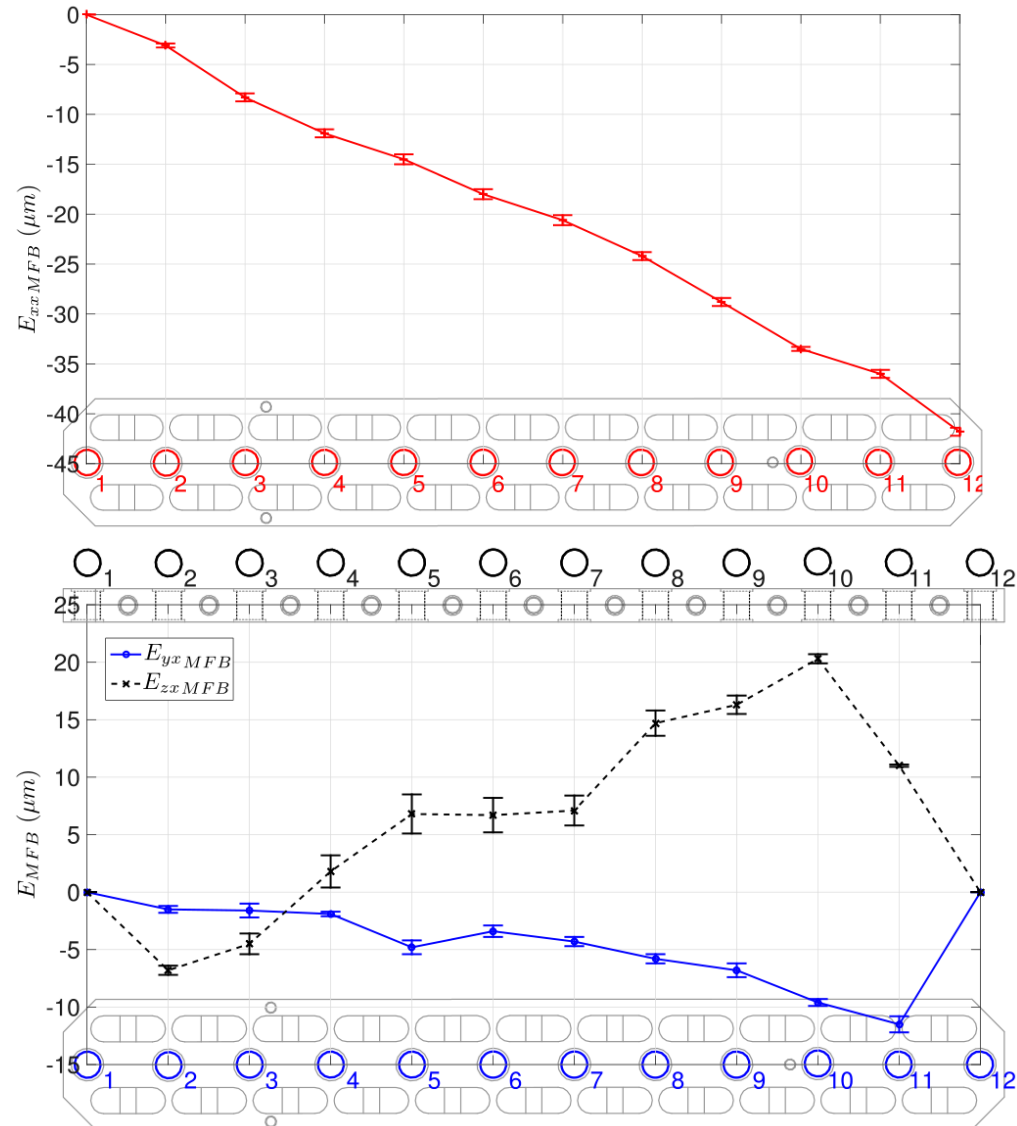
Linear positioning error along  $Z_{CMM}$

Random error

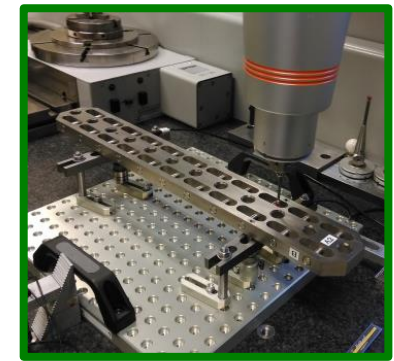
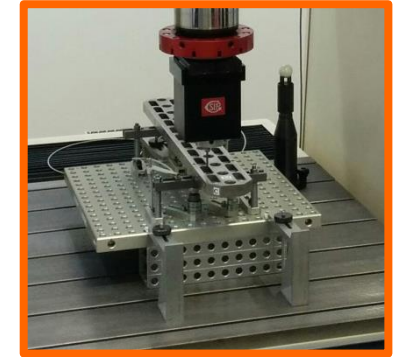
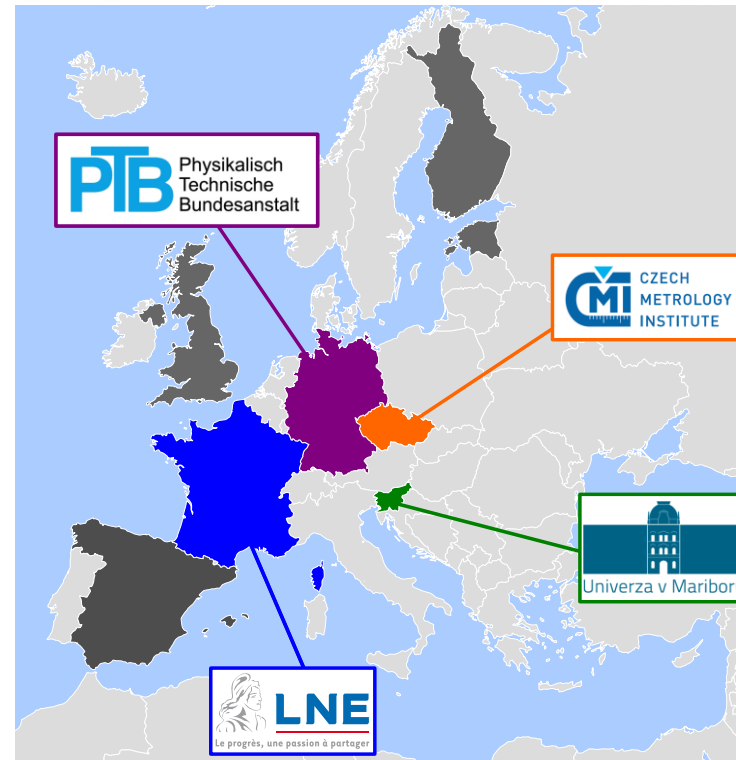
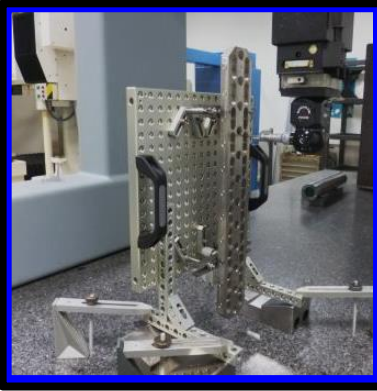




$$\forall i \in [1; N], \begin{pmatrix} x_i \\ y_i \\ z_i \end{pmatrix}_{R_{HB}} = \begin{pmatrix} (i-1) \times L & + E_{xx_{HB}}(i) \\ 0 & + E_{yx_{HB}}(i) \\ 0 & + E_{zx_{HB}}(i) \end{pmatrix}_{R_{HB}}$$



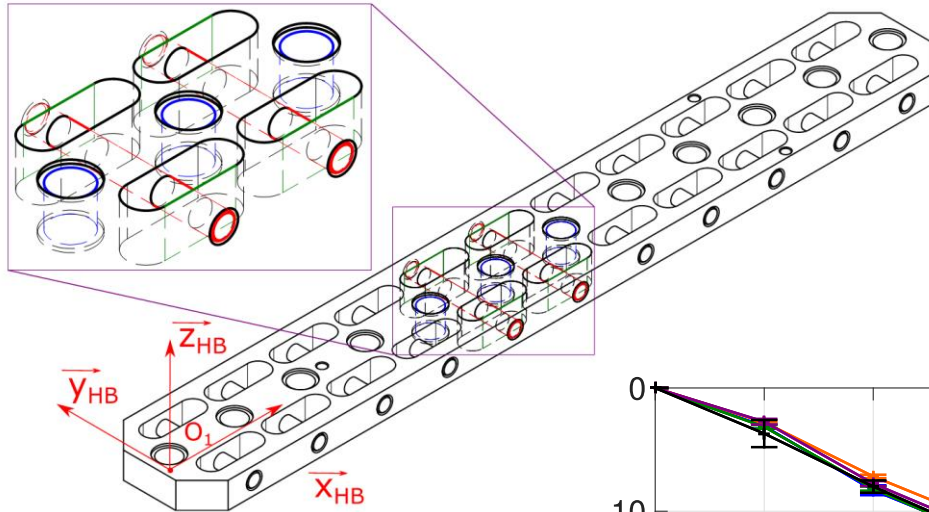
# European Participants for intercomparison



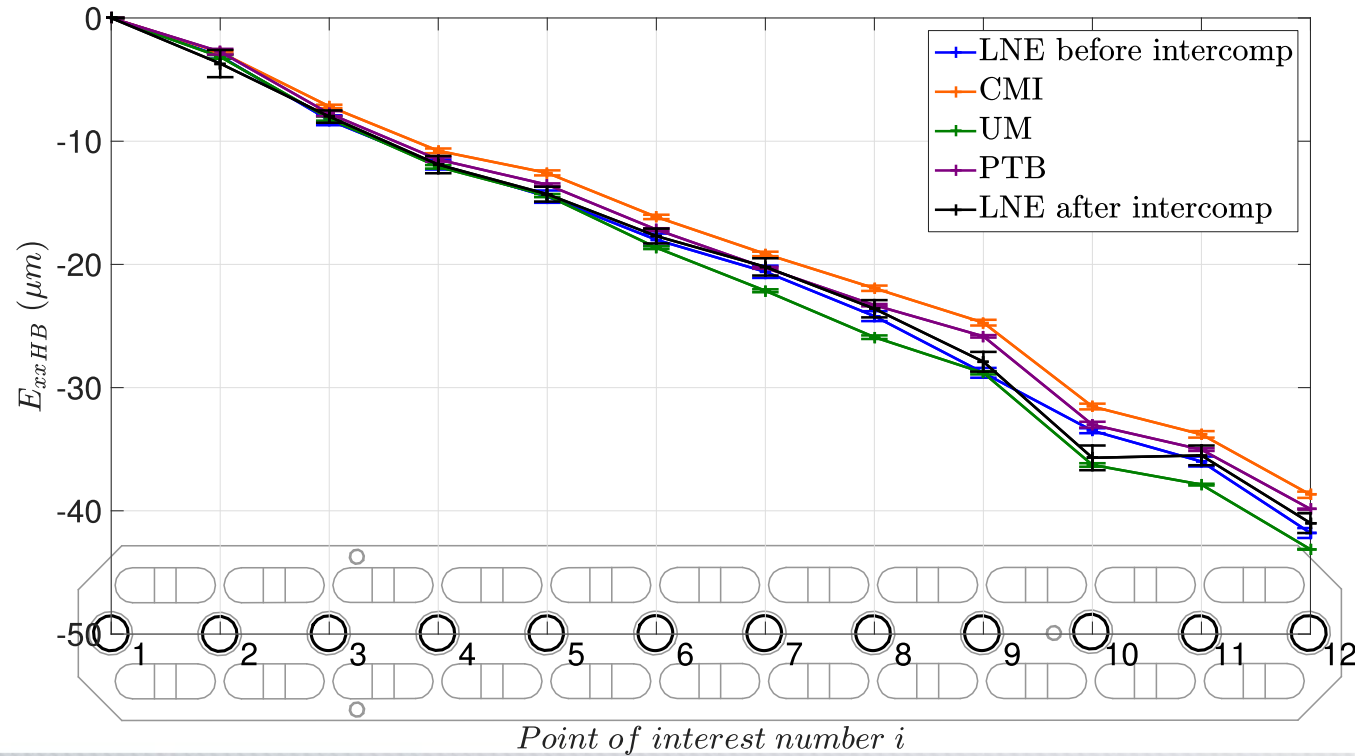
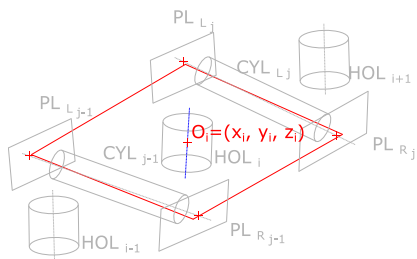
NMI	Type of CMM	Size of CMM (mm <sup>3</sup> )	U of CMM (μm+L(m)xμm)	T in metrology room (°C)	Along the CMM-axis	Operator	Signatory of CIPM MRA
<b>LNE</b>	Renault Automotion 251310	2500 x 1300 x 1000	4,5 + L x 4,0	20,26 ± 0,03	Z-axis	Fabien Viprey	Yes
<b>CMI</b>	SIP CMM5	710 x 710 x 550	0.8 + L x 1.3	19,73 ± 0,09	X-axis	Pavel Skalník	Yes
<b>UM</b>	Carl Zeiss UMC 850	1200 x 850 x 600	2,1 + L x 3,3	20,39 ± 0,03	Y-axis	Mitja Mlakar	Designated by MIRS
<b>PTB</b>	UPMC 850 CARAT	850 x 1200 x 600	0.8 + L x 3.5	20,18 ± 0,04	X-axis	Norbert Gerwien	Yes
<b>LNE</b>	Renault Automotion 251310	2500 x 1300 x 1000	4,5 + L x 4,0	20,04 ± 0,03	Z-axis	Fabien Viprey	Yes



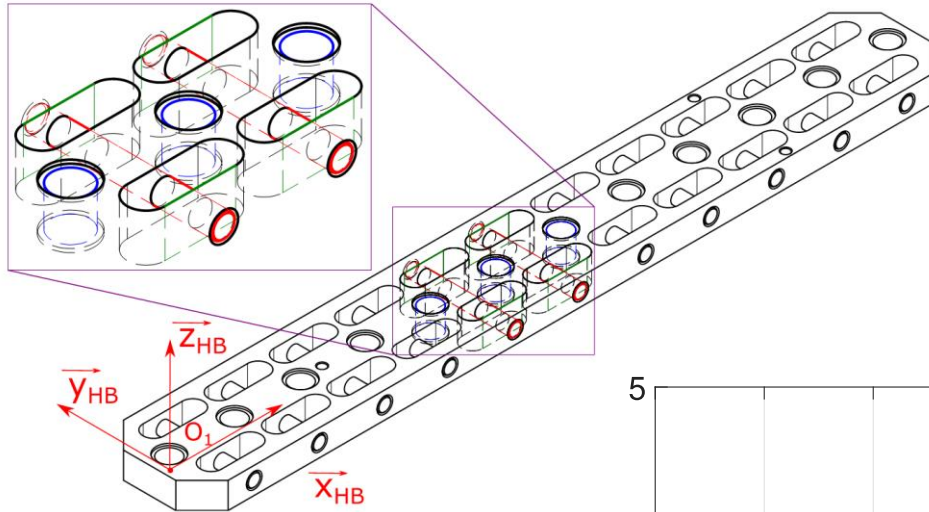
# Results: Linear positioning error along $X_{HB}$



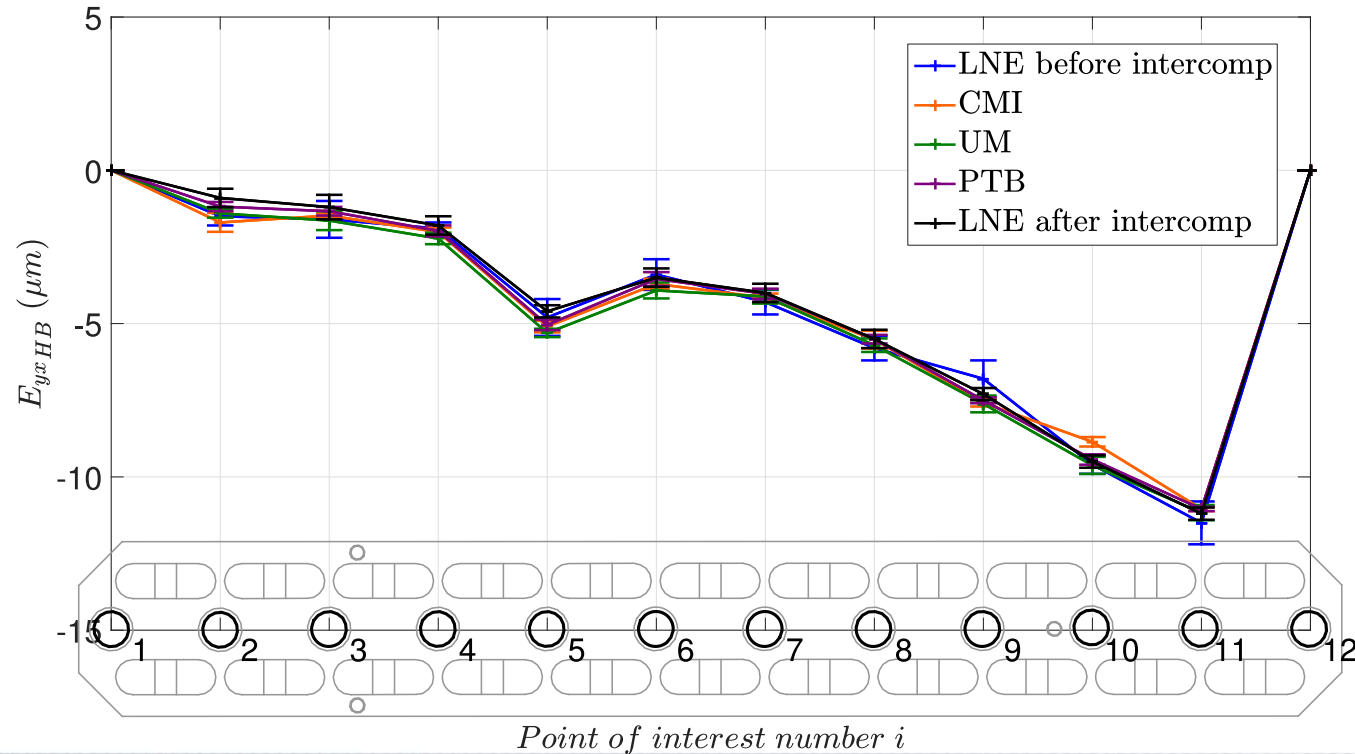
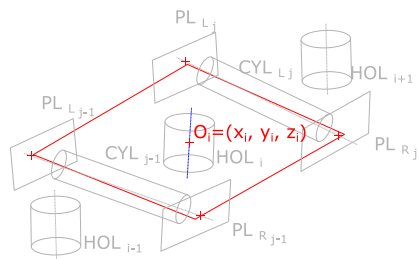
$$\forall i \in [1; N], \begin{pmatrix} x_i \\ y_i \\ z_i \end{pmatrix}_{R_{HB}} = \begin{pmatrix} (i-1) \times L & + E_{xx_{HB}}(i) \\ 0 & + E_{yx_{HB}}(i) \\ 0 & + E_{zx_{HB}}(i) \end{pmatrix}_{R_{HB}}$$



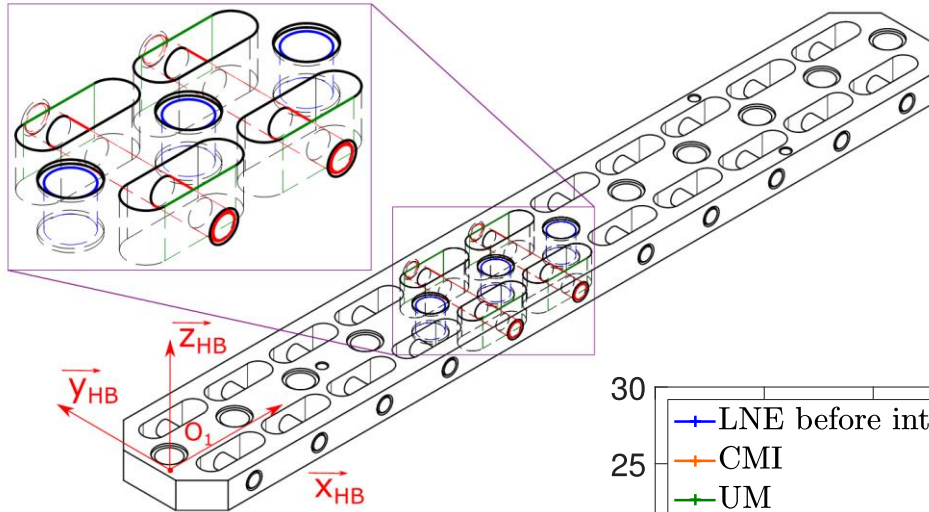
# Results: Straightness error along $Y_{HB}$



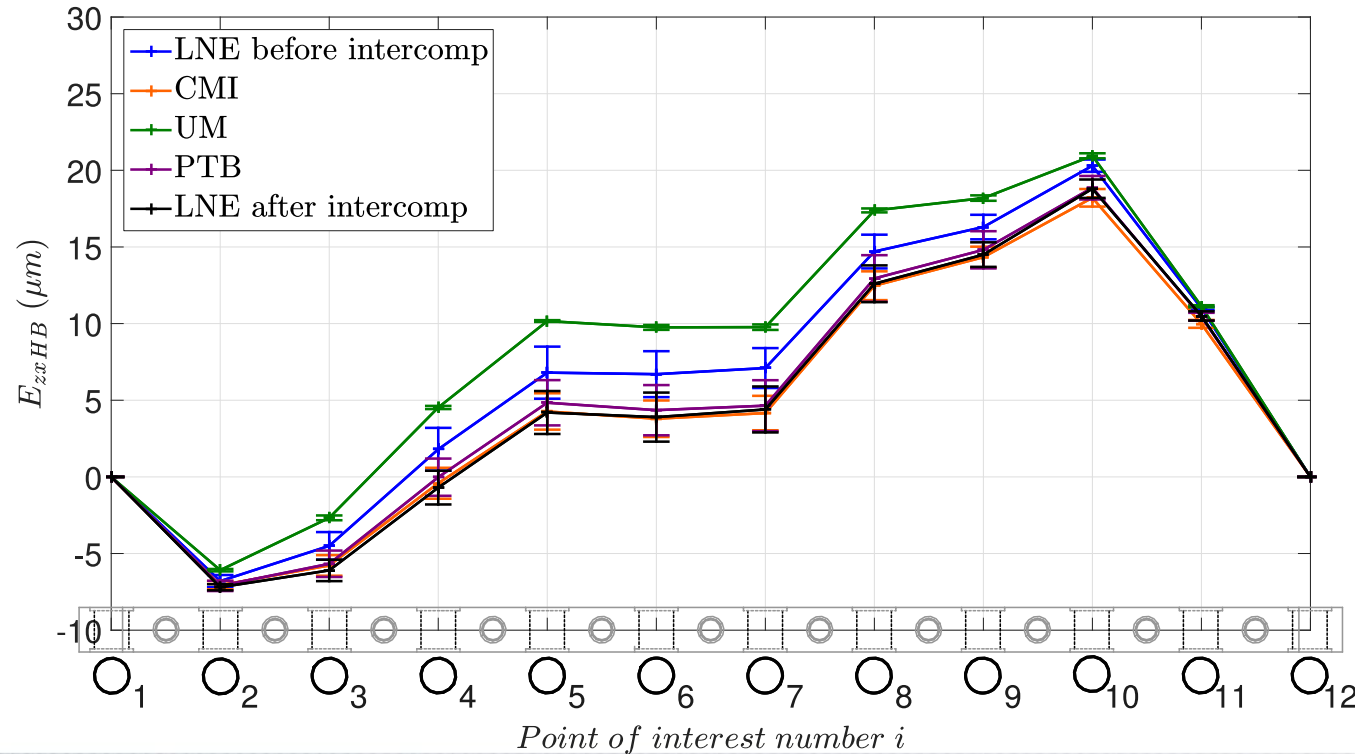
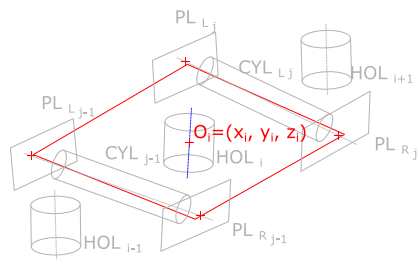
$$\forall i \in [1; N], \begin{pmatrix} x_i \\ y_i \\ z_i \end{pmatrix}_{R_{HB}} = \begin{pmatrix} (i-1) \times L & + E_{xx_{HB}}(i) \\ 0 & + E_{yx_{HB}}(i) \\ 0 & + E_{zx_{HB}}(i) \end{pmatrix}_{R_{HB}}$$



# Results: Straightness error along $Z_{HB}$

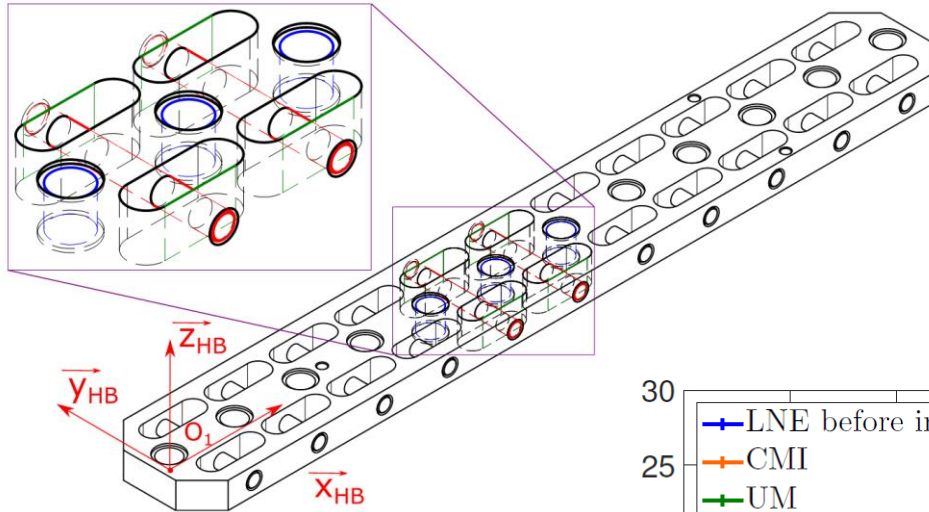


$$\forall i \in [1; N], \begin{pmatrix} x_i \\ y_i \\ z_i \end{pmatrix}_{R_{HB}} = \begin{pmatrix} (i-1) \times L & + E_{xx_{HB}}(i) \\ 0 & + E_{yx_{HB}}(i) \\ 0 & + E_{zx_{HB}}(i) \end{pmatrix}_{R_{HB}}$$

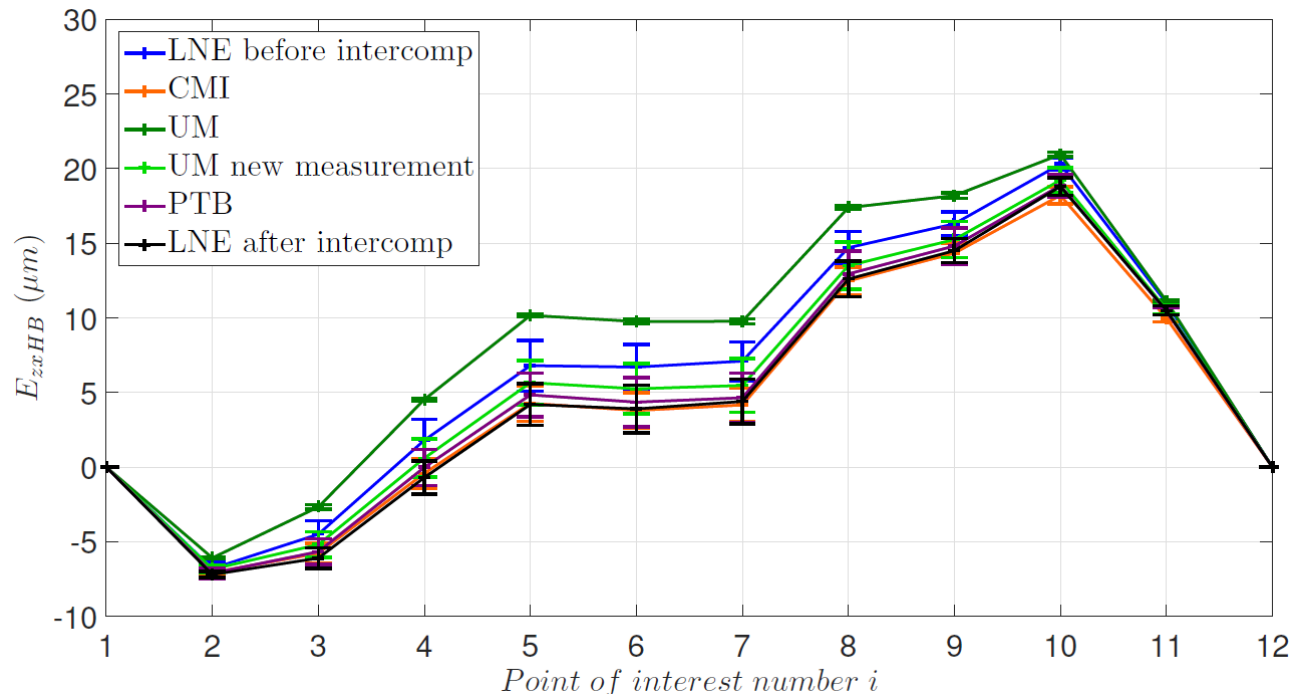




# Results: Straightness error along $Z_{HB}$



$$\forall i \in [1; N], \begin{pmatrix} x_i \\ y_i \\ z_i \end{pmatrix}_{R_{HB}} = \begin{pmatrix} (i-1) \times L & + E_{xx_{HB}}(i) \\ 0 & + E_{yx_{HB}}(i) \\ 0 & + E_{zx_{HB}}(i) \end{pmatrix}_{R_{HB}}$$



# Real time platform for Identification of geometric errors



Mikron UCP710

### Real time probing layout

PREMIUM TIM - Traceable In Process Dimensional Measurement

Created by : F. VIPREY  
Last update : September 17th 2014

#### Real time

Articular variables		
Variable		Value
X	478.095305664062	
Y	-144.59092578125	
Z	-54.55586230468...	
A	-0.003361328125...	
C	360.000269554688	

#### Capitalized data

Variable	Value
Labels[ata_mod]fed[002]4	89.0934306640...
Labels[ata_mod]fed[002]5	674.290736322...
Labels[ata_mod]fed[003]0	13125.49300...
Labels[ata_mod]fed[003]1	688.03206040...
Labels[ata_mod]fed[003]2	-144.5909257...
Labels[ata_mod]fed[003]3	-119.5943816...
Labels[ata_mod]fed[003]4	89.09343066...
Labels[ata_mod]fed[003]5	674.2907363...
Labels[ata_mod]fed[004]0	13125.45329...
Labels[ata_mod]fed[004]1	657.92678515...
Labels[ata_mod]fed[004]2	-100.4354922...
Labels[ata_mod]fed[004]3	-119.57062792...
Labels[ata_mod]fed[004]4	89.093435468...
Labels[ata_mod]fed[004]5	674.29971679...
Labels[ata_mod]fed[005]0	13122.79509...
Labels[ata_mod]fed[005]1	651.64237129...
Labels[ata_mod]fed[005]2	-100.3510576...
Labels[ata_mod]fed[005]3	-119.5889794...
Labels[ata_mod]fed[005]4	89.094468125...
Labels[ata_mod]fed[005]5	674.94972662...
Labels[ata_mod]fed[006]0	13128.84848...
Labels[ata_mod]fed[006]1	651.54478203...
Labels[ata_mod]fed[006]2	-100.4524492...
Labels[ata_mod]fed[006]3	-102.6273468...
Labels[ata_mod]fed[006]4	89.093425782...
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Labels[ata_mod]fed[007]3	-102.3625273...
Labels[ata_mod]fed[007]4	89.093474609...
Labels[ata_mod]fed[007]5	674.94970764...
Labels[ata_mod]fed[008]0	13101.05708...
Labels[ata_mod]fed[008]1	644.75493016...
Labels[ata_mod]fed[008]2	-102.0249199...

#### Last recorded values

Variable	Value
Time	13717.2257
X	478.095461448312
Y	-144.59103921878
Z	-54.5560266736878
A	-0.00346273607430153
C	360.00029236878

Probe status: ● Seated

Battery Status: ● Battery OK

Error: ● No error

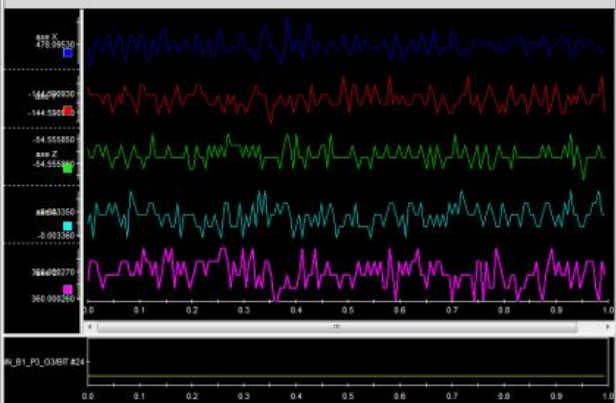
#### Control Parameters

Clock (s)	14059.39947	Force Index ON (1)	0
Longest task (s)	12.40E-005	Force Index OFF (0)	0
index Value (dSpace)	6	Fundamental sample time (s)	30.0E-005

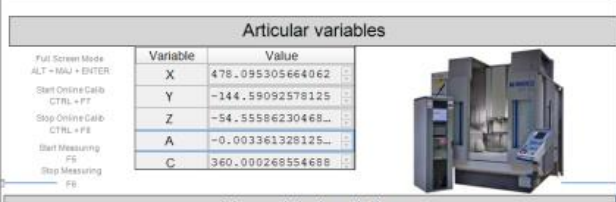
#### Init Control

Init ON (1)	0	Initialisation Status	0
Init OFF (0)	0	RMI-Q status	1
RMI-Q Power ON (1)	1	Touch probe status	1
RMI-Q Power OFF (0)	1		

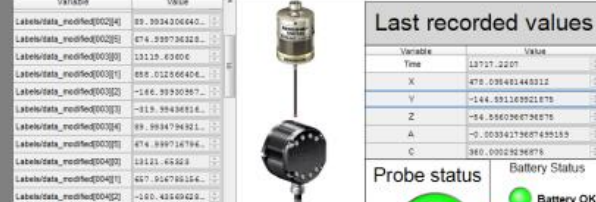
#### Time-related evolution



#### Probing trajectory



#### Real time probing



*Developed end user interface*

$$F=33,33 \text{ kHz}$$

$$T=30 \mu\text{s}$$

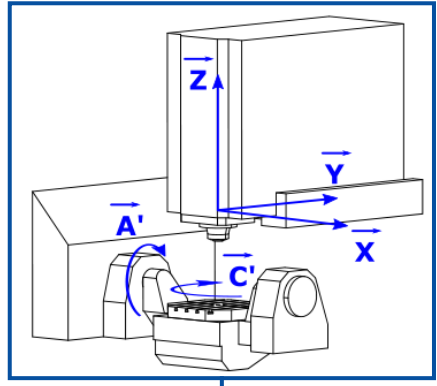
$$\text{Resolution} = 10 \text{ nm}$$

$$U_{(k=2)} \text{ RMP600} = 0,25 \mu\text{m}$$

$$U_{\text{delay max at 240mm/min}} = 0,47 \mu\text{m}$$

**dSPACE**

**MATLAB  
SIMULINK**



$$\begin{matrix}
 \underbrace{\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}}_{R_f \mathbb{T} R_{nom X}} \underbrace{\begin{bmatrix} 1 & 0 & 0 & X \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}}_{R_{nom X} \mathbb{T} R_{motion X}} \underbrace{\begin{bmatrix} 1 & -E_{CX} & E_{BX} & E_{XX} \\ E_{CX} & 1 & -E_{AX} & E_{YX} \\ -E_{BX} & E_{AX} & 1 & E_{ZX} \\ 0 & 0 & 0 & 1 \end{bmatrix}}_{R_{motion X} \mathbb{T} R_{nom Y}} \times \\
 \underbrace{\begin{bmatrix} 1 & -E_{C0Y} & 0 & 0 \\ E_{C0Y} & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}}_{R_{nom Y} \mathbb{T} R_{mean Y}} \underbrace{\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & Y \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}}_{R_{mean Y} \mathbb{T} R_{motion Y}} \underbrace{\begin{bmatrix} 1 & -E_{CY} & E_{BY} & E_{XY} \\ E_{CY} & 1 & -E_{AY} & E_{YY} \\ -E_{BY} & E_{AY} & 1 & E_{ZY} \\ 0 & 0 & 0 & 1 \end{bmatrix}}_{R_{motion Y} \mathbb{T} R_{nom Z}} \times \\
 \underbrace{\begin{bmatrix} 1 & 0 & E_{B0Z} & 0 \\ 0 & 1 & -E_{A0Z} & 0 \\ -E_{B0Z} & E_{A0Z} & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}}_{R_{nom Z} \mathbb{T} R_{mean Z}} \underbrace{\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & Z \\ 0 & 0 & 0 & 1 \end{bmatrix}}_{R_{mean Z} \mathbb{T} R_{motion Z}} \times \\
 \underbrace{\begin{bmatrix} 1 & -E_{CZ} & E_{BZ} & E_{XZ} \\ E_{CZ} & 1 & -E_{AZ} & E_{YZ} \\ -E_{BZ} & E_{AZ} & 1 & E_{ZZ} \\ 0 & 0 & 0 & 1 \end{bmatrix}}_{R_{motion Z} \mathbb{T} R_{nom T}} \underbrace{\begin{bmatrix} 1 & 0 & 0 & -J_X \\ 0 & 1 & 0 & -J_Y \\ 0 & 0 & 1 & -J_Z \\ 0 & 0 & 0 & 1 \end{bmatrix}}_{R_{nom T} \mathbb{T} R_T} \times \underbrace{\begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}}_{P_i / R_T} = \\
 \underbrace{\begin{bmatrix} a & d & g & p_x \\ b & e & h & p_y \\ c & f & i & p_z \\ 0 & 0 & 0 & 1 \end{bmatrix}}_{R_f \mathbb{T} R_W} \times \underbrace{\begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}}_{P^{w/} / R_W}
 \end{matrix}$$

Differential analysis

$$\begin{aligned}
 \delta X &= -E_{XX}(X) - E_{XY}(Y) - E_{XZ}(Z) \\
 &\quad - (E_{B0Z} + E_{BX}(X) + E_{BY}(Y)) \times G(x, y, z) \\
 &\quad + (E_{C0Y} + E_{CX}(X)) \times F(x, y, z) \\
 &\quad + E_{BZ}(Z) \times J_Z \\
 &\quad - (E_{CY}(Y) + E_{CZ}(Z)) \times J_Y \\
 \\
 \delta Y &= -E_{YX}(X) - E_{YY}(Y) - E_{YZ}(Z) \\
 &\quad + (E_{A0Z} + E_{AX}(X) + E_{AY}(Y)) \times G(x, y, z) \\
 &\quad - E_{AZ}(Z) \times J_Z \\
 &\quad + (E_{C0Y} + E_{CX}(X) + E_{CY}(Y) + E_{CZ}(Z)) \times J_X \\
 \\
 \delta Z &= -E_{ZX}(X) - E_{ZY}(Y) - E_{ZZ}(Z) \\
 &\quad - E_{AX}(X) \times F(x, y, z) \\
 &\quad + (E_{A0Z} + E_{AY}(Y) + E_{AZ}(Z)) \times J_Y \\
 &\quad - (E_{B0Z} + E_{BX}(X) + E_{BY}(Y) + E_{BZ}(Z)) \times J_X
 \end{aligned}$$

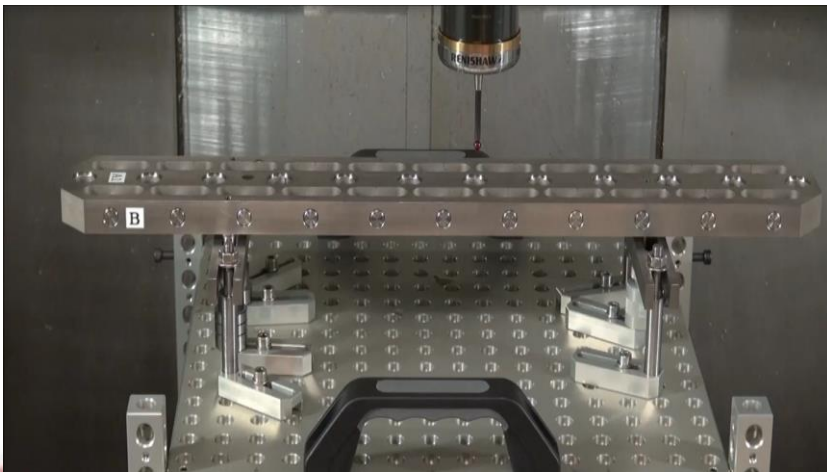
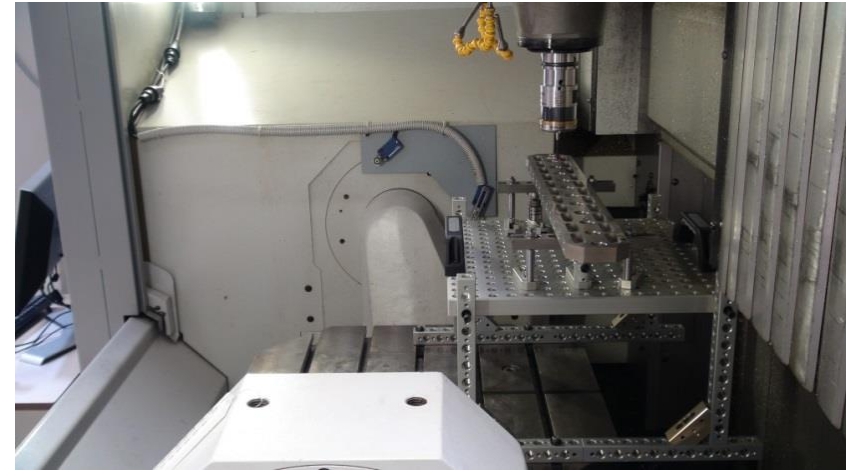
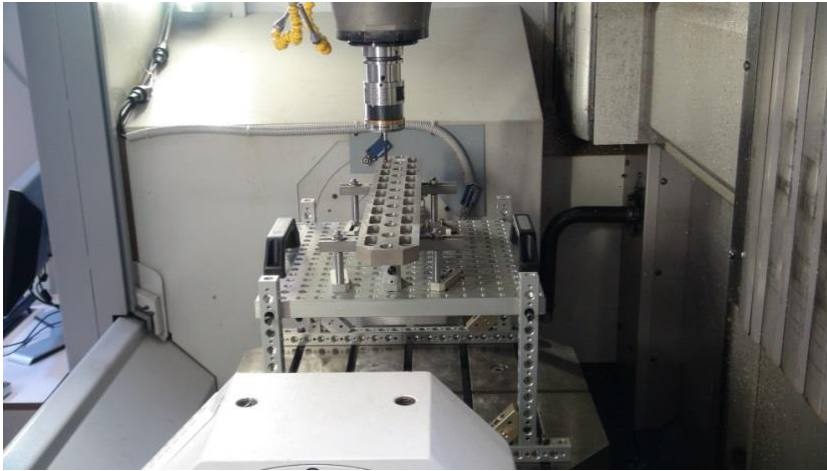
Geometric errors effects on the joint parameters







Application on Mikron UCP710 5-axis machine tool:

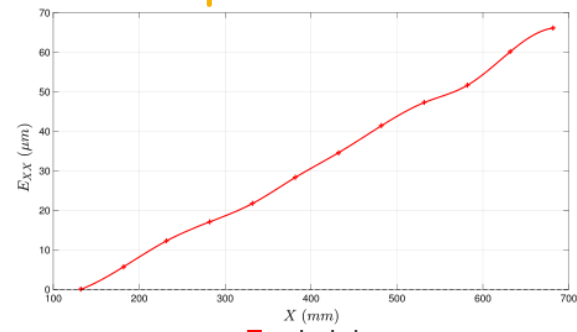
$E_{XX}$ ,  $E_{YX}$ ,  $E_{ZX}$ ,  $E_{AX}$ ,  $E_{BX}$  and  $E_{CX}$  along the X-axis identified on the points of interest  $O_i$  of the Hole-Bar:



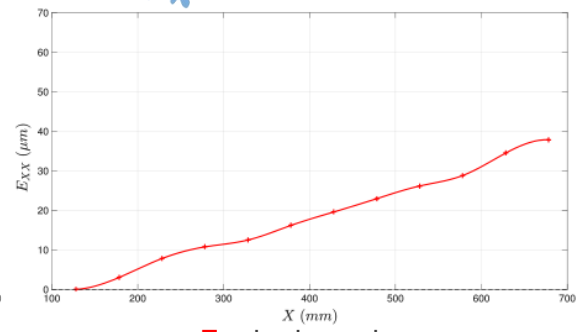
# Results of identification in the shop floor

  $T=27\pm 1^\circ\text{C}$

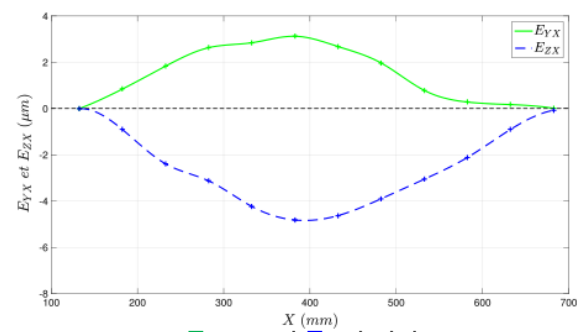
  $T=20\pm 1^\circ\text{C}$



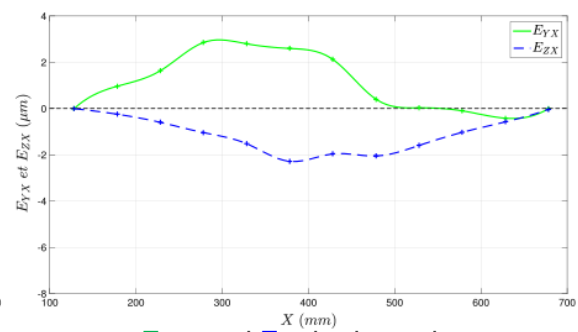
$E_{xx}$  in July



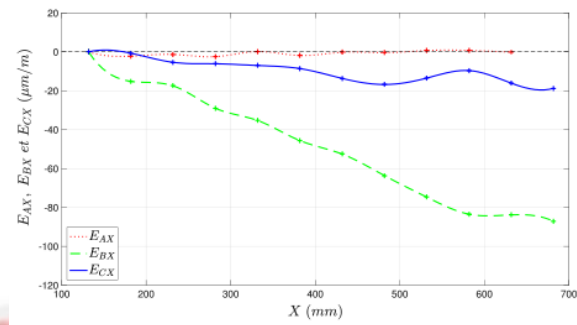
$E_{xx}$  in December



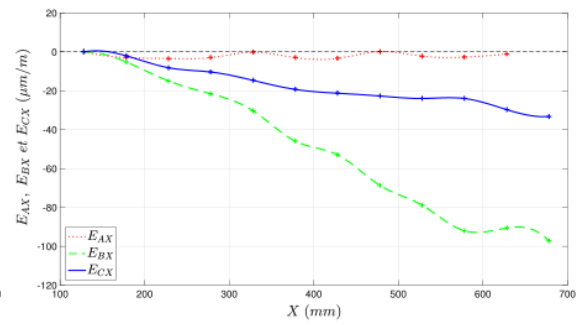
$E_{yx}$ , and  $E_{zx}$  in July



$E_{yx}$ , and  $E_{zx}$  in December



$E_{ax}$ ,  $E_{bx}$ , and  $E_{cx}$  in July





$E_{ax}$ ,  $E_{bx}$ , and  $E_{cx}$  in December

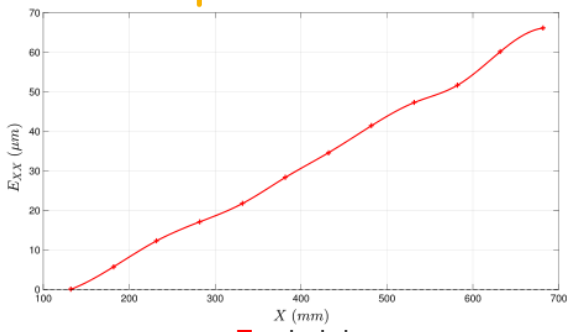




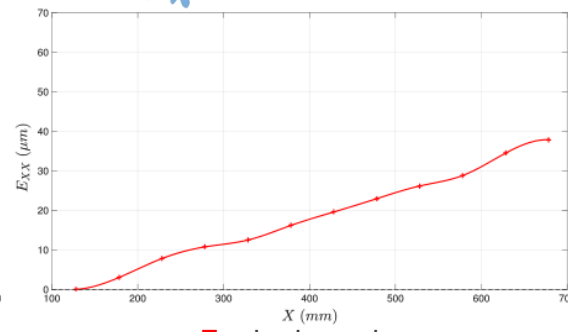
# Results of identification in the shop floor

  $T=27\pm 1^\circ\text{C}$

  $T=20\pm 1^\circ\text{C}$

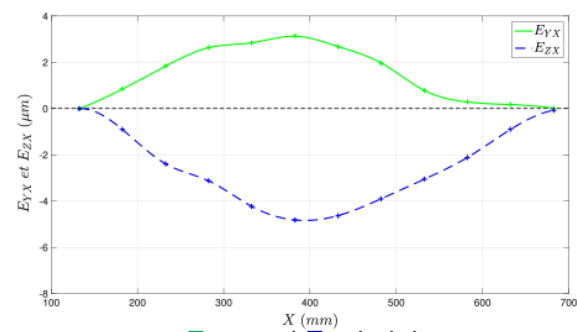


$E_{xx}$  in July

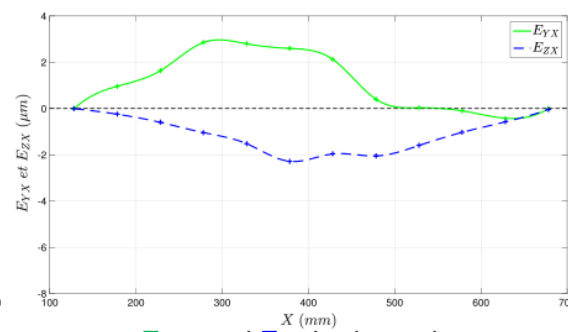


$E_{xx}$  in December

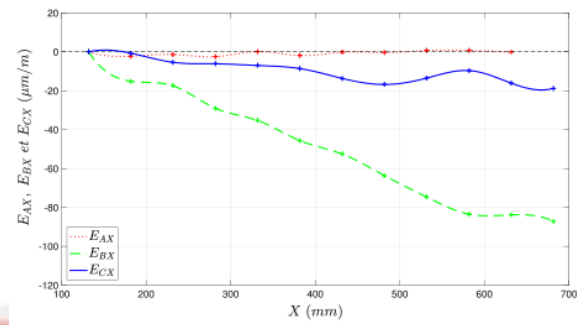
Identified geometric errors depend on the environmental conditions



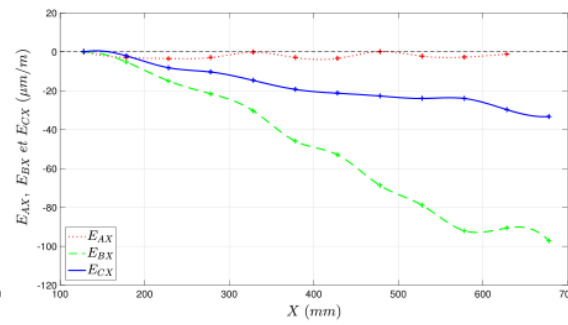
$E_{yx}$ , and  $E_{zx}$  in July



$E_{yx}$ , and  $E_{zx}$  in December




$E_{ax}$ ,  $E_{bx}$ , and  $E_{cx}$  in July




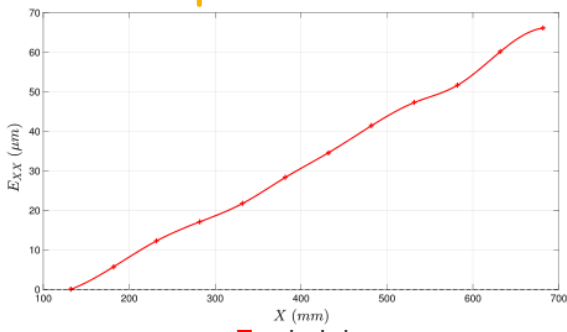
$E_{ax}$ ,  $E_{bx}$ , and  $E_{cx}$  in December



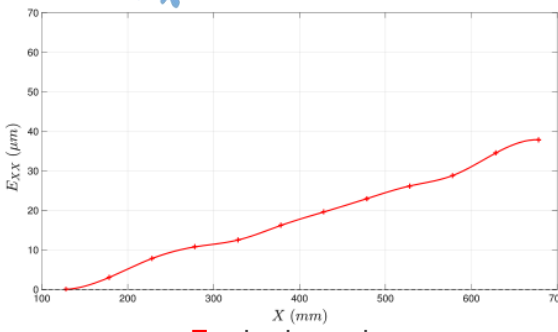
# Results of identification in the shop floor

  $T=27\pm 1^\circ\text{C}$

  $T=20\pm 1^\circ\text{C}$

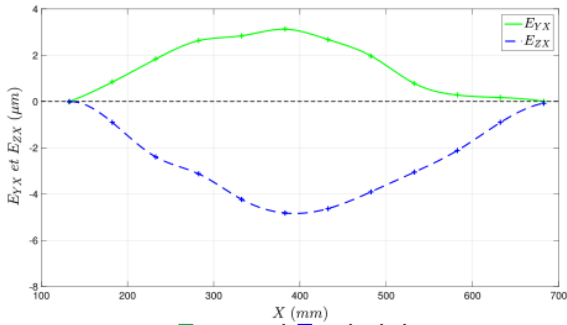


$E_{xx}$  in July

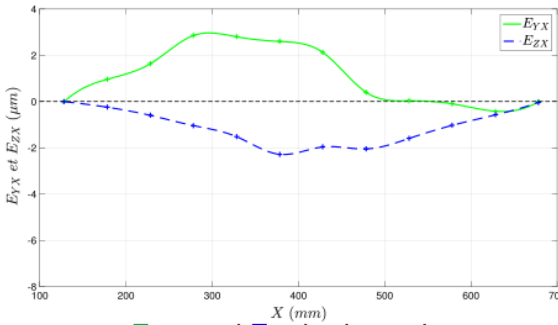


$E_{xx}$  in December

Identified geometric errors depend on the environmental conditions

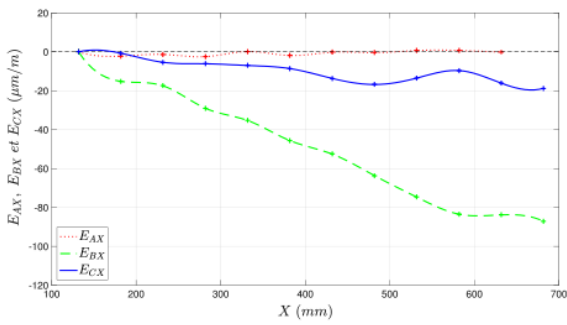


$E_{yx}$ , and  $E_{zx}$  in July

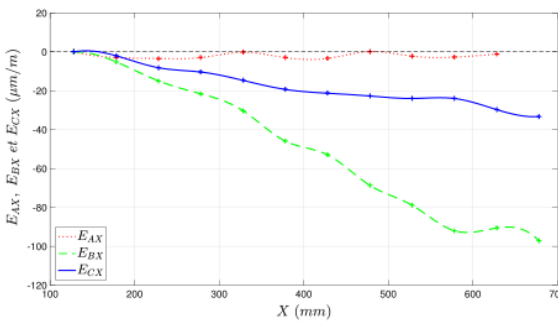


$E_{yx}$ , and  $E_{zx}$  in December

Solutions:  
 → use of climate chamber  
 → compensation of boundary conditions: several geometric models which depend on boundary conditions



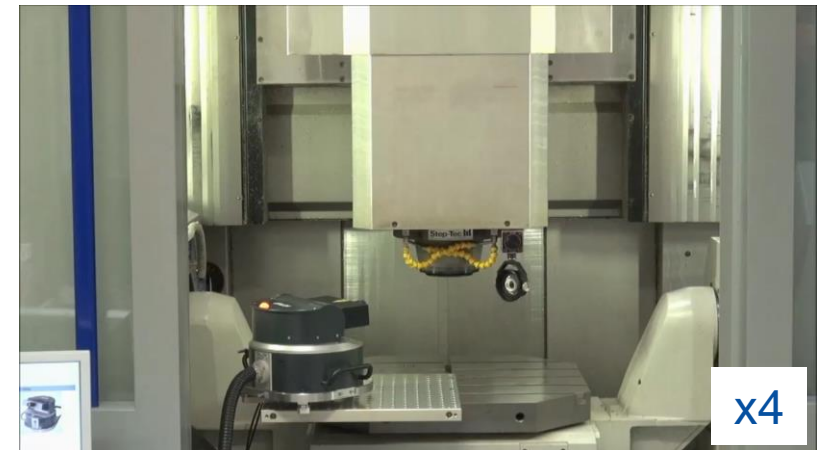
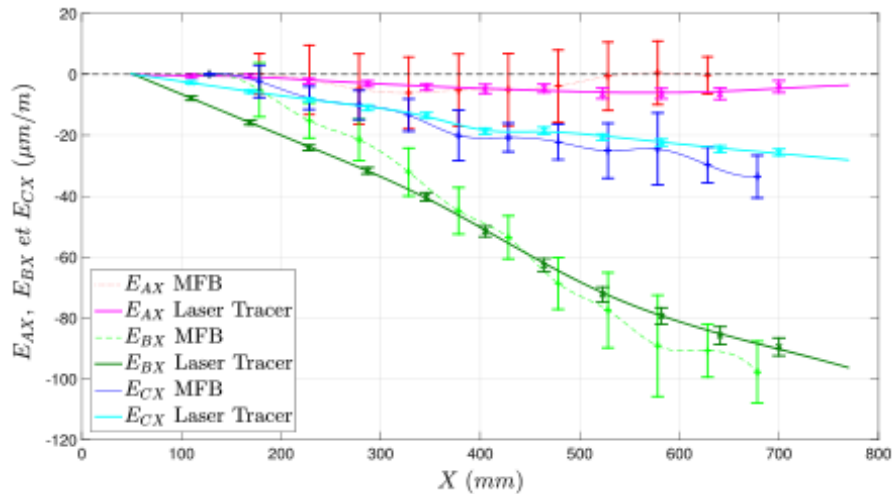
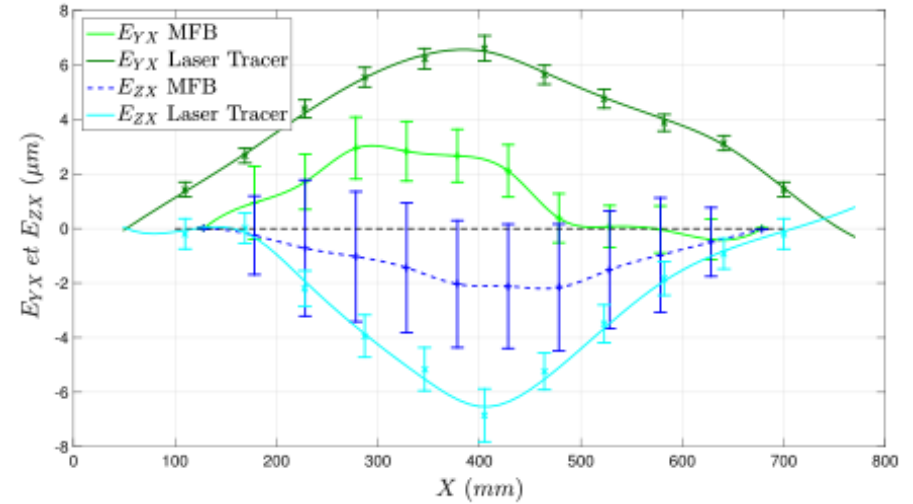
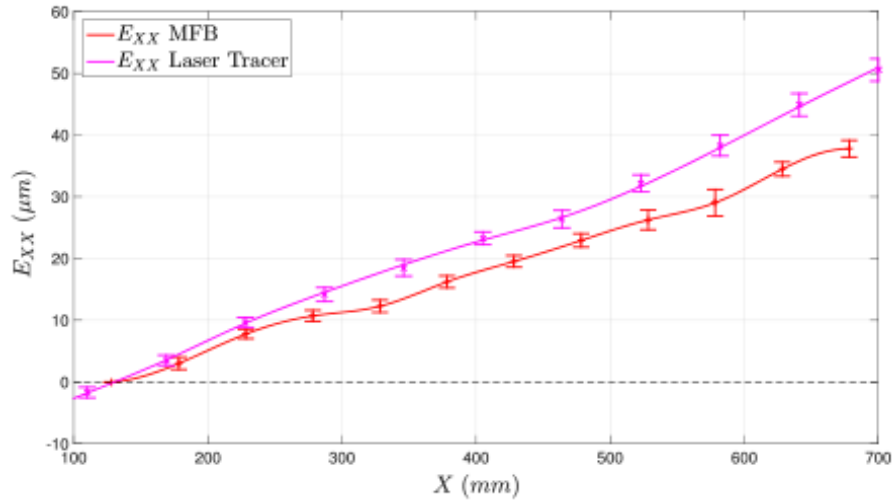
$E_{ax}$ ,  $E_{bx}$ , and  $E_{cx}$  in July

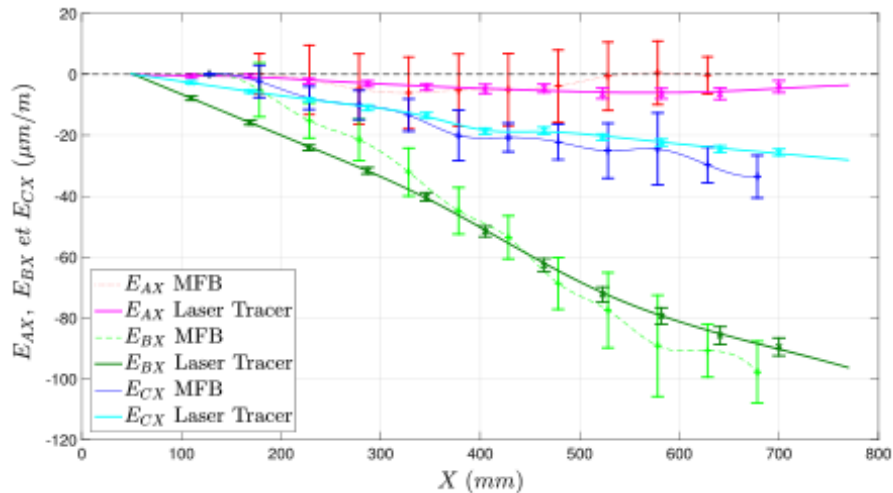
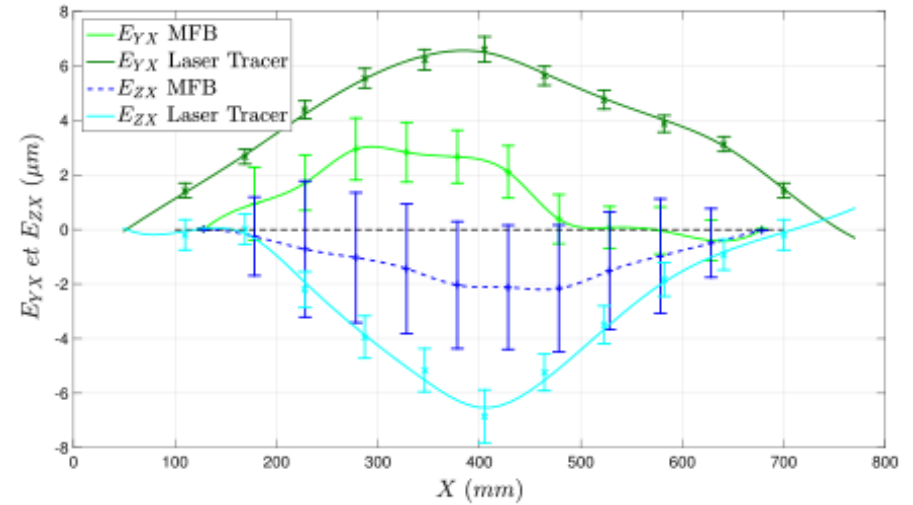
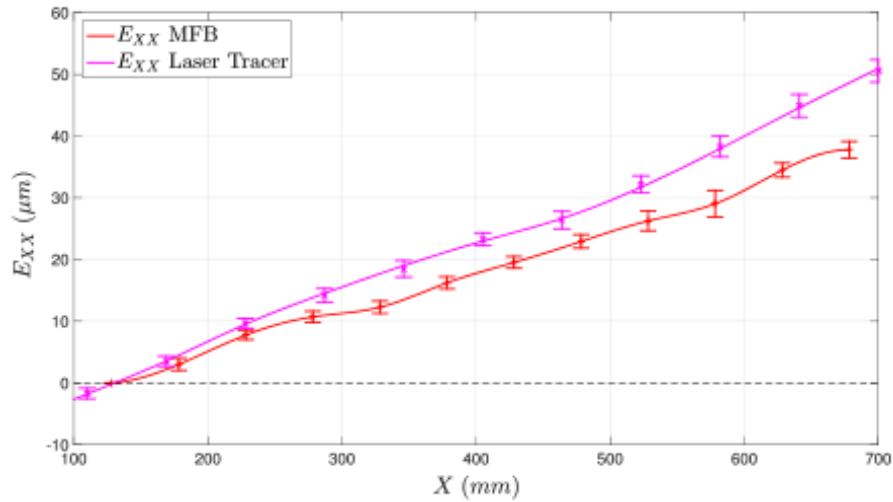


$E_{ax}$ ,  $E_{bx}$ , and  $E_{cx}$  in December



# Calibration using a Laser Tracer





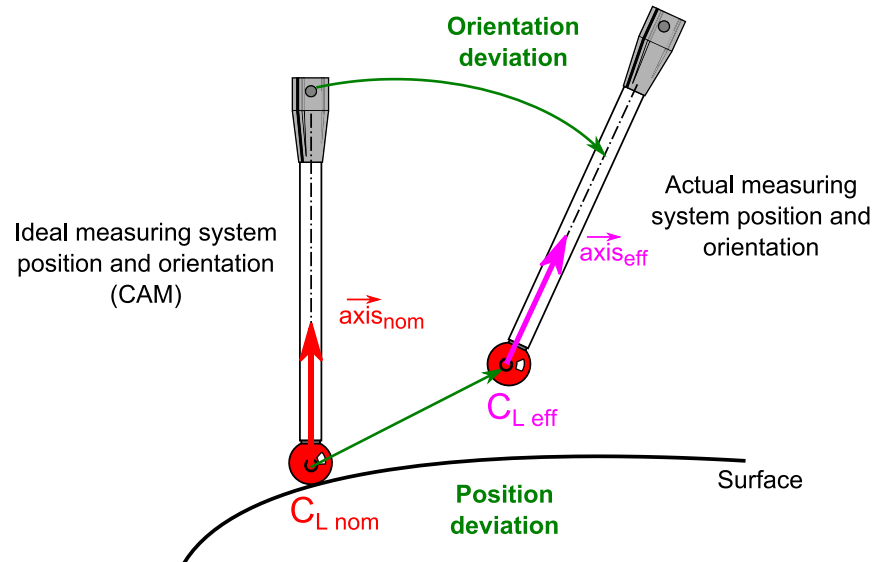
A variation between the results can be observed  $\rightarrow$  definition of end-point reference straight line (end-points), effects of the angular errors and boundary conditions

- Novel Hole-Bar made of thermo-invariant material (Invar) was defined and developed to calibrate machine tool
- The design of the Hole-Bar involves several patterns, including cylindrical and plane geometric entities, useful to extract 12 points of interests → providing 3 geometric errors (linear positioning error and 2 straightnesses) for each selected position
- The developed Hole-Bar was carefully calibrated on an accurate CMM, traceable to the SI meter definition at LNE
- The reversal technique was applied to calibrate the Hole-Bar in order to separate the motion errors of the CMM and the true intrinsic parameters of the Hole-Bar
- An intercomparison was shuttled between 4 european NMIs (PTB, CMI, UM, LNE)
- The Hole-Bar was used for the calibration of the Mikron UCP710 machine tool to evaluate the efficiency





- Submission of a journal paper about the intercomparison
- Identification of the motion errors of the rotary axes using the Hole-Bar
- Application of a compensation



## Dissemination

- 2nd MacroScale International Conference, Wien (Austria), October 2014
- Article submitted for publication in the journal: Precision Engineering

*Novel multi-feature bar design for machine tools geometric errors identification*



# Thank you for your attention!

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