Self-Supporting Graphene Films and their Applications

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Abstract

The self-supporting monolayer material which is graphene has excited enormous interest over the ten years since its discovery due to its remarkable electrical, mechanical thermal and chemical properties. In this paper we describe our work to develop chemical vapour deposition methods to grow monolayer graphene on copper foil substrates and the subsequent transfer process. Raman microscopy, scanning electron microscopy and atomic force microscopy (AFM) are used to examine the quality of the transfer red material. To demonstrate the process we describe transfer onto patterned SiO\textsubscript{2}/Si substrates which forms freely suspended graphene with focus on circular wells forming graphene drums. These show interesting mechanical properties which are being explored as nanomechanical resonators.

1. INTRODUCTION

Graphene is a monolayer of sp\textsuperscript{2} hybridised carbon atoms and has made its way to the forefront of research and development due to its unique mechanical, electrical, thermal, optical and dimensional properties [1–4]. A broad spectrum of techniques have been developed to produce high quality graphene films, including mechanical exfoliation of HOPG [2], epitaxial growth from SiC [5, 6] and, most promisingly, CVD on transition metals [7–13]. CVD graphene growth on Cu foils has become the most prominent method for scalable graphene growth due to its capability of producing consistent films of monolayer graphene up to tens of square metres, far surpassing any other method in scale and cost [13-16]. In this paper we first present an optimised recipe of CVD graphene growth.

CVD graphene can be transferred from transition metal substrate to any other surface. Current transfer techniques are plentiful but all include defect inducing steps and compromise either the structural integrity of the graphene or its cleanliness [17]. The majority of transfer processes apply a polymethylmethacrylate (PMMA) support layer and wet etch of the Cu leaving the Graphene/PMMA to be scooped onto a given substrate after being rinsed [18], this method has been proven to give reproducible and consistent results. However the physicality of this technique can lead to significant damage such as tears, cracks and wrinkles, simply from handling the delicate graphene/PMMA stack [19]. Free ions from the etchant will also be trapped in the graphene/substrate interface [18], degrading the electrical properties of the graphene via doping and scattering. The resulting chemical etch of PMMA on the surface leaves a significant amount of residue on the surface which also acts as a source of p-doping and scattering. This can be partially reduced by annealing, but high annealing temperatures (300 – 500°C) are defect inducing in the graphene [20, 21]. Other non-etchant based methods exist such as electrochemical delamination [22], but this fails to reach the scalability needed due to its complexity. The most promising method so far is a soak-and-peel method using only hot de-ionised water to separate PMMA/Graphene from Cu, however this method does not show easy reproducibility [23]. In this paper we present our optimised PMMA -based graphene transfer method that attempts to restrict all issues with PMMA -based transfer, allowing large scale CVD graphene transfer onto SiO\textsubscript{2}/Si.
The high strength, breaking strain and flexibility of graphene combine to make it potentially ideal for a range of mechanical applications exemplified by suspended graphene membranes. Finally the possibility of producing free-standing CVD graphene sheets was looked at as a means of investigating the properties of graphene without the inevitable perturbations which arise from its interactions with an underlying substrate. As well as the more obvious mechanical influence from chemical and physical bonds there are also the effects of surface gating of the graphene affecting the carrier density and mobility of the material. The drums were made using the optimised CVD growth and PMMA based wet transfer processes in spite of unwanted liquid tension leading to a lesser freestanding yield. This was done due to a lower density of debris on the graphene surface compared to other support layer removal techniques such as annealing (as confirmed by AFM statistical analysis).

2. LARGE SCALE GRAPHENE GROWTH VIA CHEMICAL VAPOUR DEPOSITION

Graphene is grown via a chemical vapour deposition (CVD) method onto a catalyst (see Fig 1) with a surface coverage of >95% monolayer graphene. Copper is used as the growth catalyst as opposed to other transition metals due to its low carbon solubility (established by isotope mapping of carbon 12 and carbon 13 [24]) and hence allows a self-restricting growth of single layer graphene. Successful and perfected graphene growth relies on the tuning of many variables, including; Cu foil pre-treatment and annealing, growth time, temperature and pressure, gas flow rates of hydrocarbon (methane C4H4), hydrogen and buffer (Argon) gases.

**FIG. 1: A cartoon depicting the mechanisms causing the growth of monolayer graphene on Cu during CVD.**

2.1 Transition Metal Pre-Treatment

Treating the copper foils before growth has a large effect on the graphene post CVD and it is ideal to have a flat and contaminant free copper foil for this. The copper used is a flattened 25µm thick foil of 99.95% purity. After being cut to a bulk size for growth, 1-3"x1-3" (this will be cut again for transfer), the foil is treated in acetic acid solution for 15 minutes and typically a DI water rinse is performed after, however this is omitted due to its contribution to forming a hydroxide layer on the Cu. The Cu will then be annealed.

2.2 Annealing

Having the copper foil positioned centrally above the filament inside the CVD chamber (quartz tube), it is annealed at 1000°C for 60 minutes with a hydrogen flow of 30sccm provided by a hydrogen generator. No buffer gas such as Argon is used to keep annealing pressure low. It has been found that annealing results in larger copper grain domains. This grain growth is driven by a favourable reduction in the energy of the system caused by a reduction of the grain boundary enthalpy [25, 26]. Grain boundaries have higher available energy, therefore; grain growth is anisotropic with their growth favouring certain orientations. We have found this to be true from X-ray diffraction analysis of our pre- and post-annealed foils, see Fig 2.
Analysing the XRD spectra, it is apparent annealing causes a shift of the relative intensity of [111] peak from $\approx 18000$ to $\approx 1800000$ and peaks associated with [200] and [220] are significantly reduced with [111] dominating. This modification of grain orientation is beneficial due to the reduction of grain boundaries per unit volume. This allows a more consistent, uninterrupted mobilisation of carbon adatoms upon the Cu surface during CVD. This allows larger graphene grain domains to form due to greater adatom mobilisation into existing graphene nucleations as well as a lower graphene nucleation density due to fewer regions of higher surface energy acting as nucleation sites [27].

The Cu we use favours [111] orientation post annealing, however we have used other Cu suppliers in which we see grain orientation shifts favouring other orientations when using identical annealing parameters. It can be determined that the treatment of the Cu by the manufacturer has a distinct effect upon the favoured orientation after annealing. This can be explained due to varying Cu foils having a more common grain pre-annealing. Pre-annealing the defect density is much higher, particularly grain boundary density. A larger density of grain boundaries will decrease the activation energy of grain motion due to a larger amount of stored energy; therefore more defects will lead to more probable grain growth during annealing. Another contribution of more grains is that fewer Cu atoms are needed to jump across a grain to cause grain boundary motion compared to coarse-grained Cu, making grain growth more probable [28]. The relevance of this to a single grain orientation dominating is that the most common grain orientation will begin to prevail at the start of annealing when the grain growth rate is the most prominent, leading to a dominant grain orientation (but not exclusive), especially if long duration and high temperature annealing is used.

2.3 Post Growth Cooling

Cooling the furnace immediately after graphene growth can have a significant effect upon the resultant graphene coverage [27, 29]. Two strategies have been explored which are fast and slow cooling.

At temperatures of 700°C+, hydrogen within the system has enough energy to bond with surface carbon to form gaseous hydrocarbon groups (reverse CVD), causing a sporadic etching of graphene, see Fig 3b. Hydrogen is needed within the system to prevent oxidation of the copper and graphene and is present from both the dissociated methane and the hydrogen flow into the system. Fast cooling takes 70 seconds to reach 700°C from 1035°C allowing a fast transition through the etching regime and gives a greater probability of continuous graphene. Slow cooling, which takes 24 times longer in our system is not favourable due to the extended period in this temperature regime with hydrogen present, leading to a higher structural defect density in the surface coverage of graphene.

2.4 Growth Pressure and Temperature

Under lower growth pressures, even with extended growth times, graphene typically only appears as separate islands and there is little continuity, see Fig 3a. This is caused by a low density of carbon
adatoms on the copper surface. With higher growth pressures a larger surface coverage is seen. The cause of low surface adatom density is due to the chemical potential of methane gas. The below equation describes how the chemical potential of methane ($\mu_{\text{methane}}$) is proportional to temperature (T) and its partial gas pressure ($P_{\text{methane}}$) of the CVD gas mixture [30].

$$\mu_{\text{methane}} = \mu_0 + RT \ln\left( \frac{P_{\text{methane}}}{P_{\text{total}}} \right)$$

(1)

Where $R$ is the ideal gas constant, $\mu_0$ is the standard reaction enthalpy of methane and $P_{\text{total}}$ is the pressure of the total gas in the system. Increasing $P_{\text{methane}}$ will cause a higher chemical potential creating a surface carbon adatom density tending toward carbon supersaturation, this is due to a greater affinity between the copper substrate and carbon from the dissociated methane, thus increasing graphene domain growth.

Nucleation density saturates $\approx$ 4 minutes into growth and higher temperatures correlate with lower nucleation density and larger lateral domain size of graphene. After 30 minutes the growth time has a negligible effect upon nucleation growth, even at hugely extended growth times graphene nuclei will not merge unless the temperature threshold of 1000°C is met, leaving channels of exposed Cu, see Fig 3c. Our optimised growth recipe for our CVD system uses a pressure of 110mbar and growth temperatures 1035°C.

![FIG. 3: SEM images of graphene and subsequent artefacts of growth from different growth parameters. a.) Inconsistent growth of graphene leaving separate nucleations and little continuous graphene due to low pressure growth (2mbar). b.) Blotchy areas of no graphene caused by reverse CVD. This is due to hydrogen etching of graphene and is prominent during slow cooling when the system is at 700°C for extended periods of time. c.) Low temperature growth (900°C) of graphene showing a reluctance of graphene nucleations to merge with each other even at extended growth times of over 120 minutes. d.) High surface coverage monolayer graphene using temperature of 1035°C, pressure of 110mbar, methane flow rate of 1sccm and hydrogen flow rate of 80sccm.](image-url)
2.5 Methane Flow Rate

The domain size and density of graphene nucleations is largely dependent upon methane flow rates. Methane flow rates of \( \geq 1 \text{sccm} \) are used and give continuous surface coverage and have been established as the standard for the system used as even this low flow rate supplies a critical density of surface carbon adatoms. A methane flow rate of \( \geq 1 \text{sccm} \) does not always give a full coverage and it is possible a larger flow rate may be more beneficial to domain size, however broken surface coverage in these circumstances is likely to be due to other effects such as low pressure, low temperature, hydrogen etching or methane dilution with buffer gases causing higher pressures but lower methane density per volume.

Monolayer graphene with small sites of bi/multi-layer on the Cu surface can be grown using methane flow of 1sccm with short growth times of 12minutes/cm\(^2\) with H\(_2\) flow rates of 80sccm, see Fig 3d.

3. GRAPHENE TRANSFER

Graphene is transferred onto patterned Si/SiO\(_2\) substrates using a PMMA support layer method. Giving a high quality yield of freestanding graphene structures (graphene drums) over the patterns etched into the substrate. SiO\(_2\) is used as the substrate surface due to its dielectric properties and strong adhesion/van der Waals forces with monolayer graphene (0.45\(+/-\) 0.02J/m\(^2\)) [31]. This force is large in comparison to most in micromechanical structures; this importantly provides strong anchoring for the graphene drums when brought to mechanical resonance. High quality CVD graphene transfer via this method is highly influenced by several variables including; substrate and substrate treatment, polymer support layer, transition metal etchant, cleaning of the sample, polymer removal and handling.

3.1 Making the substrate

A Si substrate with a thermally grown 300nm thick SiO\(_2\) layer was patterned by optical photolithography with a large array of shapes including circles and squares with diameters ranging from 2-50\(\mu\)m [32]. The photomask includes an array of navigational features, with target crosses and respective row and column numbering to allow location of each shape. Wet etching was used to remove the oxide so that the patterns represented an array of 1-3\(\mu\)m deep depressions across the Si chip. The etched wafers were cut into 10mm x 10mm chips each containing four repeats of the overall pattern, each one occupying a quadrant of the chip.

3.2 Substrate Treatment

The treatment of substrates is key to optimising graphene transfer. SiO\(_2\)/Si substrates are a standard for graphene transfer and their treatment will alter graphene’s electrical properties extensively. Oxygen plasma and UV ozone treatments are used to clean the substrate surface but cause a degree of hydrophilicity, creating a dipolar molecule affinity at the surface due to oxidation [33]. Due to graphene’s field effect behaviour, this will result in the shifting of the Dirac point to varying levels of p-doping caused by the local surface charge density (proportional to hydrophilicity) which can be determined using surface contact angle measurements. These results will be discussed in further detail in another publication.

3.3 Graphene Transfer Process

The graphene transfer process is as follows, see Fig 4: Liquid PMMA (950 PMMA A6, 6% of polymethyl-methacrylate in Anisole) is placed onto the CVD grown graphene via a syringe (0.1ml PMMA per cm\(^2\) graphene) then spin-coated at 8000RPM for 60 seconds, creating a PMMA layer of thickness \( \leq 400 \text{nm} \). The sample is cured under ambient conditions (fume cupboard in non-clean room lab) for 24 hours allowing the PMMA to naturally relax onto graphene rather than be forced to cure which has a greater chance of inducing defects such as tears in the graphene. The CVD process grows graphene on the top and bottom of Cu due to gas flow underneath the Cu during CVD, this can also be caused by carbon precipitating out to all surfaces upon cooling after diffusion of carbon species into the Cu foil during CVD, however this will be minimal due to the low carbon solubility of Cu [13, 24, 27]. The uncoated (no PMMA) side of Cu is treated by floating it on a bath of 10% nitric acid solution (HNO\(_3\)) for one minute to remove the unwanted graphene that has grown on the bottom side of the Cu
foil, leaving a Cu/Graphene/PMMA stack. This is done to prevent the monolayer of graphene on the bottom side of Cu contacting the top side graphene once the Cu has been removed, which would create a bi-layer post Cu etch.

The PMMA/graphene/Cu sample is then placed in a copper etchant, an ammonium persulphate solution (1g (NH₄)₂S₂O₈ per 100ml ultra-pure 18.2M cm at 25°C water), a series of three etchant exposures is used, each up to 12 hours. (NH₄)₂S₂O₈ has been found to be a superior Cu etchant leaving little residue compared to other commonly used etchants such as Ferric Chloride (3.5g FeCl₃ in 100ml water) which leaves significant amounts of iron on the graphene surface which needs post treatment with Hydrochloric Acid (HCl). Following Cu etching, two ultra-pure water baths are used to rinse the sample by floating it on the liquid surface for up to 6 hours per bath. The sample is moved between baths and etchants using a small beaker to scoop the sample and some of the liquid and is then poured into the new solution, the graphene is constantly sat on a small amount of liquid. This slightly contaminates the new bath with the liquid the graphene is sat on from the previous bath, but the amount of contamination is negligible in comparison to the new volume of etchant/rinse as confirmed with pH testing. This technique prevents the graphene contacting the glass or transfer scoop which can easily damage the graphene by transferring it in part to the surface it touches.

FIG. 4: A simplified drawing of the wet graphene transfer process onto substrates for both freestanding and flat graphene.

The sample is then scooped onto the wanted substrate by approaching the sample perpendicularly to the substrate, a gentle contact between the two is made and then the substrate is pulled out, connecting the sample to the surface with minimal wrinkling.

3.4 Removing PMMA

For optimum mechanical resonator performance the PMMA/Graphene stack is ironed out via heating the PMMA, this softens and expands PMMA allowing it to relax flat upon the substrate, minimising any wrinkling of the graphene and in turn restricts mechanical and electrical degradation. The heating process also serves to anneal the sample, removing PMMA via hydrogenolysis and depolymerisation. The conditions for annealing are 350°C in a furnace for 10 hours at ≈ 2mbar with a hydrogen flow rate of 100sccm. Argon is omitted from the process as it causes a dilution of hydrogen, leading to a direct increase in polymer debris left on the surface of graphene as cutting of -carboxyl functionalization is diminished. This also allows for a capillary effect of PMMA vapour due to insufficient dilution causing debris build up in the features of patterned substrates.

Wet solvent etching of the PMMA gives a cleaner surface in comparison to annealing but due to surface tension effects gives a much smaller yield of complete freestanding graphene structures, for graphene flush against an unpatterned substrate this is the optimum PMMA etch technique. Dichloromethane (DCM) is used to etch structures for 24 hours in a light current created by a magnetic
stirrer, the DCM is then replaced with Isopropanol (IPA). The IPA is rapidly heated, significantly lowering its surface tension and it is allowed to evaporate away without boiling. This gives comparable results to using a critical point dryer as outlined in [34].

4. RAMAN ANALYSIS

Perfect graphene exhibits Raman peaks at D (1350/cm), G (1580/cm) and 2D (2690/cm) [35-37]. The graphene we have grown shows all of these defining peaks, see Fig 5. The D band is strongly associated with disorder (it is an inter-valley phonon scattering from K to K’ points) and subsequently an increase in intensity of I(D)/I(G) ratios also indicates an increase in disorder. We’ve found that graphene on the SiO$_2$ surface shows a strong D band while it is negligible in freestanding graphene, it can therefore be speculated that the interaction with the SiO$_2$ is disorder inducing. Other peaks such as D + G (2940/cm) and D’ (1620/cm) are also indicative of a level of disorder in the graphene but do not present themselves strongly in our graphene Raman spectra. The I(D)/I(G) peak ratio shows two separate behaviours with disorder increase, at lower defect density the ratio will increase proportionally due to a greater quantity of elastic scattering which again reinforces the hypothesis that the substrate is disorder inducing as we have no existing ratio in freestanding graphene due to the lack of D band. As graphene disorder increases to a point where graphene can be defined to be amorphous carbon the ratio will begin to decrease due to an attenuation of all graphene defining bands, we do not see such an attenuation in any of our samples.

With an increase in graphene layers additional forces are present due to interactions between the stacked layers. With greater layer number a splitting of the 2D peak will be seen along with an increased wave-number, reduced intensity and reduced FWHM. The G peak is also affected by layer number and will red shift with increasing layers. Therefore an assumption of layer number can be derived by taking the ratio of 2D and G peak intensities (I(2D)/I(G)) [36, 37]. A poor ratio is measured in our SiO$_2$ bonded graphene of ≈ 1 whereas the freestanding graphene on the same sample has a ratio averaging at 1.5 (with maximums close to 5) which is very close to the optimum of 2. These results suggest that the number of graphene layers increases over the SiO$_2$, however this is not the case as confirmed with AFM and is an artifact from the substrate interaction with graphene. A possible explanation for this is hydrocarbons/free radicals are trapped between graphene and the SiO$_2$ as a result of the transfer process and the carbon/doping effects from these give an impression of bi/multi-layer graphene.

A shift in Fermi level from the Dirac point is a consequence of doping in the graphene and corresponds to a decrease in probability of excited charge carrier recombination [38]. This causes perturbations of photons to be non-adiabatic, removing the Kohn anomaly (an anomaly in the dispersion relation of metals at points of high symmetry in the first Brillouin zone, causing the energy of a specific phonon to be lowered) and increasing the phonon energy for the G peak, increasing its frequency and decreasing its FWHM [39]. With increasing electron concentration a decrease in 2D peak position can be seen due to a hypothesized expansion of the crystal lattice directly reducing the energy of the characterizing phonons [39]. Oddly we see very close values to the accepted graphene peaks in our SiO$_2$ bonded graphene whereas the freestanding graphene has red-shifted values for both G and 2D peaks, see table 1. This suggests that our freestanding graphene is doped while the SiO$_2$ bonded graphene is not. This is highly doubtful and it is likely that the blueshift of the bonded graphene corresponds to the substrate p-doping the graphene while graphene is un-doped while freestanding at the lower wavenumber values. The total shift away from normal wavenumber for both freestanding and bonded graphene is possibly an artefact from laser power and wavelength (532nm) used.

<table>
<thead>
<tr>
<th>Peak</th>
<th>Freestanding Wavenumber (cm$^{-1}$)</th>
<th>Peak FWHM Freestanding</th>
<th>On SiO$_2$ Wavenumber (cm$^{-1}$)</th>
<th>Peak FWHM On SiO$_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>2D</td>
<td>2638.94</td>
<td>8.75675</td>
<td>2665.2</td>
<td>15.0576</td>
</tr>
<tr>
<td>G</td>
<td>1568.58</td>
<td>6.20261</td>
<td>1579.22</td>
<td>6.49305</td>
</tr>
<tr>
<td>D</td>
<td>N/A</td>
<td>N/A</td>
<td>1339.5</td>
<td>6.72014</td>
</tr>
<tr>
<td>I(2D)/I(G)</td>
<td>1.5</td>
<td>N/A</td>
<td>1</td>
<td>N/A</td>
</tr>
<tr>
<td>I(D)/I(G)</td>
<td>N/A</td>
<td>N/A</td>
<td>0.4</td>
<td>N/A</td>
</tr>
</tbody>
</table>
FIG. 5: Top left and Bottom left, Raman spectra of the average peaks of freestanding graphene and graphene bonded to SiO2 respectively. Top right, Raman representation of 2D peak intensity of graphene sample showing clear areas of freestanding graphene drums (circular areas of dimmer brightness), graphene on SiO2 (lighter areas) and areas of no graphene (black areas). Bottom right, optical image of the Raman scan area.

<table>
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Table 1. The wavenumber Raman peak values for D, G and 2D for freestanding and SiO2 bonded graphene and their corresponding FWHM and intensity ratios.

5. AFM ANALYSIS OF DRUM SHAPE

Optical and AFM images of the chip with transferred graphene have been recorded. Optical images are capable of showing the presence of graphene films, particularly as the SiO2 layer on the Si is 300nm, a thickness which is chosen to give good interference colour contrast [40]. It is also possible to see that some depressions are not covered by graphene, others are partially covered. Also, interestingly some graphene membranes sag into the depressions, appearing to touch the bare Si base. AFM images confirm this behaviour quantitatively. Some suspended graphene membranes show different behaviour. In these cases the AFM images show a bulge rather than sagging. The AFM line scans across the centre of a 2µm diameter hole and a 5µm square which a single graphene layer is stretched in the transfer process is shown in Fig 6 and 7 respectively.
FIG. 6: AFM line scans across a 2µm diameter graphene drums. In the sequence of images the AFM set-point is successively increased. The bulge in the membrane increases at first but then in the final image the membrane goes slack.

FIG. 7: AFM line scan across a 5µm diameter graphene square.

It is interesting to try to fit the measured shape of the membrane to a simple model of excess pressure on the constrained side of the graphene. Note that it has been observed that graphene is surprisingly impermeable to all gases with the exception of water vapour (or even liquid water) [41]. Equation 2 shows the total force on the membrane of radius R with excess pressure Δp across it and is pictured in Fig 8.

\[ F = ΔpπR^2 = 2πσRsin(α) \]  

Here σ is the stress in the membrane which is related to the radial strain ε and the membrane Young’s modulus E by the expression

\[ σ = \frac{εE}{1-ν^2} \]
where $v$ is Poisson’s ratio for graphene and is believed to be approximately equal to 0.2.

We ignore the residual stress $\sigma_0$ and assume only that arising from Hooke’s law since any residual stress would cause even higher values of $\Delta p$. The result of the central bulge by an amount $\Delta z(0)$ allows us to calculate the additional length of the parabolic shaped membrane if we know the tangential angle $\alpha$ at its circumference. For small deflections ($\Delta z(0) << R$) $\sin(\alpha) \approx \Delta z(0)/R$ allowing us to derive the final expression for $\Delta p$.

$$\Delta p = \frac{8\Delta z(0)^3 R t}{3R^4(1-v^2)}$$  \hspace{1cm} (4)

Consider the AFM line-scan shown in Fig 6. For now we ignore the internal stress. The displacement of the graphene membrane centre $\Delta z(0)$ is some 25nm above the level of the Si wafer surface. The radius $R$ is 1$\mu$m, the membrane thickness $t$ is 0.4nm since the graphene is shown to be predominantly single layer via Raman analysis in Section 4. Finally the Youngs modulus $E$ has values in the range 0.3 to 1.0 TPa for graphene. Even assuming the lower of these values the pressure difference $\Delta p$ required to produce such a bulge is around 0.2 atmospheres which is not realistic given that all transfer and processing is done at room pressure and temperature. The fact that some membranes sag also indicates that there is not an excess pressure within the wells.

We tentatively rule out this as a possible source of the convex parabolic bulge of the membranes. Instead we regard the observed shape of the membranes as arising from the attractive (van der Waals) force between the AFM tip and the surface of the membrane. This explanation is supported by a scan of the same area with reduced separation between the AFM tip and the surface (achieved by changing the AFM control electronics set point). Now the bulge at the centre of the membrane above the substrate is increased, which would not happen if the bulge was only due to excess pressure. Further increase of the AFM set point (i.e. closer contact and therefore higher attractive force) leads to a dramatic shape change on scanning. Now the bulge disappears and the shape of the membrane becomes ill-defined. We believe this may be explained by the increasing attractive force between AFM tip and membrane becoming sufficient to overcome the adhesive force between the vertical wall of the well and the graphene membrane which had been drawn into it. When the force is sufficient to pull the membrane up and away from the vertical wall the diameter of the membrane becomes greater than the diameter of the hole and therefore the membrane is no longer constrained and becomes flexibly positioned, as shown in the lowest image of Fig 6. On reversing this process and reducing the force between membrane and AFM tip the van der Waals forces become sufficient to draw the graphene membrane in again to the vertical wall of the hole, leading to a return to the original bulging shape. This explanation also is supported by some observations we have made on mechanical resonances of these membranes. We have measured the piezo excited mechanical resonances using a novel near-field microwave readout method [42, 43]. These resonances show modest quality factors (Q) in air due, we believe, to air damping. These results show that, as the piezo drive force increases, non-linear behaviour is observed. Unlike most other mechanical systems, the non-linearity leads to softening of the membrane i.e. the resonant frequency reduces with increased drive level. This could again be interpreted as the effective radius of the membrane being increased as the side-wall length is reduced at higher drive levels. We will describe this effect in more detail elsewhere.

![FIG. 8: Schematic of shape of thin membrane under the influence of excess pressure $\Delta p$.](image)
6. CONCLUSIONS

Graphene is a remarkable material in many different ways. In this paper we demonstrate that a wafer-scale growth technique, chemical vapour deposition, followed by a polymer based wet transfer method is capable of allowing large areas (several square mm) to be transferred onto a substrate giving freely suspended graphene membranes with relatively high yield of intact resonators. We show that these can be non-destructively imaged by AFM and can be manipulated by the same scanned technique. Furthermore these membrane resonators show an unexpected non-linear behaviour which is explained by the sagging of unstrained graphene into the supporting well shapes. The remarkable resilience of self-supporting single atomic layers over microns of distance reinforces the belief that graphene mechanical resonators can provide exceptional sensors for example detection of single molecule adsorbed masses. Since the areal mass of single layer graphene is so extremely small and frequency is such an accurately measured parameter the frequency shift produced by adsorption of a single molecule on a graphene drum should be readily detectable, even at room temperature. This should lead to a significant range of useful applications in biology and more widely in sensitive detection.

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