

The EMPIR initiative is co-funded by the European Union's Horizon 2020 research and innovation programme and the EMPIR Participating States







Effects of coaxial cables on high-voltage lightning impulse measurement parameters: A comparison between measurements and simulations

A. Khamlichi<sup>1,2</sup>, J. Hällström<sup>3</sup>, J. Havunen<sup>3</sup>, F. Garnacho<sup>1,2</sup>, J. Rovira<sup>1</sup>

<sup>1</sup>FFII-LCOE, High Voltage Technological Center, Madrid, Spain <sup>2</sup>Polytechnic University of Madrid, Madrid, Spain <sup>3</sup>VTT Technical Research Centre of Finland Ltd, National Metrology Institute VTT MIKES, Finland

### 1. INTRODUCTION

Common practice for high-voltage lightning impulse (LI) measurements is based on voltage dividers whose output is a low voltage signal related to the high voltage impulse to be measured. This output is connected to a measuring instrument by a coaxial measuring cable. The selection of this coaxial measuring cable is usually done according to their characteristic impedance, attenuation and shielding effectiveness. Several meters or some tens of meters long measuring cables are used. As a general practice, little attention is paid to the effect of cable length on the measured signal at the output of the divider; however, cable characteristics, such as attenuation or capacitance, can differ significantly between different cables, even though they have the same characteristic impedance. Consequently, the length of the cable can affect the signal waveform depending on the characteristics of the cable.

Attenuation and distortion caused by a measuring cable can be determined accurately by modelling and by software simulation. The coaxial cable is a special case of a transmission line, whose model is based essentially on a series impedance and a parallel admittance that are frequency dependent functions, being the series impedance the one that has a strong variation with the frequency. These frequency dependent functions for coaxial cables can be determined from the equations proposed by Schelkunoff.

# 3. EXAMPLE

The error on the front time parameter,  $T_1$ , is analyzed by varying the measuring cable length. This analysis is carried out by measurements and by simulation. Fig. 2 shows the schematics and the values of the different elements for a considered capacitive damped divider.

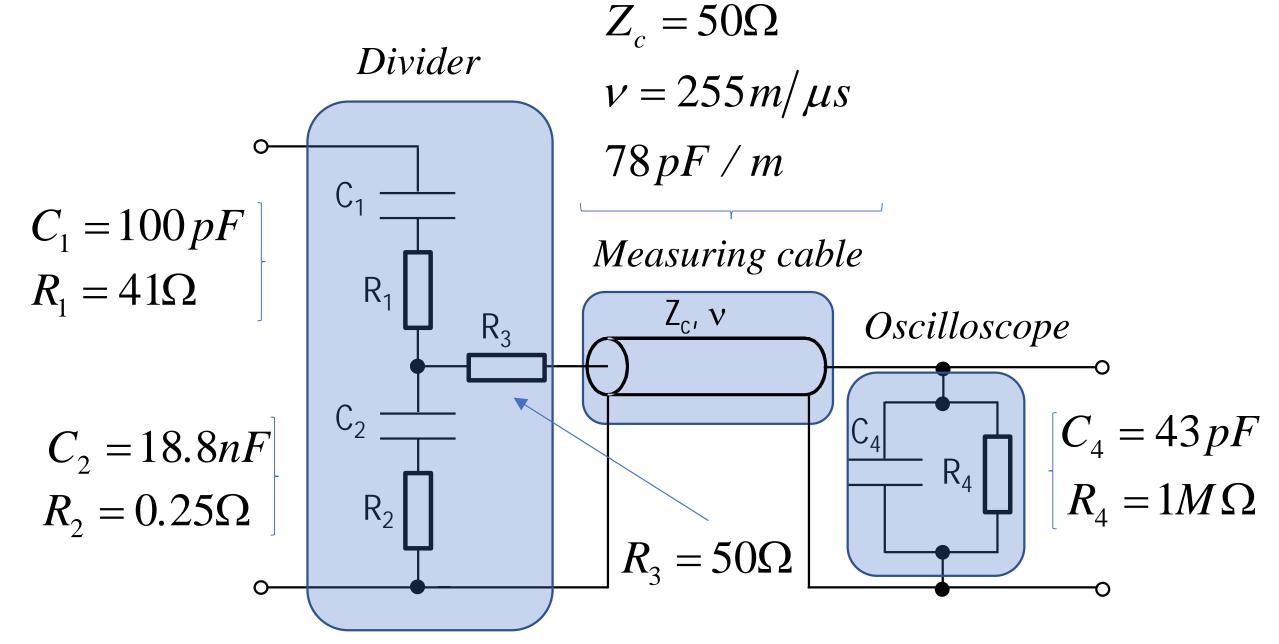


Fig. 2. Schematics for the considered capacitive damped divider.

A reference scenario with no cable connected (cable length = 0 m) has been considered, when a lightning impulse is applied ( $0.84/60 \ \mu s$ ).

#### 2. THEORETICAL BASIS

Conventional damped-capacitive lightning impulse measuring systems, as the one shown in Fig. 1, are composed by five different elements: a high-voltage arm  $Z_1$ , a low-voltage arm  $Z_2$ , a matching impedance  $Z_3$  adjusted according to the characteristic impedance  $Z_c$  of the coaxial measuring cable, and a measuring instrument with input impedance of  $Z_{4}$ .

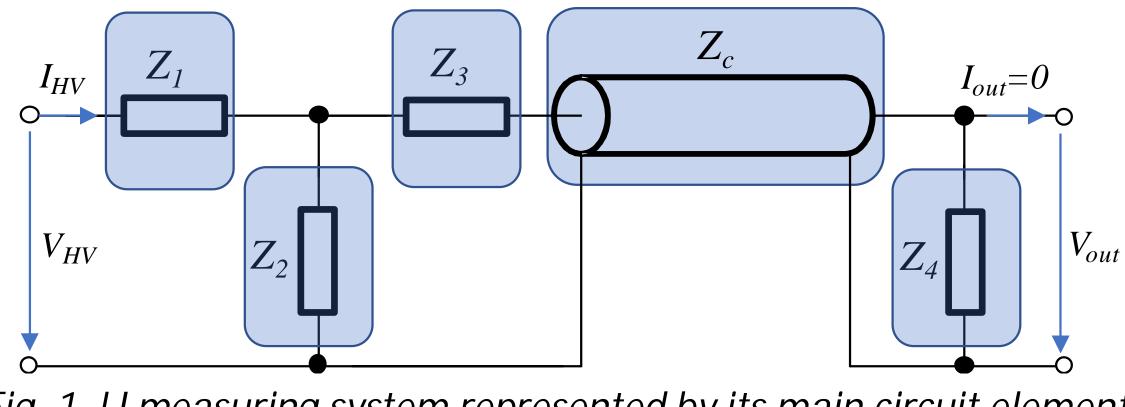


Fig. 1. LI measuring system represented by its main circuit elements.

The frequency behaviour of this equivalent circuit can be analysed as a twoport network or quadrupole. The frequency domain output voltage and current in the digital recorder input,  $V_{out}(s)$  and  $I_{out}(s)$ , are related to the input voltage and current Laplace functions at the high voltage side ( $V_{HV}(s)$  and  $I_{HV}(s)$ ) through the ABCD transmission matrix, according to

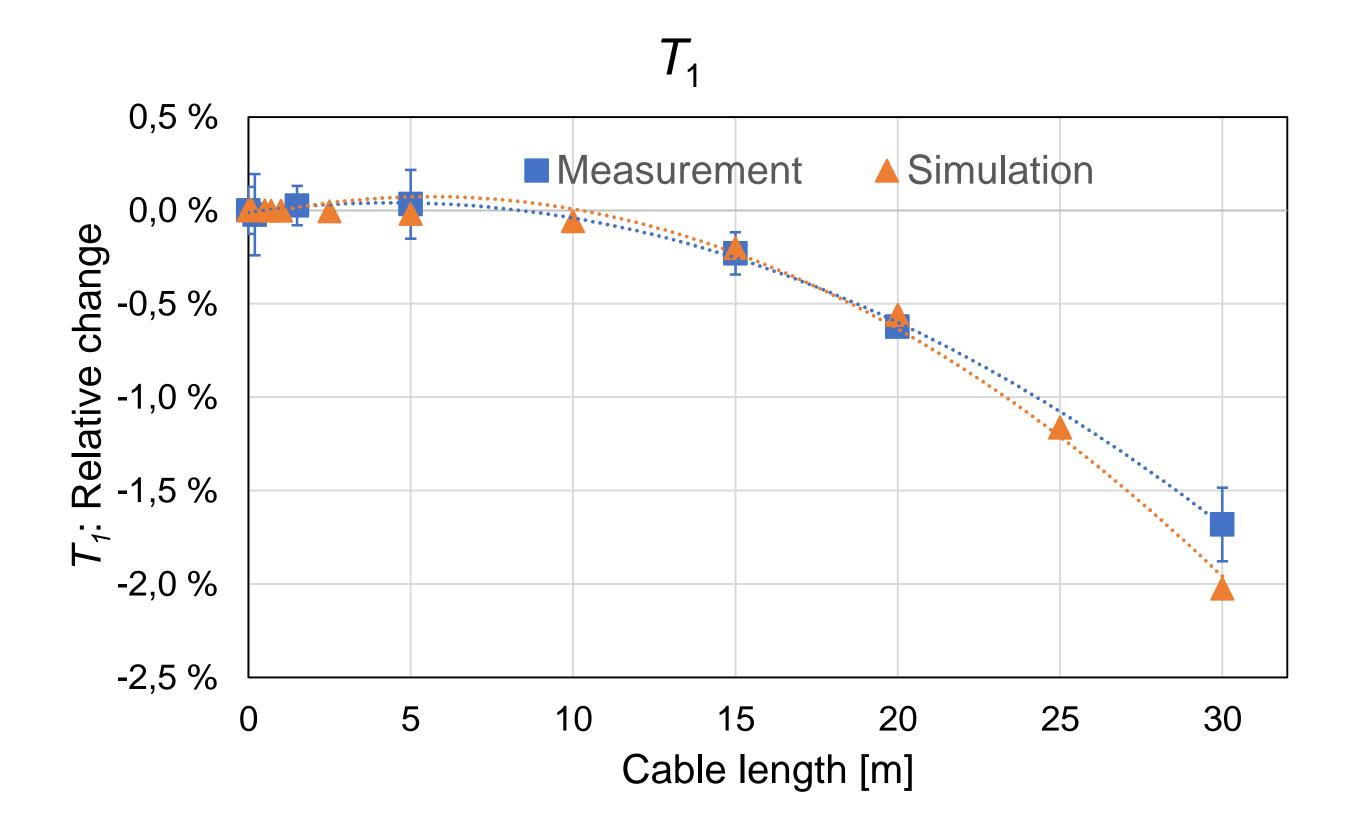
$$\begin{bmatrix} V_{out}(s) \\ I_{out}(s) \end{bmatrix} = \begin{bmatrix} A(s) & B(s) \\ C(s) & D(s) \end{bmatrix} \cdot \begin{bmatrix} V_{HV}(s) \\ I_{HV}(s) \end{bmatrix}$$
(1)

In the simulation the  $C_1$  to  $C_4$ ,  $R_1$  to  $R_4$  and cable capacitance and conductance were assumed to be frequency independent. The frequency dependencies of cable resistance and inductance were estimated.

Comparative results for the measurements and for the simulations are shown in Fig. 3. Simulation results achieve a good fitting to the measurement. The obtained results show an increasing error when the cable length is increased.

## 4. CONCLUSION

The results of this work show that the cable length has clear influence on measured LI voltage, especially on its front time. Additionally, an accurate model that can be used to estimate measurement errors is available to simulate measuring coaxial cables applied to high voltage measuring systems.



where the transmission parameters A(s), B(s), C(s) and D(s) are expressed using Laplace variable, s. To determine them, individual quadrupoles of the five different elements shown in Fig. 1 are considered. For an applied high voltage  $V_{HV}(s)$ , the output voltage function  $V_{out}(s)$  can be determined by the following equations, by considering the boundary condition  $I_{out}=0$ :

$$I_{out}(s) = 0 \rightarrow I_{HV}(s) = -\frac{C(s)}{D(s)} \cdot V_{HV}(s)$$
(3)

 $V_{out}(s) = A(s) \cdot V_{HV}(s) + B(s) \cdot I_{HV}(s)$ (4)

where  $I_{HV}(s)$  is the frequency function of the current at the high-voltage side.

For obtaining the time function  $u_{out}(t)$  corresponding to  $V_{out}(s)$  a dedicated numerical inversion of Laplace transform has been used.

Fig. 3. Comparative results for the measurements and for the simulation.

#### ACKNOWLEDGEMENT

This project 19ENG02 FutureEnergy has received funding from the EMPIR programme co-financed by the Participating States and from the European Union's Horizon 2020 research and innovation programme.