

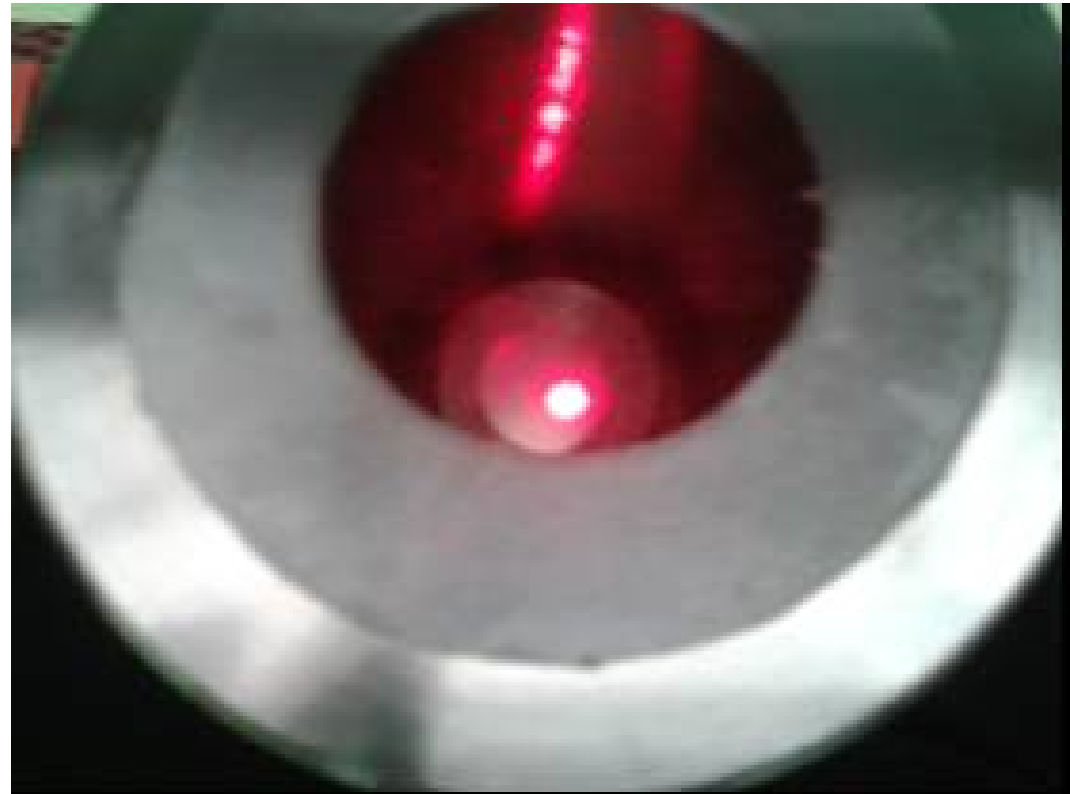


# ***DYNAMIC CALIBRATION OF FORCE TRANSDUCERS AT CEM***

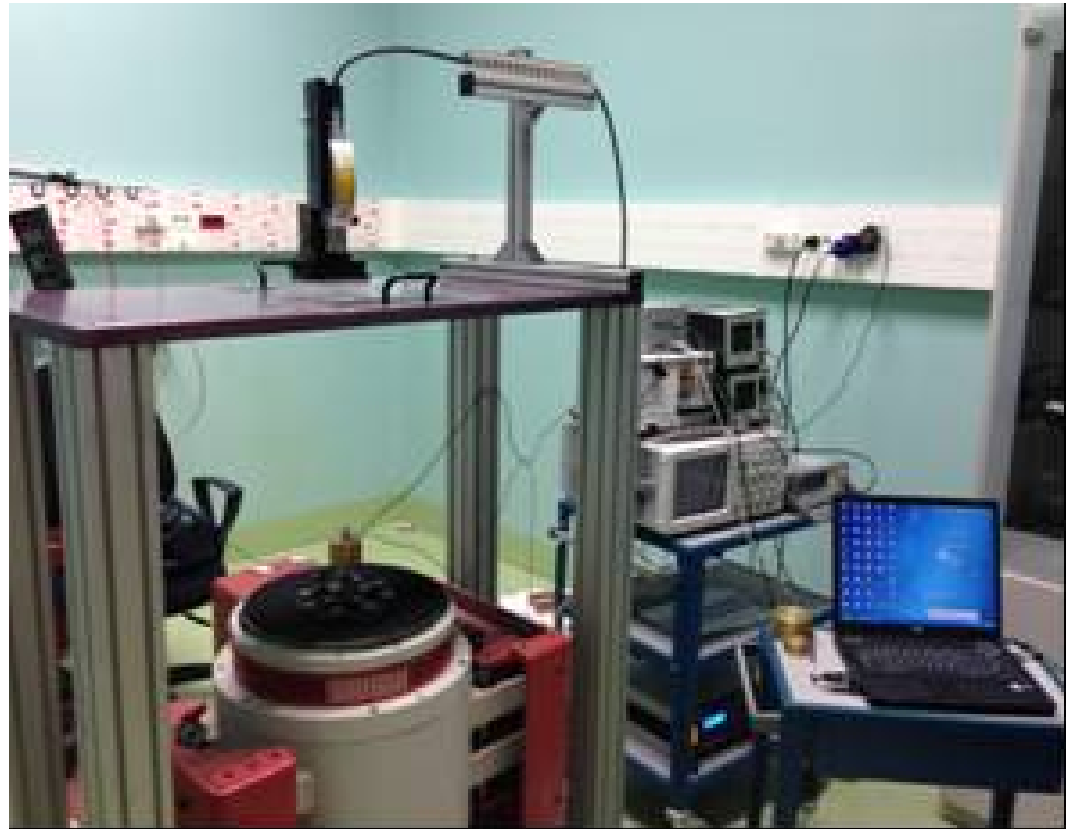
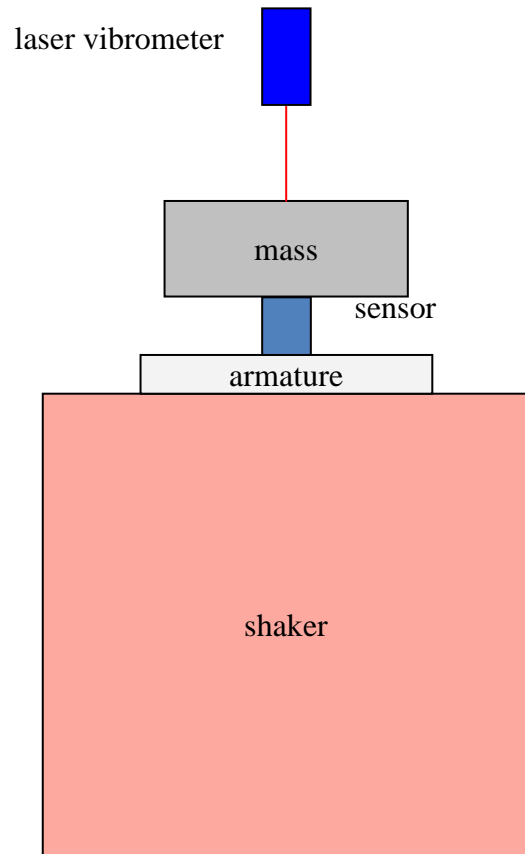
***Nieves Medina and Jorge Robles***

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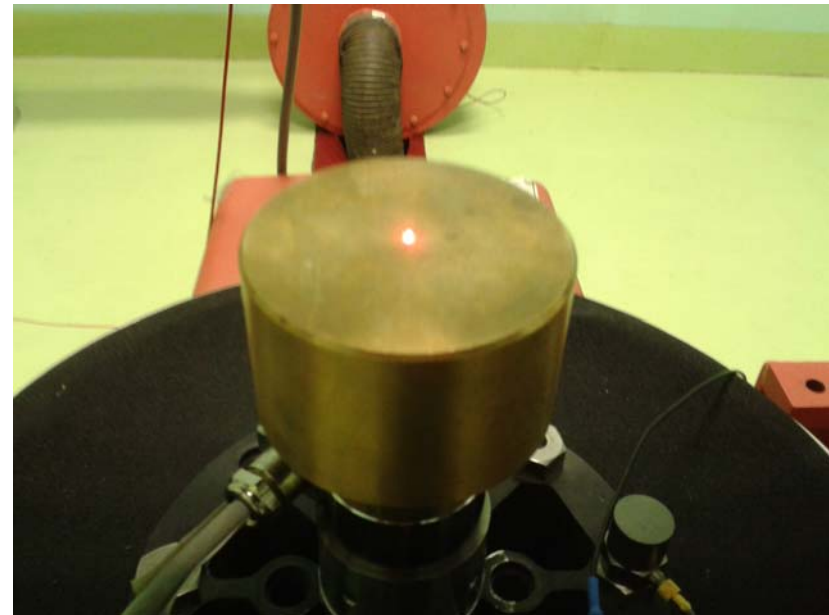
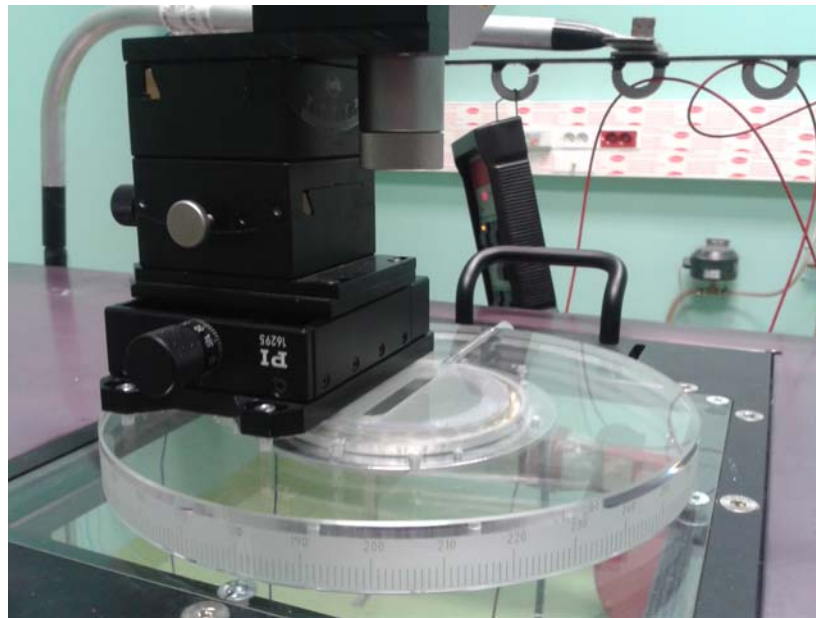


# System



## Laser vibrometer

The laser vibrometer is a modified Mach-Zehnder interferometer and it incorporates a Bragg cell (opto-acoustic modulator).



## Masses

Nominal values: 350 g, 1 kg, 2 kg, 7.3 kg and 12.3 kg

Special adaptors may be required in order to attach the masses to the sensor or the sensor to the shaker.



## Shaker

Frequency: 5 Hz to 2400 Hz  
Acceleration: 600 m/s<sup>2</sup>

## Auxiliary accelerometer

B&K 8305



## Data acquisition system

NI PXI 1033 module with a 4462 card (24 bits, 204.8 kS/s)

- Programmed in Labview
- Sampling: each signal separately with 40kS/s
- Excitation frequency directly detected by the software

**AIM: avoid harmonic distortion and noise**

## Sine approximation method

$$a(t_i) = A \cos(2\pi f t_i) - B \sin(2\pi f t_i) + C$$

*Up to 3<sup>rd</sup> harmonic*

$$\begin{aligned} a(t_i) = & A_0 \cos(2\pi f t_i) - B_0 \sin(2\pi f t_i) + C + \\ & + A_1 \cos(4\pi f t_i) - B_1 \sin(4\pi f t_i) + \\ & + A_2 \cos(6\pi f t_i) - B_2 \sin(6\pi f t_i) + \\ & + A_3 \cos(8\pi f t_i) - B_3 \sin(8\pi f t_i) \end{aligned}$$

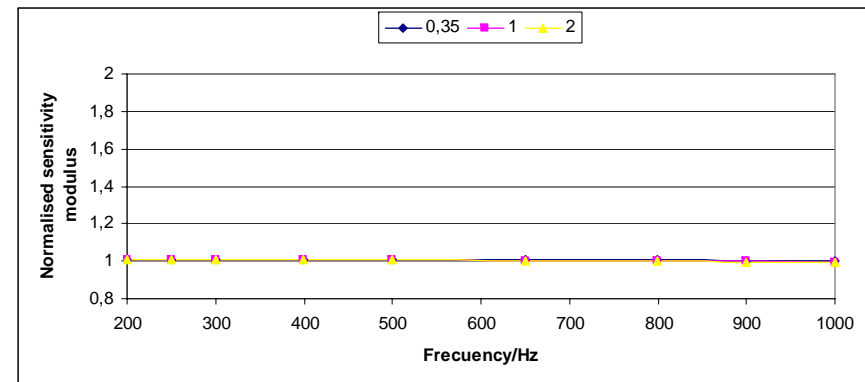
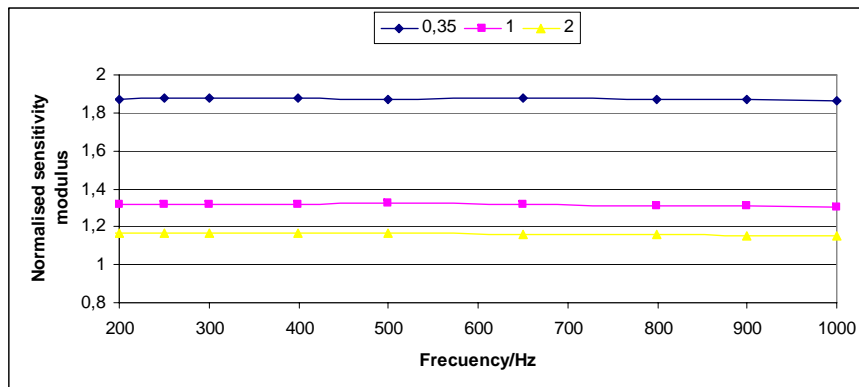
*Amplitude and phase*

$$\begin{aligned} \hat{a} &= \sqrt{(A_0)^2 + (B_0)^2} \\ a_\varphi &= \arctan\left(\frac{A_0}{B_0}\right) \end{aligned}$$

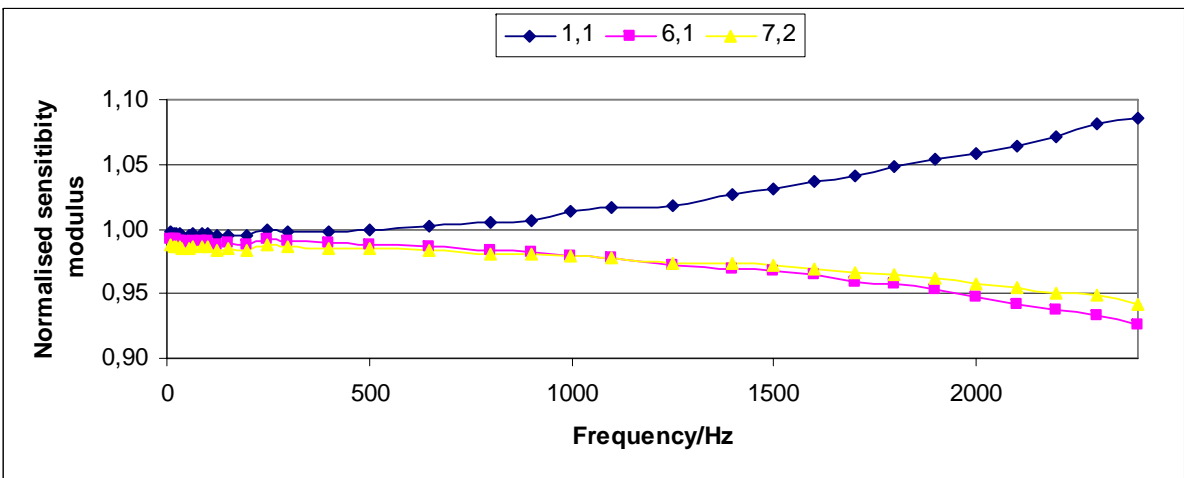
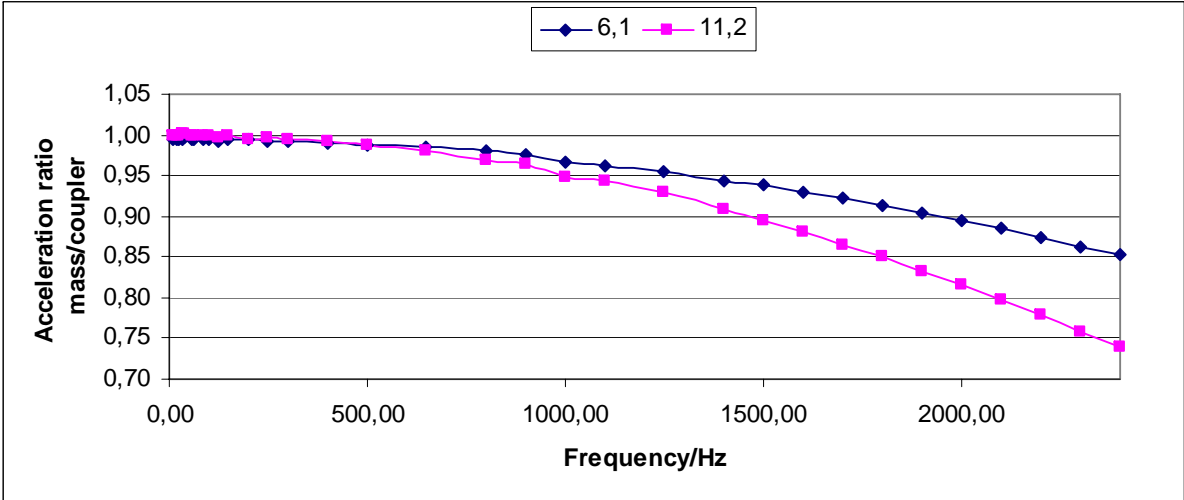
# Measurement model

$$S = \frac{U/V}{(m + m_i) \cdot a}$$

$$S = |S| \cdot e^{i\varphi}$$



$$m_i = 315 \text{ g}$$

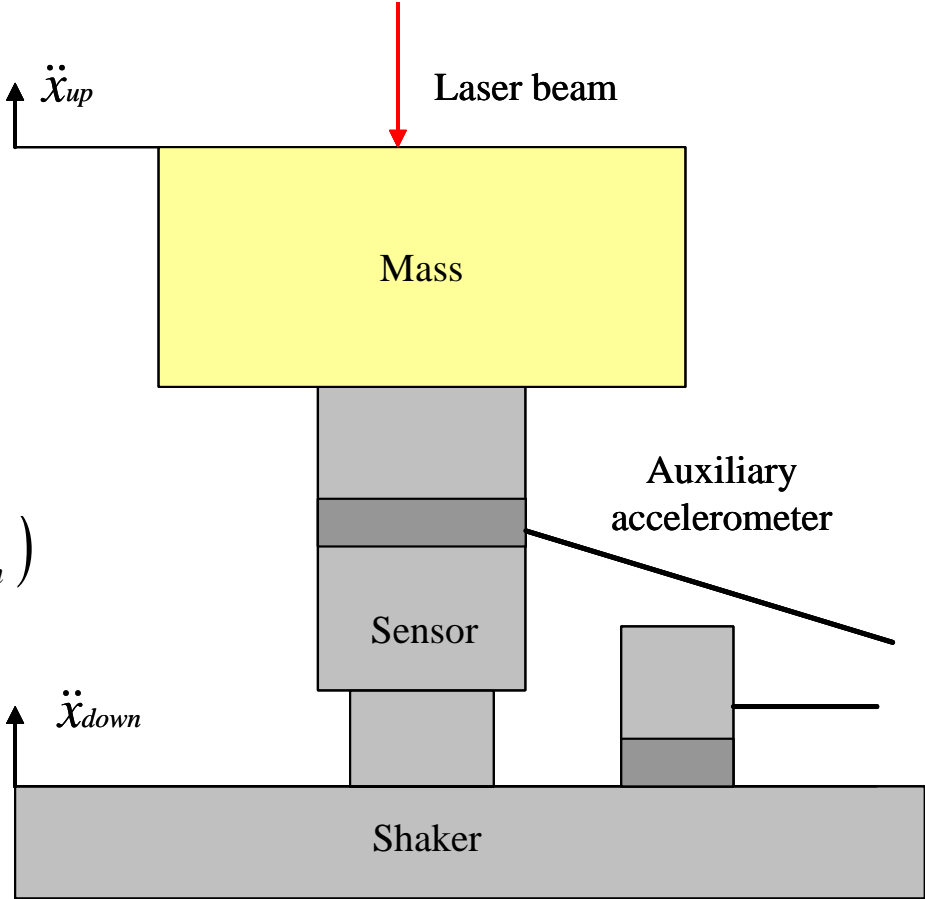


$$S = \frac{m_1 + m_2}{\frac{m_1 + m_s}{S_1} + \frac{m_2}{S_2}}$$

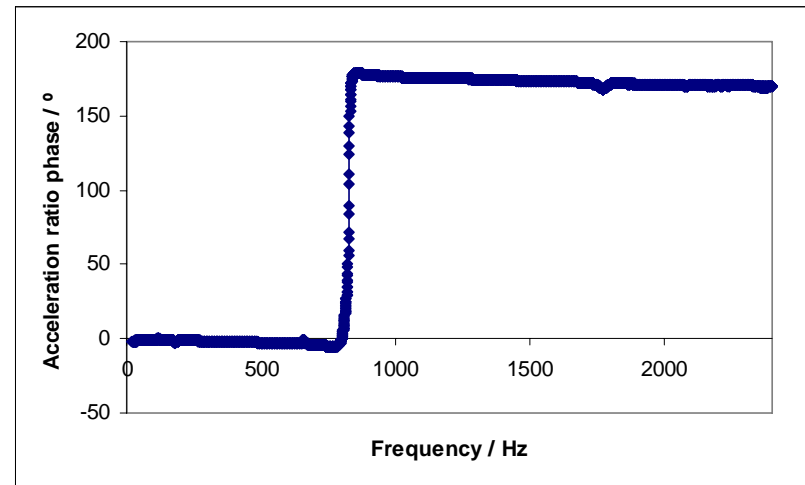
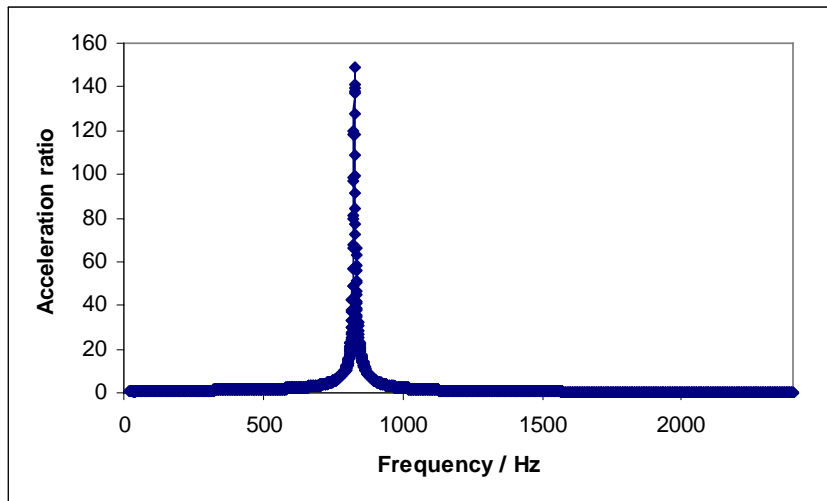


*Mechanical resonator*

$$m \cdot \ddot{x}_{up} = -k \cdot (x_{up} - x_{down}) - b \cdot (\dot{x}_{up} - \dot{x}_{down})$$



$$\frac{a_{up}}{a_{down}} = \frac{k + ib\omega}{k + ib\omega - m\omega^2}$$



# Influence factors

## Type B

Uncertainty contribution	Contribution to the sensitivity modulus	Contribution to the sensitivity phase
Data acquisition system	0.05 %	$2 \times 10^{-5}$ °/frequency
Laser vibrometer	0.1 %	0.25 °
Conditioning amplifier	0.05 %	0.25 °
Sensor temperature	< 0.06%	-
Loading mass	0.01%	-



## Type A

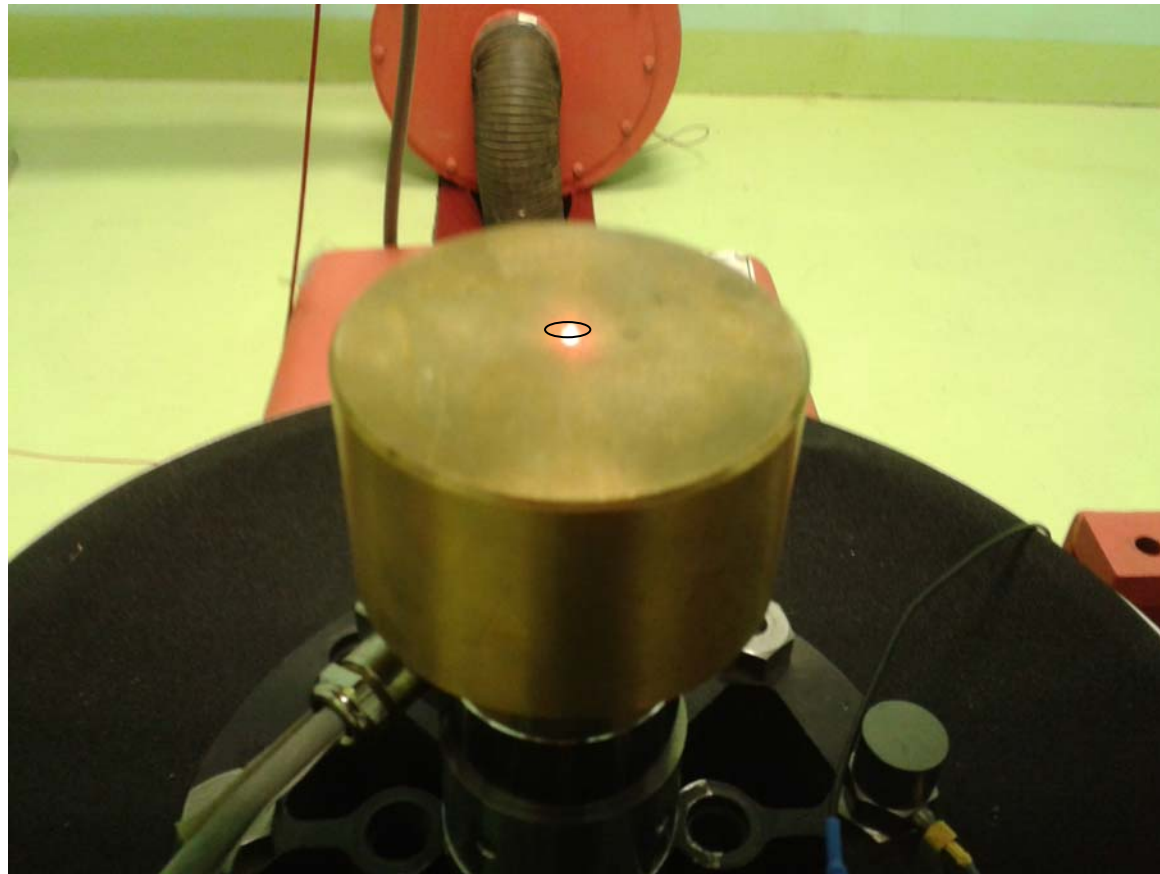
- Harmonics and noise
- Repeatability
- Transverse acceleration and rocking motion
- Reproducibility of mounting

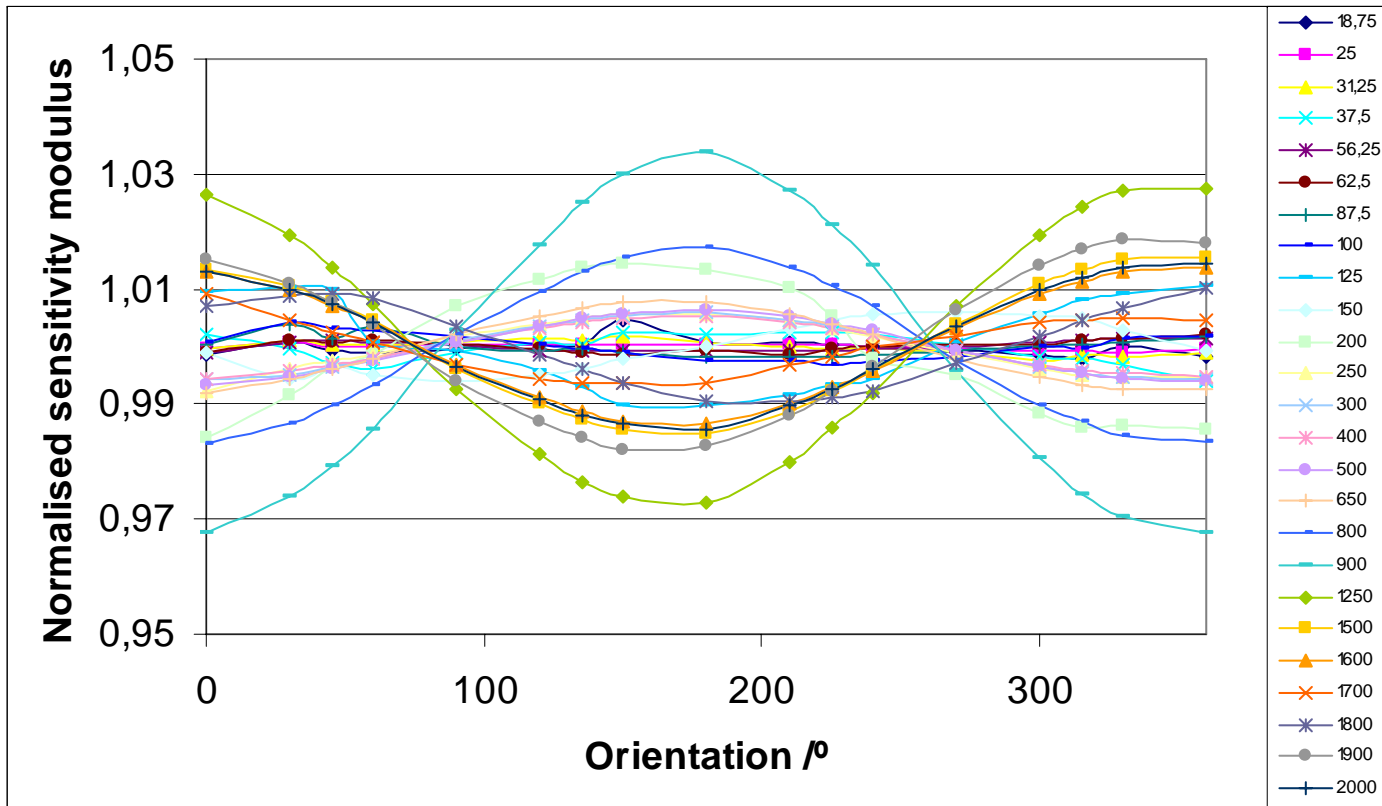
*Harmonics and noise* - Sine approximation method (40kS)

*Repeatability* - 10 measurements

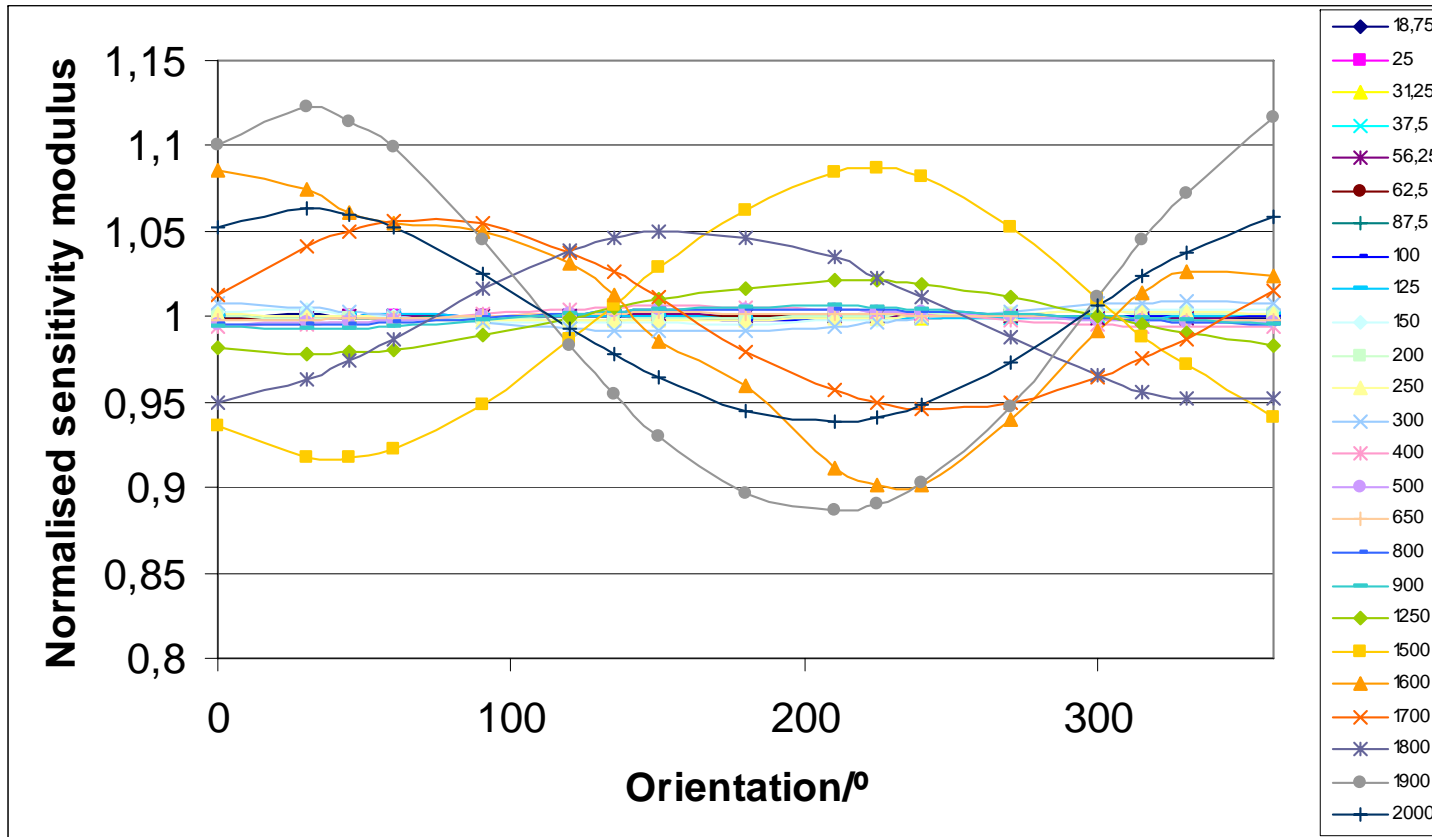
} NEGLIGIBLE

## Transverse acceleration and rocking motion

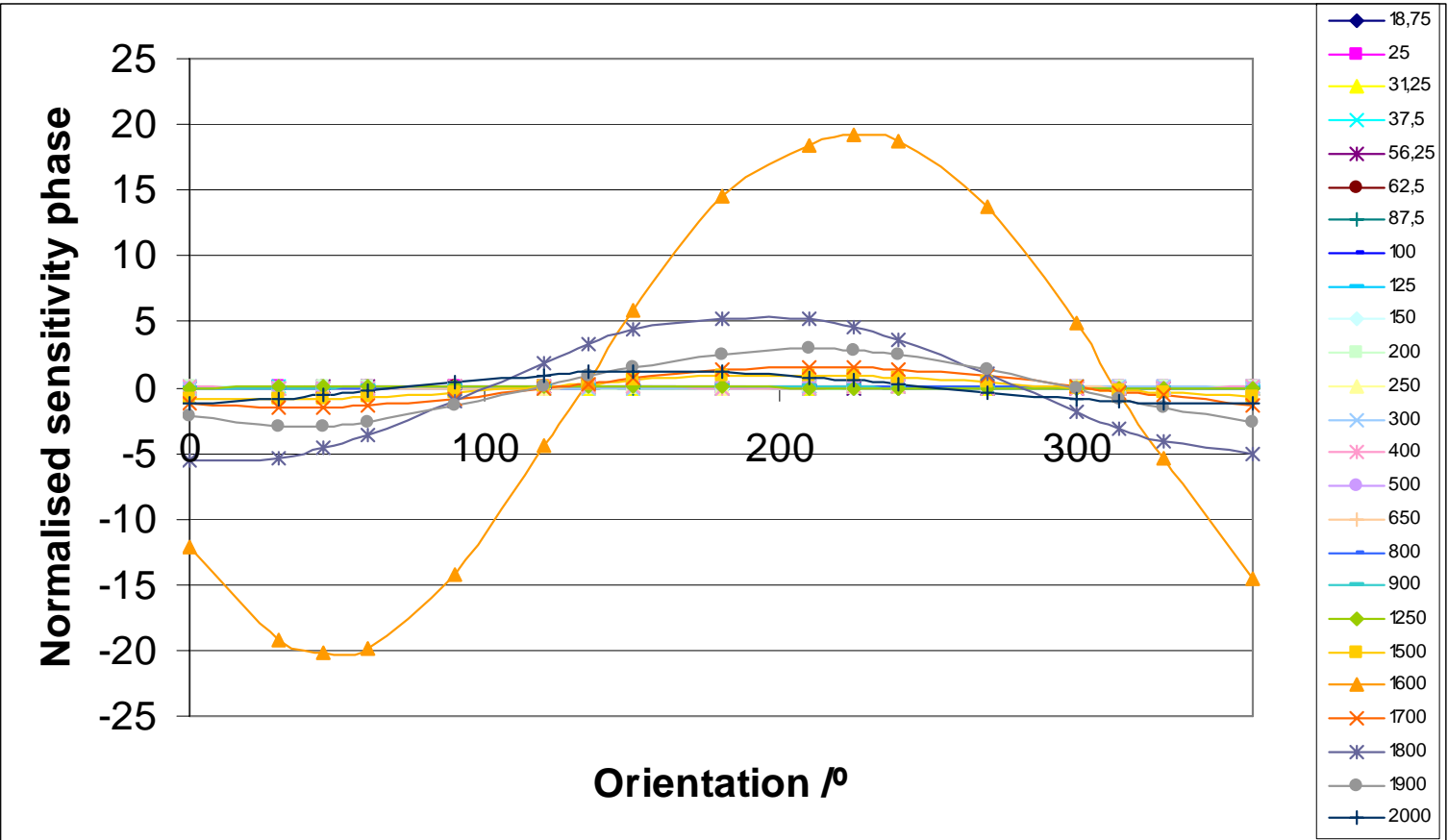




Load = 7.2 kg, radius = 1 cm

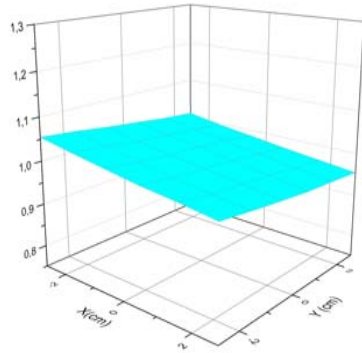


Load = 2 kg, radius = 1.7 cm

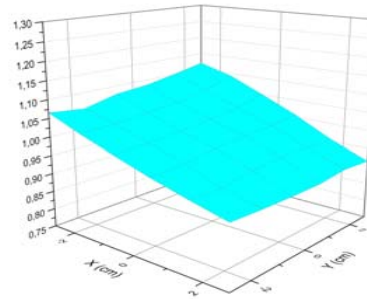


Load = 2 kg, radius = 1.7 cm

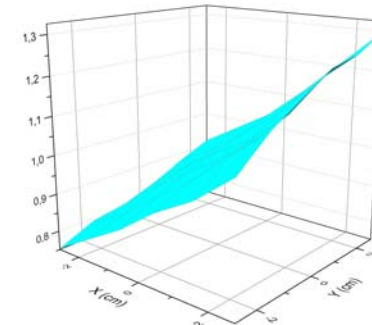




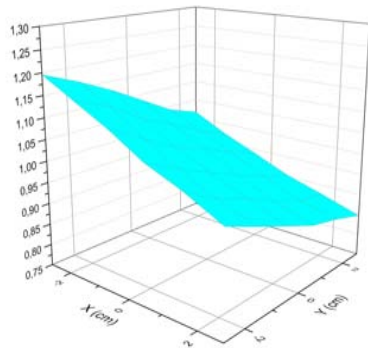
1.25 kHz



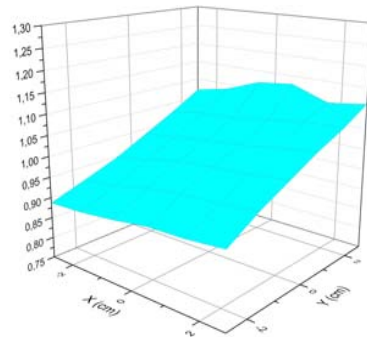
1.8 kHz



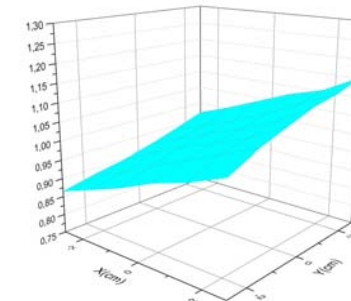
1.9 kHz



1.5 kHz

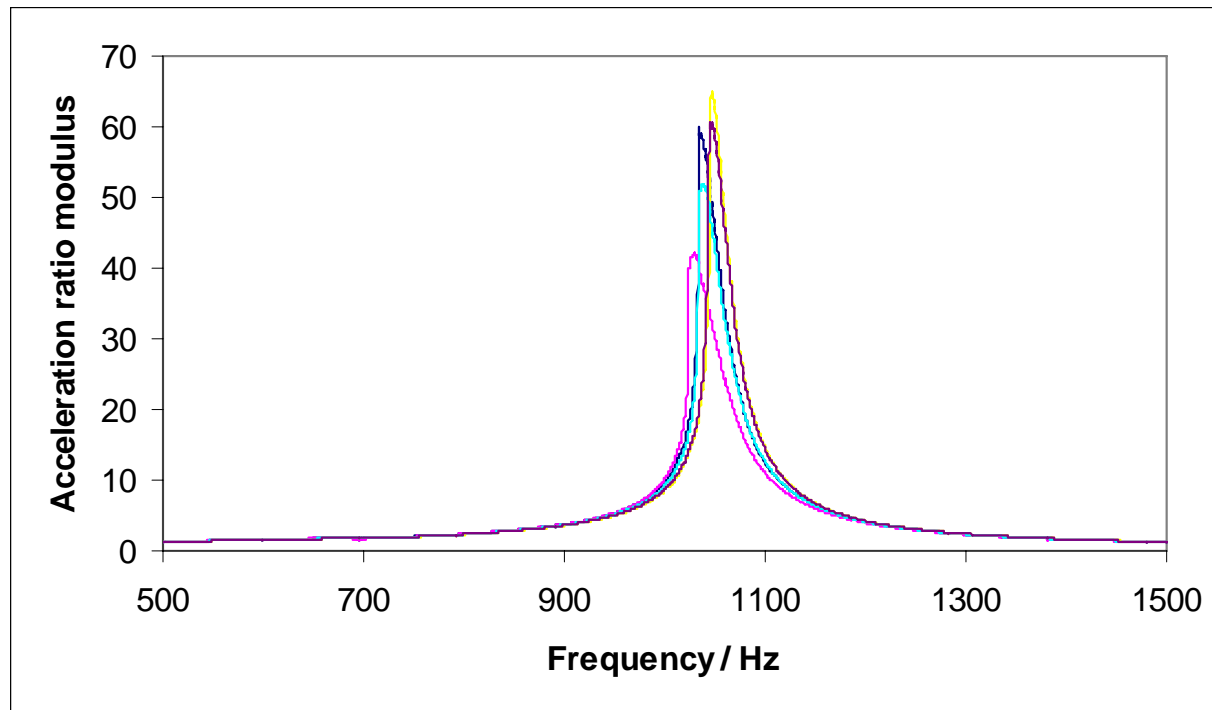


1.7 kHz



2 kHz

## Reproducibility of mounting



Special care has to be taken to ensure that the contact between pieces is made by means of flat surfaces.

The torque which is applied to connect the different parts is also under careful control.

# Conclusions

- Primary standard for dynamic forces

- Main influence: rocking motion

- Best uncertainty  $\left\{ \begin{array}{l} 0,5 \% \\ 1^\circ \end{array} \right. \longrightarrow 3 \%$

This work is part of the EMRP project  
“Traceable dynamic measurement of mechanical quantities”



**Thank you very much  
for your attention**

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