

Atomic clocks with suppressed blackbody radiation shift

V. I. Yudin*, A. V. Taichenachev, M. V. Okhapkin†, and S. N. Bagayev
Institute of Laser Physics SB RAS, Novosibirsk 630090, Russia
Novosibirsk State University, Novosibirsk 630090, Russia and
Novosibirsk State Technical University, Novosibirsk 630092, Russia

Chr. Tamm, E. Peik, N. Huntemann, T. E. Mehlstäubler, and F. Riehle
Physikalisch-Technische Bundesanstalt (PTB), Bundesallee 100, 38116 Braunschweig, Germany
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We develop a nonstandard concept of atomic clocks where the blackbody radiation shift (BBRS) and its temperature fluctuations can be dramatically suppressed (by one to three orders of magnitude) independent of the environmental temperature. The suppression is based on the fact that in a system with two accessible clock transitions (with frequencies ν_1 and ν_2) which are exposed to the same thermal environment, there exists a “synthetic” frequency $\nu_{\text{syn}} \propto (\nu_1 - \varepsilon_{12}\nu_2)$ largely immune to the BBRS. As an example, it is shown that in the case of $^{171}\text{Yb}^+$ it is possible to create a clock in which the BBRS can be suppressed to the fractional level of 10^{-18} in a broad interval near room temperature (300 ± 15 K). We also propose a realization of our method with the use of an optical frequency comb generator stabilized to both frequencies ν_1 and ν_2 . Here the frequency ν_{syn} is generated as one of the components of the comb spectrum and can be used as an atomic standard.

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The main progress in modern fundamental metrology is connected with the development of atomic clocks. The most promising frequency standards today are based on single trapped ions [1] and on ensembles of neutral atoms confined to an optical lattice at the magic wavelength [2, 3]. It is believed that these clocks can provide frequency references with unprecedented small systematic uncertainties in the 10^{-17} - 10^{-18} range. This progress will probably lead to a redefinition of the unit of Time and to new fundamental tests of physical theories in particular in the fields of General Relativity, cosmology, and unification of the fundamental interactions [4, 5].

The largest effect that contributes to the systematic uncertainty of many atomic clocks is the interaction of the thermal blackbody radiation with the atomic eigenstates. This effect was first considered in 1982 for cesium atomic clocks [6], but remains up to now a major problem for many modern atomic time and frequency standards. At present there exist three approaches to tackle the blackbody radiation shift (BBRS) problem. The first one is the use of cryogenic techniques to suppress this shift to a negligible level. This approach is pursued for the mercury ion clock [7], for the Cs fountain clock [8], and for the Sr optical lattice clock [9]. The second approach is the precise temperature stabilization of the experimental setup in combination with theoretical and/or semiempirical numerical calculations of the shift at given temperature [10, 11]. The third approach is based on the

choice of an atom or ion where both levels of the reference transition have approximately the same BBRS. Here the most promising candidate is $^{27}\text{Al}^+$ with a fractional BBRS of the reference transition frequency of $\sim 10^{-17}$ [1, 12], followed by $^{115}\text{In}^+$ [13, 14]. However, the latter approach limits the choice of candidates for tests of fundamental theories.

In the present paper we propose an alternative method allowing us to suppress the BBRS and its fluctuations in atomic frequency standards by one to three orders of magnitude without using cryogenic techniques and precise temperature stabilization. Our approach is based on the use of two reference transitions in an identical thermal environment. We show that in such a system there exists a combined frequency for which the BBRS is significantly suppressed over a wide temperature range. For instance, a trapped $^{171}\text{Yb}^+$ ion meets this condition in a straightforward way, because $^{171}\text{Yb}^+$ has at least three suitable reference transitions: an electric-quadrupole and an electric-octupole optical transition [15–17], and a magnetic-dipole radiofrequency (rf) transition between the ground-state hyperfine sublevels. Apart from laboratory standards, the proposed method can be particularly useful in cases where it is impossible to control the environmental temperature with sufficient accuracy or to use cryogenic techniques, for instance in transportable frequency standards or in space-based clocks that approach the Sun in order to test the local position invariance underlying General Relativity [4].

Our approach is based on the fact that for the large majority of transitions in atoms or ions that are of interest as frequency standard reference transitions, the temperature dependence $\Delta(T)$ of the BBRS is very well approx-

*e-mail address: viyudin@mail.ru

†also PTB

imated by the law $\propto T^4$. Consider now two clock transitions with frequencies $\nu_1^{(0)}$ and $\nu_2^{(0)}$ exposed to the same thermal environment, i.e., located in the same probe volume. We assume that $\nu_1^{(0)} < \nu_2^{(0)}$. The effect of the BBRs on each transition frequency can be represented as:

$$\nu_j(T) \approx \nu_j^{(0)} + a_j \left(\frac{T}{T_0} \right)^4 \quad (j = 1, 2), \quad (1)$$

where a_j is an individual characteristic of the transition j determined by the atomic structure and T_0 is the mean temperature of the clock operation. Let us introduce the coefficient $\varepsilon_{12} = a_1/a_2$. As is easily seen, the following superposition does not experience the BBRs: $\nu_1(T) - \varepsilon_{12}\nu_2(T) = \nu_1^{(0)} - \varepsilon_{12}\nu_2^{(0)}$. In compliance with this we define a new ‘‘synthetic’’ frequency ν_{syn} as

$$\nu_{\text{syn}} = R[\nu_1(T) - \varepsilon_{12}\nu_2(T)] = R[\nu_1^{(0)} - \varepsilon_{12}\nu_2^{(0)}], \quad (2)$$

where R is some numerical multiplier whose value can be chosen freely. Thus, one can use the frequency ν_{syn} as a new clock output frequency which is immune to the BBRs and to fluctuations in the operating temperature, while the thermal shifts $a_j T^4$ of the working frequencies ν_j can be large.

One possibility is to independently measure both frequencies $\nu_{1,2}(T)$ and to use for the clock operation the synthetic frequency according to Eq. (2) (assuming, for example, $R = \pm 1$). In this case, obviously the synthetic frequency does not directly correspond to any frequency of a physical signal. Another approach is to synthesize this frequency as a real physical signal by means of an optical frequency comb generator. Let us consider the situation where two modes of the frequency comb generator are stabilized to the two optical frequencies $\nu_{1,2}(T) = f_0 + n_{1,2}f_r$ at a given temperature T (see Fig.1). As a result, the parameters of the comb spectrum, i.e., the pulse repetition rate f_r and the offset frequency f_0 are unambiguously determined and the frequency of the m -th mode equals:

$$\begin{aligned} \nu_m(T) &= f_0 + m f_r = \\ &= \frac{m(\nu_2^{(0)} - \nu_1^{(0)}) + n_2 \nu_1^{(0)} - n_1 \nu_2^{(0)}}{n_2 - n_1} + \\ &= \frac{m(a_2 - a_1) + n_2 a_1 - n_1 a_2}{n_2 - n_1} \left(\frac{T}{T_0} \right)^4. \end{aligned} \quad (3)$$

From this expression one can define a number $m = m_0$ for which the coefficient of the temperature-dependent term is zero:

$$m_0 = \frac{n_1 a_2 - n_2 a_1}{a_2 - a_1} = \frac{n_1 - \varepsilon_{12} n_2}{1 - \varepsilon_{12}}. \quad (4)$$

This shows that the BBRs is suppressed for the frequency ν_{m_0} . After a simple transformation we see that the fre-

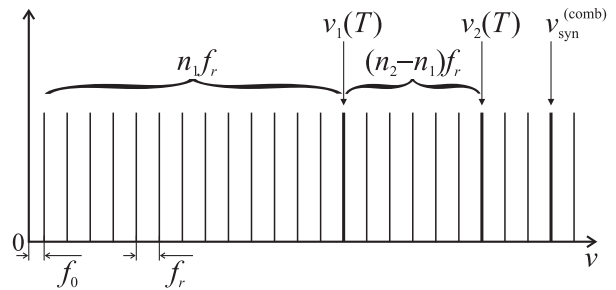


FIG. 1: Illustration of femtosecond comb stabilized to the two clock transitions with frequencies ν_1 and ν_2 at a given temperature T .

quency ν_{m_0} is the synthetic frequency defined in Eq. (2),

$$\nu_{m_0} = \nu_{\text{syn}}^{(\text{comb})} = \frac{\nu_1^{(0)} - \varepsilon_{12}\nu_2^{(0)}}{1 - \varepsilon_{12}}, \quad (5)$$

as it should be. Here, m_0 is the natural number closest to the value of the right-hand side of Eq. (4). For this it is necessary to satisfy the condition $m_0 > 0$ that is equivalent to $\nu_{\text{syn}}^{(\text{comb})} > 0$ in Eq. (5).

Apart from the frequency ν_{m_0} which is a component of the optical spectrum of the frequency comb generator, in our system one can also define the much smaller frequency

$$\frac{\nu_{m_0}}{m_0} = f_r + \frac{f_0}{m_0} \quad (6)$$

which corresponds to a rf standard at ν_{m_0}/m_0 . Since the frequencies f_r and f_0 can be extracted from a stabilized comb generator with negligible error, one can use them to synthesize ν_{m_0}/m_0 . This synthesized radiofrequency has the same immunity to BBRs as ν_{m_0} . It is interesting to note that the radiofrequency given in Eq. (6) is well-defined in our system even if $m_0 < 0$ in Eq. (4), i.e., if the basic frequency component ν_{m_0} exists only virtually.

As was shown above, in the case of a frequency comb stabilized to two BBR-shifted clock transitions with frequencies $\nu_1(T)$ and $\nu_2(T)$, there exists a frequency component ν_{m_0} (for $m_0 > 0$) for which the thermal shift and the sensitivity to temperature fluctuations vanish. This frequency component can serve as an atomic frequency standard. In practice, the BBRs is strongly suppressed for a range of comb frequencies around ν_{m_0} . The residual shift of frequency components $\nu_{m_0 \pm l}$ near ν_{m_0} is given by:

$$\begin{aligned} \nu_{m_0 \pm l} &= \nu_{m_0} \pm l f_r \\ &= \nu_{m_0} \pm l \frac{\nu_2^{(0)} - \nu_1^{(0)}}{n_2 - n_1} \pm l \frac{a_2 - a_1}{n_2 - n_1} \left(\frac{T}{T_0} \right)^4. \end{aligned} \quad (7)$$

This indicates that the suppression is effective as long as $(n_2 - n_1) \gg l$. For example, for frequencies $\nu_1^{(0)}$ and $\nu_2^{(0)}$ in the optical range, the comb mode index difference

$(n_2 - n_1)$ will typically be in the range of 10^5 or higher (see the discussion for the case of $^{171}\text{Yb}^+$ below). On the whole, the choice of the exact value of the synthetic frequency ν_{syn} is to some extent arbitrary if one takes into account that the coefficient ε_{12} is only known with limited accuracy and that Eq. (1) is an approximation that neglects higher-order terms in the temperature dependence of the BBRS [18]. Including higher-order terms the BBRS can be expressed as:

$$\Delta^{(j)}(T) = a_j \left(\frac{T}{T_0}\right)^4 + b_j \left(\frac{T}{T_0}\right)^6 + \dots \quad (j = 1, 2). \quad (8)$$

From this we can estimate a basic limitation of the possibility to suppress the BBRS and its temperature dependence. Usually, near room temperature $T_0 = 300$ K the contribution of the higher terms $[b_j(T/T_0)^6 + \dots]$ is a factor of 10 to 10^3 smaller than that of the main T^4 -term [6, 19]. This indicates that here it would not be useful to suppress the T^4 -dependence of ν_{syn} to better than one to three orders of magnitude because higher-order contributions to the BBRS remain uncompensated. For example, in order to achieve a suppression factor of 10^2 for the T^4 -dependence, it would be sufficient to know the coefficient ε_{12} with relative uncertainty of 10^{-2} .

It may be noted that apart from theoretical calculations the coefficient ε_{12} can be determined by purely experimental means. To do this we can apply a quasistatic electric field (or the field of an infrared laser) to determine the shifts of the reference transition frequencies ν_1 and ν_2 due to the differences in the static polarizabilities of the involved atomic energy levels. From a practical point of view it is very advantageous that we do not need to know the magnitude of the electric field at the place of the atoms because we only have to determine the ratio a_1/a_2 . If a frequency comb generator is stabilized to ν_1 and ν_2 as shown in Fig.1, the frequency ν_{m_0} can be identified in a direct way as the frequency component which does not experience any scalar Stark shift in the applied quasistatic field.

As an example that permits the practical realization of the ideas presented above, we consider the ion $^{171}\text{Yb}^+$. As shown in Fig.2, the level system of $^{171}\text{Yb}^+$ provides two narrow-linewidth transitions from the ground state in the visible spectral range which can be used as reference transitions of an optical frequency standard: the quadrupole transition $^2\text{S}_{1/2}(F=0) \rightarrow ^2\text{D}_{3/2}(F=2)$, $\lambda \approx 436$ nm and the octupole transition $^2\text{S}_{1/2}(F=0) \rightarrow ^2\text{F}_{7/2}(F=3)$, $\lambda \approx 467$ nm. More detailed information on the spectroscopy of these transitions can be found in [15–17, 20]. It may be noted that the case of $^{171}\text{Yb}^+$ is especially attractive because here both clock transitions lie in a technically convenient frequency range and experience exactly the same thermal environment if probed in one ion.

The BBRS of the quadrupole and octupole transitions of Yb^+ were calculated in Ref. [21]. This

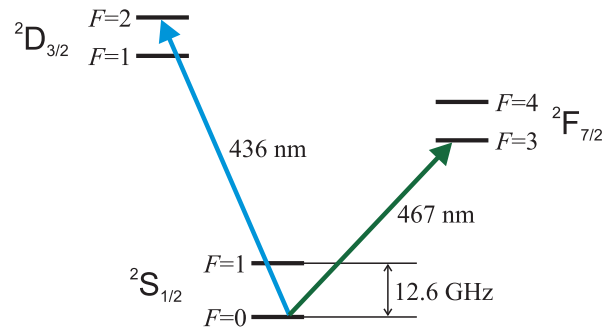


FIG. 2: (Color online) Section of the energy level scheme of $^{171}\text{Yb}^+$, showing the hyperfine levels of the $^2\text{S}_{1/2}$ ground state and the two lowest-lying excited states, which are metastable. Hyperfine splittings are not drawn to scale.

calculation is based on calculated oscillator strengths and experimental lifetime and polarizability data. The room-temperature BBRS of the quadrupole transition is calculated as $a_{\text{quad}} = -0.35(7)$ Hz (fractional shift $5.1(1.1) \times 10^{-16}$) and that of the octupole transition as $a_{\text{oct}} = -0.15(7)$ Hz (fractional shift $2.4(1.1) \times 10^{-16}$). The relatively small value of a_{oct} and the large relative uncertainty is due to nearly equal shifts of the $^2\text{S}_{1/2}$ and $^2\text{F}_{7/2}$ levels.

Using the results of Ref. [21], for $^{171}\text{Yb}^+$ we find that $\varepsilon_{12} = a_{\text{oct}}/a_{\text{quad}} = 0.43(22)$. We expect that the large uncertainty of this value can be reduced to less than 1% by improved atomic structure calculations or by a direct measurement of ε_{12} as discussed above. In the following, we will not take into account the present uncertainty because our conclusions remain qualitatively unchanged for all values of ε_{12} in this uncertainty range. In particular, we find the synthetic frequency $\nu_{\text{syn}}^{(\text{comb})} \approx 607$ THz, corresponding to a wavelength $\lambda_{\text{syn}} \approx 494$ nm. This frequency lies sufficiently close to the initial reference transitions at 436 nm and 467 nm that it can be generated as a spectral component of a femtosecond comb generator that is locked to the reference transitions as shown in Fig. 1.

The higher-order contributions in Eq.(8) to the BBRS of the octupole reference transition are negligible compared to that of the quadrupole transition. For the latter, we find $b/a \approx 0.1$ at $T_0 = 300$ K. As a result, we estimate that the BBRS can be suppressed to the fractional level of 2.7×10^{-17} at 300 K with variations at the level of $\pm 5 \times 10^{-18}$ if the ambient temperature varies in a broad interval of ± 15 K.

It is also possible to estimate the frequency interval around $\nu_{\text{syn}}^{(\text{comb})}$ where the components of the comb spectrum have a similar level of suppression of the thermal shift and of its fluctuations. For a suppression factor of 10^2 , this interval has a width of the order of 1000 GHz. Thus, for $d \sim 100$ MHz, the indicated interval contains 10^4 comb modes, each of which could be used as a stable frequency reference.

Other variants of BBRS-free optical frequency standards at a synthetic frequency can be conceived based on transitions $^1S_0 \rightarrow ^3P_0$ in alkaline-earth-like neutral atoms confined in an optical lattice. Consider, for instance, the combination of the reference transitions of strontium ($\nu_1 \approx 429$ THz, $\lambda \approx 698$ nm) and ytterbium ($\nu_2 \approx 518$ THz, $\lambda \approx 578$ nm). Using the calculations in Ref. [22], in this case we obtain $\varepsilon_{12} \approx 1.69$ and an estimated synthetic frequency $\nu_{\text{syn}}^{(\text{comb})} \approx 648$ THz ($\lambda_{\text{syn}} \approx 463$ nm). The technical realization of this variant requires the operation of two lattice-based clocks with different atoms (Sr and Yb) in the same vacuum chamber.

So far we have considered examples where both reference transition frequencies lie in the optical region. However, it is also possible to realize schemes where the high frequency ν_2 is optical, but the lower frequency ν_1 corresponds to a fine- or hyperfine-structure splitting so that it lies in the terahertz or microwave range. In contrast to the above example of ion Yb^+ , which seems unique because it provides two optical reference transitions, in this case one can find many appropriate schemes that use a single atomic species. Also the ion $^{171}\text{Yb}^+$ offers the possibility of using the ground-state hyperfine transition $F = 0 \rightarrow F = 1$ at $\nu_1 = 12.6$ GHz (see Fig.2) as a low-frequency reference transition. For the combination with the octupole transition $^2S_{1/2}(F = 0) \rightarrow ^2F_{7/2}(F = 3)$ at $\nu_2 = 642$ THz, a numerical estimate yields $\varepsilon_{12} \approx 6.6 \times 10^{-5}$ and a synthetic frequency $\nu_{\text{syn}} = -(\nu_1 - \varepsilon_{12}\nu_2) \approx 30$ GHz. (We expect that our estimate on ε_{12} is accurate to $\pm 20\%$, but it is not principal for further results.) Here the T^6 -contribution to the BBRS (see Eq.(8)) limits the BBRS suppression at the fractional level of 7.5×10^{-19} at $T = 300$ K with variations of $\pm 2 \times 10^{-19}$ in the temperature interval of 300 ± 15 K. However, we should also take into account the shift of the ground-state hyperfine levels ($\propto T^2$) due to the magnetic blackbody radiation field [6]. The corresponding BBRS of the hyperfine frequency $F = 0 \rightarrow F = 1$ for $^{171}\text{Yb}^+$ is:

$$\Delta_{\text{magn}}^{(1)}(T) = -1.616 \times 10^{-7} \times \left(\frac{T(\text{K})}{300} \right)^2 \text{ Hz.} \quad (9)$$

For $\nu_{\text{syn}} = 30$ GHz this shift results in a fractional level of 5.4×10^{-18} at $T = 300$ K with a variation of $\pm 5 \times 10^{-19}$ for 300 ± 15 K. Since the magnetic BBRS contribution can be readily calculated with an accuracy of less than 1%, it is possible to apply a corresponding correction to ν_{syn} with an uncertainty contribution of less than 10^{-19} .

For $^{171}\text{Yb}^+$ we have thus shown the possibility to create a synthetic-frequency-based atomic clock with a fractional uncertainty contribution due to BBRS of $< 1.5 \times 10^{-18}$ in a broad interval of 300 ± 15 K. To achieve this, we need to know the coefficient ε_{12} with a relative accuracy in the range of 0.1-0.2%. In order to reduce the BBRS uncertainty contribution to less than 10^{-17} , the

value of ε_{12} needs only be known with a relative accuracy of 3%. We also have pointed out that for $^{171}\text{Yb}^+$ the combination of the octupole optical clock transition with the ground-state hyperfine transition can yield a much better BBRS suppression than the combination of the octupole and quadrupole optical clock transitions. The use of the quadrupole transition yields a lower BBRS suppression because the upper level $^2D_{3/2}$ is connected to the $^2P_{1/2}$ level by a strong infrared transition at $2.44 \mu\text{m}$, which produces a relatively large T^6 -contribution to the BBRS. The final comparison of the two options for BBRS suppression should also include detailed estimates on the magnitudes of other systematic uncertainty contributions in the considered experimental setup.

The concept of a synthetic atomic frequency standard based on two reference transitions can also be extended to the case that both reference frequencies $\nu_{1,2}$ lie in the microwave range. Atomic fountain clocks are based on reference transitions in the microwave range between the ground-state hyperfine sublevels of alkali atoms. For a synthetic atomic fountain frequency standard, for instance the combination ^{87}Rb ($\nu_1 \approx 6.8$ GHz) and ^{133}Cs ($\nu_2 \approx 9.2$ GHz) can be considered. Here, at the synthetic frequency ($\nu_1 - \varepsilon_{12}\nu_2$) ≈ 1.9 GHz it is possible to suppress the fractional BBRS of the individual standards by two orders of magnitude. It is interesting to note that nearly optimal conditions for the efficient suppression of the BBRS are realized in the dual Rb/Cs fountain clock described in Ref. [23] because here both reference transitions are exposed to the same thermal environment.

We finally note that the $^{171}\text{Yb}^+$ optical frequency standard is a very sensitive system for a search for temporal variations of the fine structure constant α [24, 25]. The frequencies of the quadrupole and octupole reference transitions of Yb^+ have significant contributions from relativistic effects and would undergo changes with different sign in consequence of a change of α . The synthetic frequency that eliminates the BBRS retains this sensitivity. The α -dependence of an atomic transition frequency may be expressed generally as $\nu = \nu_0 + qx$, where $x \equiv (\alpha/\alpha_0)^2 - 1$, ν_0 defines the frequency at the present value of the fine structure constant, α_0 , and q quantifies the sensitivity to changes of α [24]. The q parameter for the synthetic frequency is simply given by $q_{\text{syn}} = (q_1 - \varepsilon_{12}q_2)/(1 - \varepsilon_{12})$. For Yb^+ , with q parameters as given in Ref. [24], q_{syn} amounts to about -3220 THz. Comparison with the Yb^+ synthetic frequency $\nu_{\text{syn}}^{(\text{comb})} \approx 607$ THz indicates the strong sensitivity. In a test for variations of α , the synthetic frequency would have to be compared to an ‘‘anchor’’ reference transition with small q value, like the $^1S_0 \rightarrow ^3P_0$ transition in Al^+ .

In conclusion, we have proposed and developed the concept of an atomic frequency standard where the frequency shift due to the ambient blackbody radiation and related fluctuations of the output frequency can be suppressed by one to three orders of magnitude without us-

ing cryogenic techniques. We also expect that our results will stimulate refined atomic structure calculations on Yb^+ and other atomic systems that are of interest in this context. Such calculations can yield precise values for the frequency synthesis parameter ε_{12} and determine limitations of the achievable BBRS suppression.

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